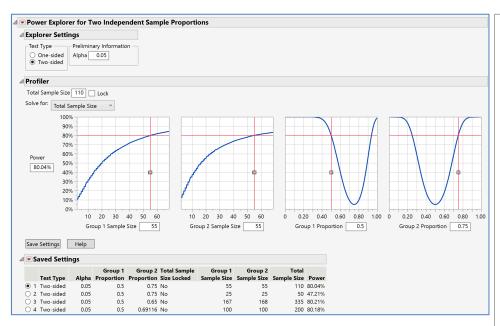


## Sample Size and Power for Two Sample Proportions

Use to interactively explore the relationships between Power, Sample Sizes, and Alternative Proportions in testing a hypothesis comparing two independent population proportions. See the Two Proportions Test and Confidence Interval guide to learn how to perform a statistical test comparing two population proportions.

## Sample Size and Power - Two Sample Proportion

- 1. Select DOE > Sample Size Explorers and choose Power > Power for Two Independent Sample Proportions.
- Choose the type of test: **One-Sided** or **Two-Sided** and choose **Alpha** (significance level for the test). The Null Hypothesis is that the two proportions are equal. Here we chose a two-sided alternative which is used to test that the two proportions are not equal.
  - This null and alternative hypothesis can be written using notation as  $H_0$ :  $p_1 = p_2$  vs.  $H_A$ :  $p_1 \neq p_2$
- 3. Enter values for the **Group 1** and **Group 2 Population Proportions** under H<sub>A</sub> to base the analysis on. Here we consider the scenario where **Proportion 1** is 0.50 and **Proportion 2** is 0.75. Solve for: Total Sample Size
- 4. Select parameter to solve for. Here we chose Total Sample Size.
- 5. Enter a value for the **Power**. Here we entered 0.80. The solution of Total Sample Size of 110 ( $n_1$ =55 and  $n_2$ =55) is displayed.
- 6. Use the interactive cross-hair tool (or type in values) for Power, Sample Sizes, and Assumed Proportions to study the relationship between these parameters solving for many different scenarios.



Note: Determining sample size to achieve a desired margin of error in a Confidence Interval can be done using DOE > Sample Size Explorers > **Confidence Intervals > Margin of Error for Two Independent Sample** Proportions.

The settings and solution for each analysis performed can be saved. The table of saved settings shows the results of five different analyses performed when testing the hypothesis  $H_0$ :  $p_1 = p_2$  vs.  $H_A$ :  $p_1 \neq p_2$ 

Total Sample Size

Group 1 Sample Size

Group 2 Sample Size Group 1 Proportion

Group 2 Proportion

- 1. What sample size is needed to achieve a power of 80% assuming  $p_1$ =0.50 and  $p_2$ =0.75? Answer: 110  $(n_1 = 55 \text{ and } n_2 = 55)$
- 2. What is the power with a sample size of 25 in each group assuming p<sub>1</sub>=0.50 and  $p_2$ =0.75? *Answer: Power = 47.2%*
- 3. What sample size is needed to achieve a power of 80% assuming  $p_1$ =0.50 and  $p_2$ =0.65? Answer: 335 ( $n_1 = 167$  and  $n_2 = 168$ )
- 4. What difference from 0.50 for the proportion of group 2 can be detected with 80% power using a sample size of 100 in each group?

Answer: 0.69