

## Version 16

# Quality and Process Methods

"The real voyage of discovery consists not in seeking new landscapes, but in having new eyes."

Marcel Proust

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## JMP® 16 Quality and Process Methods

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# Get the Most from JMP

Whether you are a first-time or a long-time user, there is always something to learn about JMP.

Visit JMP.com to find the following:

- live and recorded webcasts about how to get started with JMP
- video demos and webcasts of new features and advanced techniques
- details on registering for JMP training
- schedules for seminars being held in your area
- success stories showing how others use JMP
- the JMP user community, resources for users including examples of add-ins and scripts, a forum, blogs, conference information, and so on

https://www.jmp.com/getstarted

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# Chapter 1

# Learn about JMP

#### **Documentation and Additional Resources**

Learn about JMP documentation, such as book conventions, descriptions of each JMP document, the Help system, and where to find additional support.

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# **Formatting Conventions in JMP Documentation**

These conventions help you relate written material to information that you see on your screen:

- Sample data table names, column names, pathnames, filenames, file extensions, and folders appear in Helvetica (or sans-serif online) font.
- Code appears in Lucida Sans Typewriter (or monospace online) font.
- Code output appears in *Lucida Sans Typewriter* italic (or monospace italic online) font and is indented farther than the preceding code.
- Helvetica bold formatting (or bold sans-serif online) indicates items that you select to complete a task:
  - buttons
  - check boxes
  - commands
  - list names that are selectable
  - menus
  - options
  - tab names
  - text boxes
- The following items appear in italics:
  - words or phrases that are important or have definitions specific to JMP
  - book titles
  - variables
- Features that are for JMP Pro only are noted with the JMP Pro icon property of JMP Pro features, visit https://www.jmp.com/software/pro.

**Note:** Special information and limitations appear within a Note.

**Tip:** Helpful information appears within a Tip.

## JMP Help

JMP Help in the Help menu enables you to search for information about JMP features, statistical methods, and the JMP Scripting Language (or *JSL*). You can open JMP Help in several ways:

- Search and view JMP Help on Windows by selecting Help > JMP Help.
- On Windows, press the F1 key to open the Help system in the default browser.
- Get help on a specific part of a data table or report window. Select the Help tool ?? from
  the Tools menu and then click anywhere in a data table or report window to see the Help
  for that area.
- Within a JMP window, click the Help button.

**Note:** The JMP Help is available for users with Internet connections. Users without an Internet connection can search all books in a PDF file by selecting **Help > JMP Documentation Library**. See "JMP Documentation Library" for more information.

# **JMP Documentation Library**

The Help system content is also available in one PDF file called *JMP Documentation Library*. Select **Help > JMP Documentation Library** to open the file. You can also download the Documentation PDF Files add-in if you prefer searching individual PDF files of each document in the JMP library. Download the available add-ins from <a href="https://community.jmp.com">https://community.jmp.com</a>.

The following table describes the purpose and content of each document in the JMP library.

Document Title	Document Purpose	Document Content
Discovering JMP	If you are not familiar with JMP, start here.	Introduces you to JMP and gets you started creating and analyzing data. Also learn how to share your results.
Using JMP	Learn about JMP data tables and how to perform basic operations.	Covers general JMP concepts and features that span across all of JMP, including importing data, modifying columns properties, sorting data, and connecting to SAS.

<b>Document Title</b>	<b>Document Purpose</b>	Document Content
Basic Analysis	Perform basic analysis using this document.	Describes these Analyze menu platforms:
		Distribution
		• Fit Y by X
		• Tabulate
		Text Explorer
		Covers how to perform bivariate, one-way ANOVA, and contingency analyses through Analyze > Fit Y by X. How to approximate sampling distributions using bootstrapping and how to perform parametric resampling with the Simulate platform are also included.
Essential Graphing	Find the ideal graph	Describes these Graph menu platforms:
	for your data.	Graph Builder
		• Scatterplot 3D
		• Contour Plot
		• Bubble Plot
		Parallel Plot
		• Cell Plot
		• Scatterplot Matrix
		• Ternary Plot
		• Treemap
		• Chart
		Overlay Plot
		The book also covers how to create background and custom maps.
Profilers	Learn how to use interactive profiling tools, which enable you to view cross-sections of any response surface.	Covers all profilers listed in the Graph menu. Analyzing noise factors is included along with running simulations using random inputs.

Document Title	<b>Document Purpose</b>	Document Content
Design of Experiments Guide	Learn how to design experiments and determine appropriate sample sizes.	Covers all topics in the DOE menu.
Fitting Linear Models	Learn about Fit Model platform and many of its personalities.	Describes these personalities, all available within the Analyze menu Fit Model platform:
		Standard Least Squares
		• Stepwise
		<ul> <li>Generalized Regression</li> </ul>
		Mixed Model
		<ul> <li>MANOVA</li> </ul>
		Loglinear Variance
		Nominal Logistic
		Ordinal Logistic
		Generalized Linear Model

Document Title	Document Purpose	Document Content
Predictive and Specialized Modeling	Learn about additional modeling techniques.	Describes these Analyze > Predictive Modeling menu platforms:
		Neural
		• Partition
		Bootstrap Forest
		Boosted Tree
		K Nearest Neighbors
		Naive Bayes
		Support Vector Machines
		Model Comparison
		Model Screening
		Make Validation Column
		Formula Depot
		Describes these Analyze > Specialized Modeling menu platforms:
		• Fit Curve
		Nonlinear
		Functional Data Explorer
		Gaussian Process
		Time Series
		Matched Pairs
		Describes these Analyze > Screening menu platforms:
		<ul> <li>Modeling Utilities</li> </ul>
		Response Screening
		Process Screening
		Predictor Screening
		Association Analysis
		Process History Explorer

<b>Document Title</b>	<b>Document Purpose</b>	Document Content
Multivariate Methods	Read about techniques for analyzing several variables simultaneously.	Describes these Analyze > Multivariate Methods menu platforms:
		Multivariate
		Principal Components
		Discriminant
		Partial Least Squares
		Multiple Correspondence Analysis
		Structural Equation Models
		Factor Analysis
		<ul> <li>Multidimensional Scaling</li> </ul>
		Item Analysis
		Describes these Analyze > Clustering menu platforms:
		Hierarchical Cluster
		K Means Cluster
		Normal Mixtures
		Latent Class Analysis
		Cluster Variables
Quality and Process Methods	Read about tools for evaluating and improving processes.	Describes these Analyze > Quality and Process menu platforms:
		<ul> <li>Control Chart Builder and individual control charts</li> </ul>
		Measurement Systems Analysis
		Variability / Attribute Gauge Charts
		<ul> <li>Process Capability</li> </ul>
		<ul> <li>Model Driven Multivariate Control Chart</li> </ul>
		Legacy Control Charts
		• Pareto Plot
		Diagram
		Manage Spec Limits
		• OC Curves

Document Title	Document Purpose	Document Content	
Reliability and Survival Methods	Learn to evaluate and improve reliability in a product or system and analyze survival data for people and products.	Describes these Analyze > Reliability and Survival menu platforms:	
		Life Distribution	
		• Fit Life by X	
		Cumulative Damage	
		Recurrence Analysis	
		Degradation	
		Destructive Degradation	
		Reliability Forecast	
		Reliability Growth	
		Reliability Block Diagram	
		Repairable Systems Simulation	
		• Survival	
		Fit Parametric Survival	
		Fit Proportional Hazards	
Consumer Research	Learn about methods for studying consumer preferences and using that insight to create better products and services.	Describes these Analyze > Consumer Research menu platforms:	
		Categorical	
		• Choice	
		• MaxDiff	
		• Uplift	
		Multiple Factor Analysis	
Scripting Guide	Learn about taking advantage of the powerful JMP Scripting Language (JSL).	Covers a variety of topics, such as writing and debugging scripts, manipulating data tables, constructing display boxes, and creating JMP applications.	
JSL Syntax Reference	Read about many JSL functions on functions and their arguments, and messages that you send to objects and display boxes.	Includes syntax, examples, and notes for JSL commands.	

## Additional Resources for Learning JMP

In addition to reading JMP help, you can also learn about JMP using the following resources:

- "JMP Tutorials"
- "Sample Data Tables"
- "Learn about Statistical and JSL Terms"
- "Learn JMP Tips and Tricks"
- "JMP Tooltips"
- "JMP User Community"
- "Free Online Statistical Thinking Course"
- "JMP New User Welcome Kit"
- "Statistics Knowledge Portal"
- "JMP Training"
- "JMP Books by Users"
- "The JMP Starter Window"

#### **JMP Tutorials**

You can access JMP tutorials by selecting **Help > Tutorials**. The first item on the **Tutorials** menu is **Tutorials Directory**. This opens a new window with all the tutorials grouped by category.

If you are not familiar with JMP, start with the **Beginners Tutorial**. It steps you through the JMP interface and explains the basics of using JMP.

The rest of the tutorials help you with specific aspects of JMP, such as designing an experiment and comparing a sample mean to a constant.

## **Sample Data Tables**

All of the examples in the JMP documentation suite use sample data. Select **Help > Sample Data Library** to open the sample data directory.

To view an alphabetized list of sample data tables or view sample data within categories, select **Help > Sample Data**.

Sample data tables are installed in the following directory:

On Windows: C:\Program Files\SAS\JMP\16\Samples\Data

On macOS: \Library\Application Support\JMP\16\Samples\Data

In JMP Pro, sample data is installed in the JMPPRO (rather than JMP) directory.

To view examples using sample data, select **Help > Sample Data** and navigate to the Teaching Resources section. To learn more about the teaching resources, visit <a href="https://jmp.com/tools">https://jmp.com/tools</a>.

#### **Learn about Statistical and JSL Terms**

For help with statistical terms, select Help > Statistics Index. For help with JSL scripting and examples, select **Help > Scripting Index**.

**Statistics Index** Provides definitions of statistical terms.

**Scripting Index** Lets you search for information about JSL functions, objects, and display boxes. You can also edit and run sample scripts from the Scripting Index and get help on the commands.

## **Learn JMP Tips and Tricks**

When you first start JMP, you see the Tip of the Day window. This window provides tips for using JMP.

To turn off the Tip of the Day, clear the **Show tips at startup** check box. To view it again, select **Help > Tip of the Day**. Or, you can turn it off using the Preferences window.

## **JMP Tooltips**

JMP provides descriptive tooltips (or *hover labels*) when you hover over items, such as the following:

- Menu or toolbar options
- Labels in graphs
- Text results in the report window (move your cursor in a circle to reveal)
- Files or windows in the Home Window
- Code in the Script Editor

**Tip:** On Windows, you can hide tooltips in the JMP Preferences. Select **File > Preferences > General** and then deselect **Show menu tips**. This option is not available on macOS.

## **JMP User Community**

The JMP User Community provides a range of options to help you learn more about JMP and connect with other JMP users. The learning library of one-page guides, tutorials, and demos is a good place to start. And you can continue your education by registering for a variety of JMP training courses.

Other resources include a discussion forum, sample data and script file exchange, webcasts, and social networking groups.

To access JMP resources on the website, select **Help > JMP User Community** or visit https://community.jmp.com.

## **Free Online Statistical Thinking Course**

Learn practical statistical skills in this free online course on topics such as exploratory data analysis, quality methods, and correlation and regression. The course consists of short videos, demonstrations, exercises, and more. Visit <a href="https://www.jmp.com/statisticalthinking">https://www.jmp.com/statisticalthinking</a>.

#### JMP New User Welcome Kit

The JMP New User Welcome Kit is designed to help you quickly get comfortable with the basics of JMP. You'll complete its thirty short demo videos and activities, build your confidence in using the software, and connect with the largest online community of JMP users in the world. Visit <a href="https://www.jmp.com/welcome">https://www.jmp.com/welcome</a>.

## **Statistics Knowledge Portal**

The Statistics Knowledge Portal combines concise statistical explanations with illuminating examples and graphics to help visitors establish a firm foundation upon which to build statistical skills. Visit <a href="https://www.jmp.com/skp">https://www.jmp.com/skp</a>.

## **JMP Training**

SAS offers training on a variety of topics led by a seasoned team of JMP experts. Public courses, live web courses, and on-site courses are available. You might also choose the online e-learning subscription to learn at your convenience. Visit <a href="https://www.jmp.com/training">https://www.jmp.com/training</a>.

## JMP Books by Users

Additional books about using JMP that are written by JMP users are available on the JMP website. Visit <a href="https://www.jmp.com/books">https://www.jmp.com/books</a>.

#### The JMP Starter Window

The JMP Starter window is a good place to begin if you are not familiar with JMP or data analysis. Options are categorized and described, and you launch them by clicking a button. The JMP Starter window covers many of the options found in the Analyze, Graph, Tables, and File menus. The window also lists JMP Pro features and platforms.

- To open the JMP Starter window, select View (Window on macOS) > JMP Starter.
- To display the JMP Starter automatically when you open JMP on Windows, select File >
   Preferences > General, and then select JMP Starter from the Initial JMP Window list. On
   macOS, select JMP > Preferences > Initial JMP Starter Window.

# **JMP Technical Support**

JMP technical support is provided by statisticians and engineers educated in SAS and JMP, many of whom have graduate degrees in statistics or other technical disciplines.

Many technical support options are provided at https://www.jmp.com/support, including the technical support phone number.

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# **Introduction to Quality and Process Methods**

#### **Tools for Process and Product Improvement**

Quality and Process Methods describes a number of methods and tools that are available in JMP to help you evaluate and improve quality and process performance:

- Control charts provide feedback on key variables and show when a process is in, or out of, statistical control. "Control Chart Builder" describes the JMP approach to creating control charts using an interactive control chart platform called Control Chart Builder.
- The Measurement Systems Analysis platform assesses the precision, consistency, and bias of a system. Before you can study a process, you need to make sure that you can accurately and precisely measure the process. If variation comes from the measurement itself, then you are not reliably learning about the process. Use this analysis to find out how your system is performing. See "Measurement Systems Analysis".
- The Variability/Attribute Gauge Chart platform creates variability or attribute gauge
  charts. Variability charts analyze continuous measurements and reveal how your system is
  performing. Attribute charts analyze categorical measurements and show you measures of
  agreement across responses. You can also perform a gauge study to see measures of
  variation in your data. See "Variability Gauge Charts" and "Attribute Gauge Charts".
- The Process Capability platform measures the ability of a process to meet specification limits. You can compare process performance, summarized by process centering and variability, to specification limits. The platform calculates capability indices based on both long-term and short-term variation. The analysis helps identify the variation relative to the specifications; this enables you to achieve increasingly higher conformance values. See "Process Capability".
- CUSUM charts enable you to make decisions based on the cumulative sum. These charts can detect small shifts in a process. See "CUSUM Control Charts".
- Exponentially weighted moving average (EWMA) charts can also be used to detect small shifts in a process. See "EWMA Control Charts".
- When you need to monitor multiple process characteristics simultaneously, see "Multivariate Control Charts".
- The Model Driven Multivariate Control Chart (MDMVCC) platform enables you to build a
  control chart based on principal components or partial least squares models. See "Model
  Driven Multivariate Control Charts".
- "Legacy Control Charts" describes the older control chart platforms in JMP. Instead of
  using these platforms, you are encouraged to use the Control Chart Builder platform, as
  well as the new CUSUM and EWMA Control Chart platforms.

- The Pareto Plot platform shows the frequency of problems in a quality related process or operation. Pareto plots help you decide which problems to solve first by highlighting the frequency and severity of problems. See "Pareto Plots".
- The Diagram platform constructs cause-and-effect diagrams, which organize the sources
  of a problem for brainstorming or as a preliminary analysis to identify variables for further
  experimentation. Once complete, further analysis can be done to identify the root cause of
  the problem. See "Cause-and-Effect Diagrams".
- The Manage Spec Limits utility enables you to quickly add or edit many specification limits for several columns at once. See "Manage Spec Limits Utility".
- The Operating Characteristic (OC) Curves utility enables you to construct OC curves for control charts and attribute acceptance sampling plans. See "Operating Characteristic Curves Utility".

## **Control Chart Builder**

#### **Create Control Charts Interactively**

A control chart is a graphical and analytic tool for monitoring process variation. The natural variation in a process can be quantified using a set of control limits. Control limits help distinguish common-cause variation from special-cause variation. Typically, action is taken to identify and eliminate special-cause variation. It is also important to quantify the common-cause variation in a process, as this determines the capability of a process.

Use Control Chart Builder to create control charts of your process data. Control Chart Builder can be launched as an interactive workspace or from specific control chart menu options. In the interactive workspace, you select the variables that you want to chart and drag them into zones. JMP automatically chooses an appropriate chart type based on the data. You can quickly create another type of chart, or change the current settings for an existing chart.

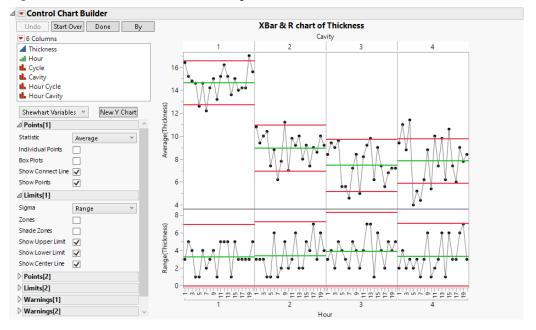


Figure 3.1 Control Chart Builder Example

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## **Overview of Control Chart Builder**

A control chart is a graphical and analytic tool for monitoring process variation and identifying special-cause variation in a process. Establishing control limits to filter out routine variation helps determine whether a process is stable and predictable. If the variation in a process is more than desired, the process can be adjusted to create higher quality output with potential cost savings.

All processes exhibit measurement variation as the process is monitored over time. There are two types of variation in process measurements:

- Routine or common-cause variation. Measurements from a stable process still exhibit random variation. When process measurements exhibit only common-cause variation, the measurements stay within expected limits.
- Abnormal or special-cause variation. Special-cause variation is indicated by patterns
  observed on the control chart. Examples include a shift in the process mean, points above
  or below the control limits, or measurements that trend up or down. These shifts in the
  process measurements can be caused by factors such as a broken tool or machine,
  equipment degradation, or changes to raw materials. A change or defect in the process is
  often identifiable by abnormal variation in the process measurements.

Control Chart Builder enables you to create several types of control charts including Shewhart and Rare Event control charts. Shewhart control charts are broadly classified into control charts for variables and control charts for attributes. Rare event charts are designed for events that occur infrequently. JMP provides a flexible, user-defined approach to building control charts. You can construct control charts in the following ways:

- Use the interactive Control Chart Builder workspace. When you drag a data column to the
  workspace, Control Chart Builder creates an appropriate chart based on the data type and
  sample size.
- Use the control chart menu options to build a specific control chart using a launch window.

Once an initial chart is created through either method above, use the menus and other options to change the type of chart, change the statistic on the chart, reformat the chart, or add additional charts.

# **Example of Control Chart Builder**

The Socket Thickness.jmp sample data table contains measurements for the thickness of sockets. There has been an increase in the number of defects during production and you want to investigate why this is occurring. This example illustrates how to perform this investigation in Control Chart Builder using either the interactive approach or the launch window approach. The second approach is convenient if you know which type of control chart you want to build.

#### Control Chart Builder Interactive Method

Use the interactive Control Chart Builder workspace to investigate the variability in the process data.

- Select Help > Sample Data Library and open Quality Control/Socket Thickness.jmp.
- 2. Select Analyze > Quality and Process > Control Chart Builder.
- 3. Drag Thickness to the Y zone.
- 4. Drag Hour to the **Subgroup** zone (at bottom).

XBar & R chart of Thickness 11.5 ☐ Thickness Limit Summaries Points Limits Subgroup 11.0 UCL Sigma LCL plotted Avg Size 10.5 7.788772 9.7375 11.68623 Range 20 4.499516 10.85 17.20048 Range 20 10.0 Average(Thickness 9.5 9.0 8.5 8.0 7.5 7.0 16 Range(Thickness) 14 12 10 8 9 10 11 12 13 14 15 16 17 18 19 20

Figure 3.2 Control Charts for Socket Thickness

Looking at the Average chart, you can see that there are several points below the lower control limit of 7.788772. You want to see whether another variable might be contributing to the problem.

- 5. Drag Cavity into the **Phase** zone.
- 6. Click Done.

✓ Control Chart Builder XBar & R chart of Thickness Cavity Points Limits plotted Cavity LCL **UCL Sigma** 16 12,7465 14.65 16.5535 Range Average 6.979973 8.97 10.96003 Range Average 2 5.191564 7.47 9.748436 Range Average 3 Average(Thickness) Average 7.86 9.792345 Range 5.927655 12 Range 0 3.3 6.977847 Range Range 3.45 7.295022 Range 0 10 Range 3.95 8.352272 Range Range 3.35 7.083572 Range 8 Range(Thickness) 

**Figure 3.3** Control Charts for Each Cavity

From the Average chart, you can conclude the following:

- There are differences between the cavities, indicating the need for separate control limits for each cavity.
- Cavity 1 is producing sockets with an average thickness above that of the other cavities. This indicates that further investigation of the differences between cavities is warranted.
- All of the cavities have points that are outside the control limits. Therefore, you should investigate the lack of control in the process for each cavity.

The Range chart for each cavity shows that the within-subgroup measurements are in control and are similar across cavities.

#### Control Chart Builder Launch Window Method

Use the XBar Control Chart launch window to obtain the same chart as Figure 3.3.

- Select Help > Sample Data Library and open Quality Control/Socket Thickness.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > XBar Control Chart.
- 3. Select Thickness and click Y.
- 4. Select Hour and click **Subgroup**.
- Select Cavity and click Phase.
- 6. Click OK.

You should see the same control chart that appears in Figure 3.3.

# **Control Chart Types**

Control Chart Builder enables you to create several types of control charts, including Shewhart Variable, Shewhart Attribute, and Rare Event charts.

- "Shewhart Control Charts for Variables"
- "Shewhart Control Charts for Attributes"
- "Rare Event Control Charts"
- "Control Chart Types"

#### **Shewhart Control Charts for Variables**

Control charts for variables are classified according to the subgroup summary statistic plotted on the chart.

- XBar charts are a type of location chart that display subgroup means (averages).
- R charts are a type of dispersion chart that display subgroup ranges (maximum minimum).
- S charts are a type of dispersion chart that display subgroup standard deviations.
- Individual Measurement charts are a type of location chart that display individual measurements.
- Run charts are a type of location chart that display individual measurements as a connected series of points.
- Presummarize charts display both subgroup means and standard deviations.
- Moving Range charts are a type of dispersion chart that display moving ranges of two successive measurements.

**Note:** If you remove a dispersion chart or turn off the preference Show Two Shewhart Charts in File > Preferences > Platforms > Control Chart Builder, you will see only the location chart. Any associated scripts will contain the JSL option Show Two Shewhart Charts set to off (0).

#### XBar, R, and S Charts

For quality characteristics measured on a continuous scale, a typical analysis shows both the process mean and its variability with a mean chart aligned above its corresponding R or S chart.

#### **Individual Measurement Charts**

Individual Measurement charts displays individual measurements. Individual Measurement charts are appropriate when only one measurement is available for each sampling time point. If you are charting individual measurements, the individual measurement chart shows above its corresponding moving range chart. Moving Range charts displays moving ranges of two successive measurements.

#### **Presummarize Charts**

If your data consist of repeated measurements of the same process unit, you can combine these into one measurement for the unit. Pre-summarizing is not recommended unless the data contain repeated measurements on each process or measurement unit.

Presummarize summarizes the process column into sample means and/or standard deviations, based either on the sample size or sample label chosen. Then it charts the summarized data based on the options chosen in the window.

#### **Levey-Jennings Charts**

Levey-Jennings charts show a process mean with control limits based on a long-term sigma. The control limits are placed at 3s distance from the center line. The standard deviation, s, for the Levey-Jennings chart is calculated the same way standard deviation is in the Distribution platform.

#### **Shewhart Control Charts for Attributes**

Attributes charts are applicable for count data. Attribute charts are based on binomial and Poisson models. Because the counts are measured per subgroup, it is important when comparing multiple charts to determine whether you have a similar number of items in the subgroups between the charts. Attribute charts, like variables charts, are classified according to the subgroup sample statistic plotted on the chart.

**Table 3.1** Attribute Chart Determination

Distribution Used to Calculate Sigma	Statistic Type: Proportion	Statistic Type: Count
Binomial	P chart	NP chart
Poisson	U chart	C chart

Control Chart Builder makes some decisions for you based on the variable selected. Once the basic chart is created, you can use the menus and other options to change the type, the statistic, and the format of the chart.

- P charts display the proportion of nonconforming (defective) items in subgroup samples, which can vary in size. Because each subgroup for a P chart consists of N<sub>i</sub> items, and an item is judged as either conforming or nonconforming, the maximum number of nonconforming items in a subgroup is N<sub>i</sub>.
- NP charts display the number of nonconforming (defective) items in subgroup samples. Because each subgroup for an NP chart consists of  $N_i$  items, and an item is judged as either conforming or nonconforming, the maximum number of nonconforming items in subgroup i is  $N_i$ .
- C charts display the number of nonconformities (defects) in a subgroup sample that usually, but does not necessarily, consists of one inspection unit.
- U charts display the number of nonconformities (defects) per unit in subgroup samples that can have a varying number of inspection units.

## **Rare Event Control Charts**

A Rare Event chart is a control chart that provides information about a process where the data comes from rarely occurring events. Tracking processes that occur infrequently on a traditional control chart tend to be ineffective. Rare event charts were developed in response to the limitations of control charts in rare event scenarios. Control Chart Builder provides two types of rare event charts (G charts and T charts). The difference between a G chart and a T chart is the quantity used to measure distance between rare events. The G chart measures counts of events between incidents, whereas the T chart measures time intervals between incidents.

**Table 3.2** Rare Event Chart Determination Based on Sigma

Distribution Used to Calculate Sigma	Chart Type
Negative Binomial	G chart
Weibull	T chart

Chapter 3

#### G charts

A G chart measures the number of events between rarely occurring errors or nonconforming incidents, and creates a chart of a process over time. Each point on the chart represents the number of units between occurrences of a relatively rare event. For example, in a production setting, where an item is produced daily, an unexpected line shutdown can occur. You can use a G chart to look at the number of units produced between line shutdowns.

When reading a G chart, the points above the upper control limit indicate that the number of events between errors has increased. If the number of events between rarely occurring errors or nonconforming incidents has increased, that is good. Therefore, a point flagged as out of control above the limits is generally considered a desirable effect when working with G charts.

#### T charts

A T chart measures the time intervals elapsed since the last event. Each point on the chart represents a number of time intervals that have passed since a prior occurrence of a rare event. A T chart can be used for numeric, nonnegative data, date/time data, and time-between data. Since a traditional plot of these data might contain many points at zero and an occasional point at one, using a T chart avoids flagging numerous points as out of control. The data points for a T chart in Control Chart Builder are restricted to integer values.

When reading a T chart, the points above the upper control limit indicate that the amount of time between events has increased. This means that the rate of adverse events has decreased. Therefore, a point flagged as out of control above the limits is generally considered a desirable effect when working with T charts.

## **Control Chart Types**

The most common control charts are available in Control Chart Builder and in the platforms in the Analyze > Quality and Process > Control Chart menu. Use Control Chart Builder as your first choice to easily and quickly generate charts. JMP automatically chooses the appropriate chart type based on the data. Table 3.3 through Table 3.7 summarize the different control chart types.

**Table 3.3** Variable Charts Without Grouping (X) Variable or Nonsummarized Data

Chart Types	Control Chart Builder Options	
	Points > Statistic	Limits > Sigma
Individual	Individual	Moving Range
Moving Range on Individual	Moving Range	Moving Range

Table 3.3 Variable Charts Without Grouping (X) Variable or Nonsummarized

Control Chart Builder Options	
Points > Statistic	Limits > Sigma
Individual	Median Moving Range
Moving Range	Median Moving Range
Individual	Levey Jennings
	Points > Statistic  Individual  Moving Range

Table 3.4 Variable Charts with Grouping (X) Variables or Summarized Data

Chart Types	Control Chart Builder Options	
	Points > Statistic	Limits > Sigma
XBar (limits computed on range)	Average	Range
XBar (limits computed on standard deviation)	Average	Standard Deviation
R	Range	Range
S	Standard Deviation	Standard Deviation
Levey Jennings	Average	Levey Jennings or overall Standard Deviation

Table 3.5 Presummarize Charts

Chart Types	Control Chart Builder Options	
	Points > Statistic	Limits > Sigma
Individual on Group Means	Average	Moving Range
Individual on Group Means (limits computed on median moving range)	Average	Median Moving Range
Individual on Group Std Devs	Standard Deviation	Moving Range

 Table 3.5 Presummarize Charts (Continued)

Chart Types	Control Chart Builder Options	
	Points > Statistic	Limits > Sigma
Individual on Group Std Devs (limits computed on median moving range)	Standard Deviation	Median Moving Range
Moving Range on Group Means	Moving Range on Means	Moving Range
Median Moving Range on Group Means	Moving Range on Mean	Median Moving Range
Moving Range on Group Std Devs	Moving Range on Std Dev	Moving Range
Median Moving Range on Group Std Devs	Moving Range on Std Dev	Median Moving Range

**Table 3.6** Attribute Charts

Chart Types	Control Chart Builder Options	
	Points > Statistic	Limits > Sigma
P chart	Proportion	Binomial
NP chart	Count	Binomial
C chart	Count	Poisson
U chart	Proportion	Poisson

**Table 3.7** Rare Event Charts

Chart Types	Control Chart Builder Options	
	Points > Statistic	Limits > Sigma
G chart	Count	Negative Binomial
T chart	Count	Weibull

## **Launch Control Chart Builder**

You can launch Control Chart Builder in the following two ways:

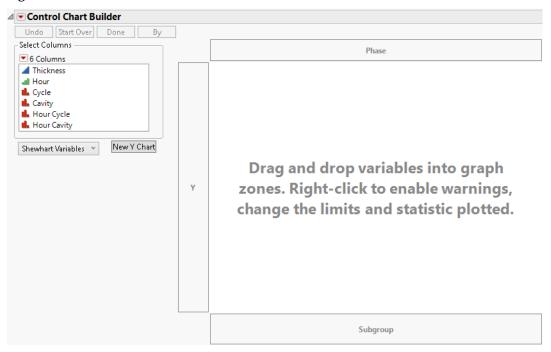
- If you are not sure what type of control chart is appropriate for your data, select Analyze >
   Quality and Process > Control Chart Builder. This method enables you to drag data
   columns to the workspace and Control Chart Builder creates an appropriate chart based
   on the data type and sample size. See "Control Chart Builder Interactive Workspace".
- If you know which type of control chart is appropriate for your data, select the appropriate
  chart from the Analyze > Quality and Process > Control Chart submenu. This displays a
  control chart launch window. See "Launch Windows for Specific Control Charts". There
  are control chart builder launch windows for the following control charts:
  - I/MR Control Chart
  - XBar Control Chart
  - Run Chart
  - P Control Chart
  - NP Control Chart
  - C Control Chart
  - U Control Chart
  - Levey Jennings Control Chart
  - I/MR on Means Control Chart
  - Three Way Control Chart

**Note:** The CUSUM Control Chart, EWMA, and Multivariate Control Charts launch in their own platforms instead of launching in Control Chart Builder, and are documented separately. See "CUSUM Control Charts", "Multivariate Control Charts", and "EWMA Control Charts".

Once you click OK in a launch window, the Control Chart Builder window appears with the Control Panel hidden by default. All other options and features are the same.

## **Control Chart Builder Interactive Workspace**

Figure 3.4 Interactive Control Chart Builder Window



For more information about the options in the Select Columns red triangle menu, see *Using IMP*.

To begin creating a control chart, drag variables from the **Select Columns** box into the zones. If you drop variables in the center, JMP guesses where to put them based on whether the variables are continuous or categorical. The Control Chart Builder workspace contains the following zones:

**Y** Assigns the process variable.

**Subgroup** Assigns subgroup variables. To define subgroup levels as a combination of multiple columns, add multiple variables to the **Subgroup** zone. When a subgroup variable is assigned, each point on the control chart corresponds to a summary statistic for all of the points in the subgroup.

**Phase** Assigns phase variables. When a Phase variable is assigned, separate control limits are computed for each phase. See also "XBar and R Chart Phase Example".

The initial Control Chart Builder window contains the following buttons:

**Undo** Reverses the last change made to the window.

- **Start Over** Returns the window to the default condition, removing all data, and clearing all zones.
- **Done** Hides the buttons and the Select Columns box and removes all drop zone outlines. In this presentation-friendly format, you can copy the graph to other programs. To restore the window to the interactive mode, click the Control Chart Builder red triangle and select **Show Control Panel**.
- **By** Identifies the variable and produces a separate analysis for each value that appears in the column.
- **Shewhart Variables/Shewhart Attribute/Rare Event** Enables you to select Shewhart Variables, Shewhart Attribute, or Rare Event control chart types. If you select an Attribute chart type, an n Trials box and zone appear on the chart.
- **n Trials** (Available for Attribute charts.) Assigns a lot size for an attribute control chart.
- **New Y Chart** Produces a copy of the current chart for every column selected in the Select Columns box. The new charts use the selected columns in the Y role.

Once you drag variables to the chart, other buttons and options appear at left that enable you to show, hide or switch items on the chart (Figure 3.7). Many of these functions (Points, Limits, Warnings, etc.) are the same as the functions available when you right-click the chart. See "Options Panel and Right-Click Chart Options". For information about warnings and rules, see "Tests" and "Westgard Rules".

- **Three Way Control Chart** Enables you to produce a three way control chart for variable chart types. The subgroup size must be greater than one. The plotting statistic is based on subgroup averages, within-subgroup variation, or between-subgroup variation. The default set of three includes a presummarized chart of the averages using Moving Range limits, a Moving Range chart and a Range chart.
- **Event Chooser** Allows the chart to respond in real time to selection changes. There are several standard groups of responses that are recognized and pre-scored (for example, pass/fail, yes/no, Likert Scales, conforming/non-conforming, and defective/non-defective). If you are analyzing results from a survey and want to focus solely on a specific sector of the results for one or more questions, you can make the selection on the screen. When you make the selection, the chart is scored again and replotted immediately. The levels selected in the Event Chooser are counted as events, and all other levels are counted as non-events.

The Event Chooser is available for attribute charts with response columns that have a modeling type of nominal or ordinal. If you want the Event Chooser to work on a numeric integer-valued nominal or ordinal response column, you must select the Use Event Chooser option from the Control Chart Builder red triangle menu. The Event Chooser does not appear for response columns with a modeling type of continuous.

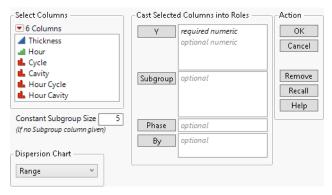
## **Launch Windows for Specific Control Charts**

The options that you see in the launch windows vary depending on whether you are launching variable control charts or attribute control charts.

#### **Launch Windows for Variable Control Charts**

This section contains information about the launch windows for I/MR, XBar, Run, Levey Jennings, I/MR on Means, and Three Way Control Charts.

Figure 3.5 Launch Window for Variable Control Charts



For more information about the options in the Select Columns red triangle menu, see *Using JMP*.

- **Y** Assigns the process variables.
- **Subgroup** (Available only for XBar, Levey Jennings, I/MR on Means, and Three Way Control Charts.) Assigns the subgroup variables. When a subgroup variable is assigned, each point on the control chart corresponds to a summary statistic for all of the points in the subgroup.
- **Sample Label** (Available only for I/MR Charts.) Assigns a sample label variable to uniquely label individual measurements.
- **Phase** (Not available for Run Charts.) Assigns the phase variable. When a Phase variable is assigned, separate control limits are computed for each phase.
- **By** Identifies a variable to produce a separate analysis for each value that appears in the column.
- **Sort by Sample Label** Sorts all variables by the sample label.

**Constant Subgroup Size** (Available only for XBar charts.) Specifies a number of observations that make up each subgroup. If the number of observations per subgroup is not constant, you should specify a column in the Subgroup role.

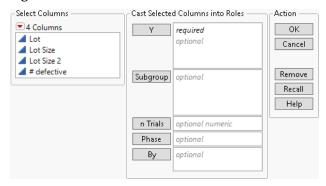
**Note:** If you specify a Subgroup variable, the platform ignores the setting for the Constant Subgroup Size option.

**Dispersion Chart** (Available only for XBar charts.) Specifies the type of dispersion chart that appears below the XBar chart. You can choose between no dispersion chart, a range chart (XBar & R), or a standard deviation chart (XBar & S).

#### **Launch Windows for Attribute Control Charts**

This section contains information about the launch windows for NP, P, C, and U Control Charts.

Figure 3.6 Launch Window for Attribute Control Charts



For more information about the options in the Select Columns red triangle menu, see *Using IMP*.

**Y** Assigns the process variables.

**Subgroup** Assigns the subgroup variables. When a subgroup variable is assigned, each point on the control chart corresponds to a summary statistic for all of the points in the subgroup.

**n Trials** Assigns the subgroup sample size.

**Phase** Assigns the phase variable. When a Phase variable is assigned, separate control limits are computed for each phase.

**By** Identifies a variable to produce a separate analysis for each value that appears in the column.

## **Control Chart Builder Window**

Use Control Chart Builder to construct control charts for process data. The analysis produces a chart that can be used to evaluate whether a process is in a state of statistical control. The report varies depending on which type of chart you select. Control charts update dynamically as data is added or changed in the data table. Figure 3.7 displays the Control Chart Builder window for the Bottle Tops.jmp sample data table.

#### *To create the chart:*

- 1. Select **Help > Sample Data Library** and open Quality Control/Bottle Tops.jmp.
- 2. Select Analyze > Quality and Process > Control Chart Builder.
- 3. Drag Status to the **Y** zone.
- 4. Drag Sample to the **Subgroup** zone (at bottom).

NP chart of Status Undo Start Over Done By ▼ 4 Columns △ Status Limit Summaries Phase ▲ Sample ■ Status 20 LCL Avg UCL Sigma plotted ▲ Phase
 Notes Count 0.435598 8.346154 16.25671 Binomial Shewhart Attribute V New Y Chart 15 Status 4 Points Statistic nt(Status) Show Connect Line 🗸 10 Show Points **⊿** Limits Sigma Binomial (P,NP) center line UCL and LCL Zones Shade Zones Show Upper Limit Show Lower Limit Show Center Line 🗸 Warnings 50 Where(100 rows excluded)

Figure 3.7 Control Chart Builder Window

You can drag other variables into the various zones to augment the analysis and use the "Control Chart Builder Options" to further examine the data. Some of the right-click chart options (for example, show or hide points, limits, warnings, and zones; select statistic and sigma options) also appear on the left hand side of the chart for easy access.

Control charts have the following characteristics:

 Each point plotted on the chart represents an individual process measurement or summary statistic. Subgroups should be chosen *rationally*, that is, they should be chosen to maximize the probability of seeing a true process signal *between* subgroups. Often, this requires knowledge of the process to determine the most effective grouping strategy. See Wheeler (2004); Woodall and Adams (1998).

- The vertical axis of a control chart is scaled in the same units as the summary statistic.
- The horizontal axis of a control chart identifies the subgroup samples and is time ordered. Observing the process over time is important in assessing if the process is changing.

The green line is the center line, or the average of the data. The center line indicates the average (expected) value of the summary statistic when the process is in statistical control. Measurements should appear equally on both sides of the center line. If not, this is possible evidence that the process average is changing.

The two red lines are the upper and lower control limits, labeled UCL and LCL. These
limits give the range of variation to be expected in the summary statistic when the process
is in statistical control. If the process is exhibiting only routine variation, then all the points
should fall randomly in that range.

**Note:** To hide the lower control limits on dispersion, attribute, and rare event charts, deselect the Show Lower Limit option in the options panel. To change the default to always hide the lower control limits, deselect the Show Lower Control Limit preference in File > Preferences > Platforms > Control Chart Builder.

• A point outside the control limits signals the presence of a special cause of variation.

Options in the Control Chart Builder window create control charts that can be updated dynamically as samples are received and recorded or added to the data table. When a control chart signals abnormal variation, action should be taken to return the process to a state of statistical control if the process degraded. If the abnormal variation indicates an improvement in the process, the causes of the variation should be studied and implemented.

When you double-click the axes, the appropriate Axis Specification window appears for you to specify the format, axis values, number of ticks, gridline, reference lines, and other options to display.

# **Control Chart Builder Options**

Control Chart Builder options appear in the red triangle menu or by right-clicking on a chart or axis. Some of the right-click chart options also appear on the bottom left hand side of the chart for easy access. You can also set preferences for many of the options in Control Chart Builder at File > Preferences > Platforms > Control Chart Builder.

- "Control Chart Builder Red Triangle Menu Options"
- "Options Panel and Right-Click Chart Options"
- "Control Chart Builder Right-Click Axis Options"

## **Control Chart Builder Red Triangle Menu Options**

The Control Chart Builder red triangle menu contains the following options:

**Show Control Panel** Shows or hides the following elements:

- buttons
- the Select Columns box
- the drop zone borders
- check boxes and drop-down menus

**Show Limit Summaries** Shows or hides the Limit Summaries report. This report shows the control limits (LCL and UCL), the center line (Avg), the Points and Limits plotted, and the Sample Size for the chart. Sample size is not shown for rare event charts.

Show Capability (Available only for Shewhart Variables charts that have specification limits.) Shows or hides the Process Capability Analysis report. Since the report is part of the Limit Summaries report, the Process Capability report appears only when the Show Limit Summaries option is selected. For more information, see "The Process Capability Report". You can set preferences for many of the options in the Process Capability report in Control Chart Builder at File > Preferences > Platforms > Process Capability.

**Note:** Show Capability is not available if the response variable has no variation.

**Show Alarm Report** Shows or hides a report that contains information about out of control samples. The report reflects failures for currently enabled tests in each chart and updates automatically as different tests are enabled and disabled and as data and row states change. A second table lists the currently enabled tests for each chart. The first table contains the following columns:

**Position** Indicates the numerical position of the chart, starting from the top of the report.

**Total Samples Out of Control** Counts the number of samples that failed at least one of the selected tests.

**Alarm Rate** The total number of samples out of control divided by the total number of nonmissing samples. This is also known as the Proportion Out of Control.

**Note:** The counts that contribute to the calculation of the alarm rate include excluded samples only if the Test Excluded Subgroups and the Show Excluded Region options are both selected.

**Show Limit Labels** Shows or hides labels for the limits in each chart. The limits are shown inside the right frame of the chart.

**Show Sigma Report** (Available only for Shewhart Variables charts.) Shows or hides the Process Sigma Report, which is a table of sigma values. The Process Sigma Report contains the overall sample size, number of subgroups, sample mean, overall sigma, within sigma, and stability index. For three way control charts, the between-sigma and between-and-within sigma values are also shown. If a phase variable is specified, a set of values is given for each phase.

Note: The Process Sigma Report appears only if the Limit Summaries report is turned on.

**Get Limits** Retrieves the control limits that are stored in an open or saved data table.

**Show Excluded Region** Shows (on) or removes (off) the regions of the chart where samples have been excluded. When entirely excluded subgroups are shown on the location chart, they appear as dimmed points to indicate that they are excluded.

**Caution:** The Show Excluded Region option impacts the chart. Excluded samples are removed from the calculation of control limits, whether this option is on or off. Excluded samples are included in alarm rate calculations only if the Test Excluded Subgroups and the Show Excluded Region options are both selected.

**Set Subgroup Size** (Not available if a subgroup variable is specified.) Sets a subgroup size. Missing values are taken into account when computing limits and sigma.

**Note:** If the Set Subgroup Size option is used, the Show Excluded Region option is turned on automatically.

**Save Limits** Saves the control limits in one of the following ways:

- **in Column** Saves control limits as a column property in the existing data table for the response variable. If the limits are constant, LCL, Avg, and UCL values for each chart type in the report are saved. This option is not available with phase charts. In addition, the option has no effect if the sample sizes are not constant for each chart.
- **in New Table** Saves the standard deviation and mean for each chart into a new data table. If the limits are constant, the LCL, Avg, UCL, and Sample Size for each chart are saved as well. If there are phases, a new set of values is saved for each phase. There is a row for each statistic and a column for each Y variable.
- **in New Tall Table** (Not available for Rare Event, Attribute, or Phase charts.) Saves the standard deviation, mean, and Sigma for each chart into a new data table. If the limits are constant, the LCL, Avg, UCL, and Sample Size for each chart are saved as well. There is a row for each Y variable and a column for each statistic. A column for Sigma that can be used in the Process Screening platform is also saved.

**Save Summaries** Creates a new data table containing such information as the sample label, sample sizes, statistic being plotted, center line, control limits, and any tests, warnings and failures. The specific statistics included in the table depend on the type of chart.

**Graph Spacing** Sets the amount of space between the graphs.

**Include Missing Categories** Enables the graph to collect rows with missing values in a categorical column, and displays the missing values on the graph as a separate category. If this option is disabled, all rows with a missing X value are removed from the calculations, in addition to being hidden from the graph.

This option is not available for continuous X variables or categorical Y variables because there is no compelling way to display the collected missing values on the relevant axes. By default, this option is enabled.

**Note:** If Include Missing Categories is enabled, capability analysis results in Control Chart Builder do not match those in the Process Capability platform if a categorical X variable has missing values.

**Use Event Chooser** (Available only for attribute charts with numeric non-continuous Y variables.) Categorizes ordinal numeric data and offers individual numeric-level modeling selections.

**Alarm Script** Enables you to write and run a script that indicates when the data fail special causes tests. See "Tests". Results can be written to a file, written to the log or sent in an email. There is an option to include an explanation of why the test failed.

As an Alarm Script is invoked, the following variables are available, both in the issued script and in subsequent JSL scripts:

qc\_col is the name of the column

qc\_test is the test that failed

qc\_sample is the sample number

qc\_phase is the label of the phase during which the failure occurred

See the Scripting Guide for more information about writing custom Alarm Scripts.

**Note:** Alarm scripts are not available in reports that use the Local Data Filter.

**Sort by Row Order** Sorts all subgroup and phase variables in the order in which the levels appear in the data table. This applies to all combinations of nested subgroup and phase variables.

**Test Excluded Subgroups** (Available only if the Show Excluded Region option is selected.) Includes (on) or excludes (off) entirely excluded subgroups in the computation of tests.

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When excluded subgroups are shown and the Text Excluded Subgroups option is not selected, the excluded subgroups are treated as missing values.

**Note:** For any test that relies on consecutive points (runs tests), an entirely excluded subgroup is treated as missing and counts of consecutive points are restarted.

**Control Chart Dialog** (Available only if the control chart is launched through a Control Chart launch window.) Opens the Control Chart launch window with the original settings that were used to create the control chart.

See *Using JMP* for more information about the following options:

**Local Data Filter** Shows or hides the local data filter that enables you to filter the data used in a specific report.

**Redo** Contains options that enable you to repeat or relaunch the analysis. In platforms that support the feature, the Automatic Recalc option immediately reflects the changes that you make to the data table in the corresponding report window.

**Save Script** Contains options that enable you to save a script that reproduces the report to several destinations.

- Column Switcher is available only for a single Y variable having two or fewer associated charts. Based on the selected chart type, only columns that are appropriate for the Y role are included in the Column Switcher column list.
- In Control Chart Builder, the Automatic Recalc option is turned on by default and cannot be turned off.
- When using the local data filter, you can deselect the Show Excluded Region option for more focused exploration.

## **Options Panel and Right-Click Chart Options**

The following options appear on the left hand side of the Control Chart Builder report or when you right-click a chart. Some options appear in both locations.

**Event Chooser** (Available only for attribute charts with response columns that have a modeling type of nominal or ordinal.) Allows the chart to respond in real time to selection changes. See "Event Chooser".

**Points** Provides the following options:

**Statistic** Changes the statistic plotted on the chart. See "Statistic".

**Individual Points** Show or hides individual observations in a subgroup. Available only with a subgroup variable or Set Sample Size. This option is not available for Attribute chart types or Rare Event charts.

**Box Plots** (Available only for Shewhart Variables charts.) Shows or hides box plots on the chart.

**Show Connect Line** Shows connecting lines between the points.

**Show Points** Shows or hides the points on the chart.

**Limits** Provides the following options:

**Sigma** Specifies the method of computing sigma. See "Sigma".

**Zones** (Available only for Variables and Attribute chart types.) Shows or hides the zones on the chart. There are three equal-width zones on either side of the mean. Zones are not drawn below the LCL or above the UCL. If the limits for a Variables chart are not centered around the mean, min(Avg-LCL,UCL-Avg)/3 is used as the width of each zone. The zones for an Attributes chart use a width of (UCL-Avg)/3.

**Shade Zones** Shows or hides shading zones by ranges. Zone C is shaded green, zones A and B are shaded yellow, and beyond zone A is shaded red.

**Spec Limits** (Available only if the data table has a Spec Limits column property or if you specify Spec Limits using the Add Spec Limits option.) Shows or hides the specification limits on the chart. By default, the spec limits are shown if the Spec Limits column property has the Show as Graph Reference Lines option selected. See *Using JMP* for information about adding a Spec Limits column property.

**Add Spec Limits** (Available in the right-click menu.) Enables you to enter specification limits.

**Set Control Limits** (Available in the right-click menu.) Enables you to enter control limits for tests. After you click OK in the Set Control Limits window, the specified control limits are set uniformly across groups. Select this option again to remove the specified control limits.

**Add Limits** (Available in the right-click menu.) Specifies additional control limits to be plotted on the chart. These limits are not used in tests.

**Show Upper Limit** Shows or hides the upper control limit on the chart. If you hide the upper control limit on a chart, the Test Beyond Limits and Test 1 options do not flag points associated with the hidden upper control limit.

**Show Lower Limit** Shows or hides the lower control limit on the chart. If you hide the lower control limit on a chart, the Test Beyond Limits and Test 1 options do not flag points associated with the hidden lower control limit.

**Show Center Line** Shows or hides the center line on the chart.

**Add Dispersion Chart** (Available in the right-click menu.) Adds a dispersion chart to the chart area. Change the chart type with the Points options. A dispersion chart illustrates the variation in the data by plotting one of many forms of dispersion, including the range, standard deviation, or moving range. Available only for Variables chart types.

**Note:** You can customize the default dispersion chart type using the Dispersion Chart and Summarized Dispersion Chart preferences in File > Preferences > Platforms > Control Chart Builder.

**Set Subgroup Size** Sets a subgroup size. Missing values are taken into account when computing limits and sigma.

**Warnings** Provides the following options:

**Customize Tests** (Available in the right-click menu.) Enables you to design custom tests and select or deselect multiple tests at once. After the option is selected, the Customize Tests window appears for designing the tests. Select a test description, and enter the desired number (n) and label. You can save the settings to preferences and also restore the default settings. Available only for Variables and Attribute chart types.

**Tests** Enables you to select which statistical control tests to enable. For more information about tests, see "Tests". Available only for Variables and Attribute chart types.

Note: Hover over a flagged point on the chart to see a description of the test that failed.

**Westgard Rules** Specifies the set of Westgard statistical control tests that are enabled. Because Westgard rules are based on sigma and not the zones, they can be computed without regard to constant sample size. For more information about tests, see "Westgard Rules". Available only for Variables and Attribute chart types.

**Test Beyond Limits** (Called Test 15 in JMP) Enables the test for any points beyond the control limits. These points are identified on the chart. This test works on all charts with limits, regardless of the sample size being equal.

**Note:** If you hide the upper or lower control limits, the Test Beyond Limits option does not flag points that are beyond limits that are not shown on the control chart.

**Remove Graph** (Available in the right-click menu.) Removes the control chart.

**Remove Location Chart** (Available only if you right-click a location chart.) Removes the location chart from the report.

**Remove Dispersion Chart** (Available only if you right-click a dispersion chart.) Removes the dispersion chart from the report.

**Note:** For a description of the Rows, Graph, Customize, and Edit menus, see *Using JMP*.

**Three Way Control Chart** Enables you to produce a three way control chart for variable chart types. See "Three Way Control Chart".

#### Statistic

You can change the statistic represented by the points on the chart. The options available depend on the chart type selected.

For Variables chart types, you can change the statistic represented by the points on the chart using the following options:

**Individual** Creates a chart where each point represents an individual value in the data table.

**Average** Creates a chart where each point represents the average of the values in a subgroup.

**Range** Creates a chart where each point represents the range of the values in a subgroup.

**Standard Deviation** Creates a chart where each point represents the standard deviation of the values in a subgroup.

**Moving Range on Means** Computes the difference in the range between two consecutive subgroup means.

**Moving Range on Std Dev** Computes the difference in the range between two consecutive subgroup standard deviations.

**Moving Range** Creates a chart where each point is the difference between two consecutive observations.

**Note:** The Average, Range, Standard Deviation, Moving Range on Means, and Moving Range on Std Dev methods appear only if a subgroup variable with a sample size greater than one is specified or a sample size is set.

For Attribute chart types, you can change the statistic represented by the points on the chart using the following options:

**Proportion** Creates a chart where each point represents the proportion of items in subgroup samples.

**Count** Creates a chart where each point represents the number of items in subgroup samples.

For Rare Event chart types, the statistic represented by the points on the chart uses the Count option.

## Sigma

You can change the method for computing sigma for the chart. The options available depend on the chart type selected.

For Variables chart types, you can use the following options:

**Range** Uses the range of the data in a subgroup to estimate sigma.

**Standard Deviation** Uses the standard deviation of the data in a subgroup to estimate sigma.

**Moving Range** Uses the moving ranges to estimate sigma. The moving range is the difference between two consecutive points.

**Median Moving Range** Uses the median moving range to estimate sigma, rather than the average moving range.

**Levey-Jennings** Uses the standard deviation of all the observations to estimate sigma. If your chart has phases, sigma is calculated for each phase separately.

For Attribute chart types, you can use the following options:

**Binomial** Uses the binomial distribution model to estimate sigma. The model indicates the number of successes in a sequence of experiments, where each experiment yields success with some probability. Selecting Binomial yields either a P or NP chart.

**Poisson** Uses the Poisson distribution model to estimate sigma. The model indicates the number of events and the time at which these events occur in a given time interval. Selecting Poisson yields either a C or U chart.

For Rare Event chart types, you can use the following options:

**Negative Binomial** Uses the negative binomial distribution model to estimate sigma. The model indicates the number of successes in a sequence of trials before a specified number of failures occur. Selecting Negative Binomial yields a G chart.

**Weibull** Uses the Weibull distribution model to estimate sigma. The model indicates the mean time between failures. Selecting Weibull yields a T chart.

#### **Tests**

The Warnings option in the pop-up menu or on the left hand side of the window displays a submenu for Tests selection. You can select one or more tests for special causes (Western Electric rules) from the menu. Nelson (1984) developed the numbering notation used to identify special tests on control charts. The tests work with both equal and unequal sample sizes.

If a selected test is positive for a particular sample, that point is labeled with the test number. When you select several tests for display and more than one test signals at a particular point, the label of the numerically lowest test specified appears beside the point. You can hover over a flagged point on the chart to see a description of the test that failed.

**Tip:** To add or remove several tests at once, select or deselect the tests in the Control Panel under **Warnings > Tests**.

Table 3.8 lists and interprets the eight tests, and Figure 3.9 illustrates the tests. The following rules apply to each test:

- The area between the upper and lower limits is divided into six zones, each with a width of one standard deviation.
- The zones are labeled A, B, C, C, B, A with zones C nearest the center line.
- A point lies in Zone B or beyond if it lies beyond the line separating zones C and B. That is, if it is more than one standard deviation from the center line.
- Any point lying on a line separating two zones lines is considered belonging to the innermost zone. So, if a point lies on the line between Zone A and Zone B, the point is considered to be in Zone B.
- When a Phase variable is specified, the counts for each test are reset at the start of each phase.

#### Notes:

- Tests 1 through 8 apply to all Shewhart Variables chart types.
- Tests 1, 2, 5, and 6 apply to the upper and lower halves of the chart separately.
- Tests 3, 4, 7, and 8 apply to the whole chart.
- Once a runs test (one that is based on consecutive observations) is triggered, the counts do not reset to 0 when moving to the next sample.
- Runs tests handle excluded rows based on the setting of the Show Excluded Region and Test Excluded Subgroups options.
  - By default, both options are selected, and the excluded rows are included in the runs tests calculations.
  - If the Show Excluded Region option is selected and the Test Excluded Subgroups
    option is not selected, the excluded rows are treated as missing and the counts for the
    runs tests reset to 0 when moving to the next sample.
  - If the Show Excluded Region option is not selected, the excluded rows are treated as if they are deleted.
- Tests 5 through 8 are not available for attribute charts.

See Nelson (1984, 1985) for further recommendations on how to use these tests.

Individual & Moving Range chart of Acid

Phase

Points
Points
Individual 7.087263 10.56667 14.04607 Moving Range 11

Moving Range 0 1.308896 4.274896 Moving Range 11

A Center line

The standard Summaries

Points LCL Avg UCL Limits Signa Si

Figure 3.8 Zones for Western Electric Rules

Table 3.8 Description and Interpretation of Tests for Special Causes<sup>a</sup>

12 14 16 18 20

10

Test 1	One point beyond Zone A (upper or lower)	Detects a shift in the mean, an increase in the standard deviation, or a single aberration in the process. For interpreting Test 1, any dispersion chart (R, S, or MR) can be used to rule out increases in variation.
		Note that if you hide the upper or lower control limits, the Test 1 option does not flag points that are associated with limits that are not shown on the control chart.
Test 2	Nine points in a row in a single (upper or lower) side of Zone C or beyond	Detects a shift in the process mean.
Test 3	Six points in a row steadily increasing or decreasing (anywhere on the chart)	Detects a trend or drift in the process mean.
Test 4	Fourteen points in a row alternating up and down (anywhere on the chart)	Detects systematic effects such as two alternately used machines, vendors, or operators.

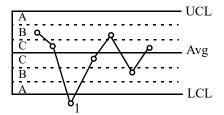
**Table 3.8** Description and Interpretation of Tests for Special Causes<sup>a</sup> (Continued)

Test 5	Two out of three points in a row in or beyond Zone A and the point itself is in or beyond Zone A; the two points must be on the same side (upper or lower)	Detects a shift in the process average or increase in the standard deviation. Any two out of three points provide a positive test.
Test 6	Four out of five points in a row in or beyond Zone B and the point itself is in or beyond Zone B; the four points must be on the same side (upper or lower)	Detects a shift in the process mean. Any four out of five points provide a positive test.
Test 7	Fifteen points in a row in Zone C, above and below the center line	Detects stratification of subgroups when the observations in a single subgroup come from various sources with different means. Also detects a reduction in variation.
Test 8	Eight points in a row on both sides of the center line with none in Zones C	Detects stratification of subgroups when the observations in one subgroup come from a single source, but subgroups come from different sources with different means.

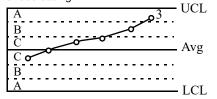
a. Nelson (1984, 1985)

Figure 3.9 Illustration of Special Causes Tests<sup>1</sup>

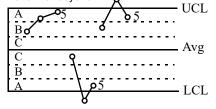
Test 1: One point beyond Zone A



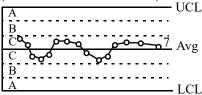
**Test 3:** Six points in a row steadily increasing or decreasing



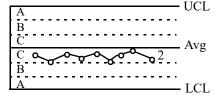
**Test 5:** Two out of three points in a row in Zone A or beyond



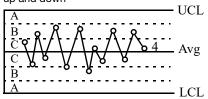
**Test 7:** Fifteen points in a row in Zone C (above and below the center line)



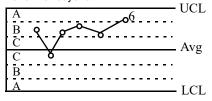
**Test 2:** Nine points in a row in a single (upper or lower) side of Zone C or beyond



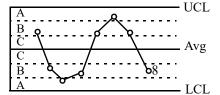
**Test 4:** Fourteen points in a row alternating up and down



**Test 6:** Four out of five points in a row in Zone B or beyond



**Test 8:** Eight points in a row on both sides of the center line with none in Zone C



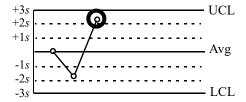
## Westgard Rules

Westgard rules are implemented under the Westgard Rules submenu of the Warnings option when you right-click a chart or on the left hand side of the window. The different tests are abbreviated with the decision rule for the particular test. For example, **1 2s** refers to a test where one point is two standard deviations away from the mean.

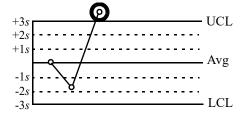
#### Notes:

- Once a runs test (one that is based on consecutive observations) is triggered, the counts do not reset to 0 when moving to the next sample.
- Runs tests handle excluded rows based on the setting of the Show Excluded Region and Test Excluded Subgroups options.
  - By default, both options are selected, and the excluded rows are included in the runs tests calculations.
  - If the Show Excluded Region option is selected and the Test Excluded Subgroups
    option is not selected, the excluded rows are treated as missing and the counts for the
    runs tests reset to 0 when moving to the next sample.
  - If the Show Excluded Region option is not selected, the excluded rows are treated as if they are deleted.

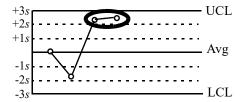
Rule 1 2S (called Test 9 in JMP) is commonly used with Levey-Jennings charts, where control limits are set 2 standard deviations away from the mean. The rule is triggered when any one point goes beyond these limits.



Rule 1 3S (called Test 10 in JMP) refers to a rule common to Levey-Jennings charts where the control limits are set 3 standard deviations away from the mean. The rule is triggered when any one point goes beyond these limits.

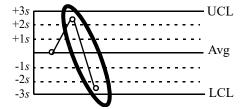


Rule 2 2S (called Test 11 in JMP) is triggered when two consecutive control measurements are farther than two standard deviations from the mean.

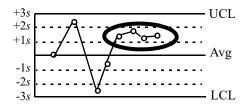


Control Chart Builder Options

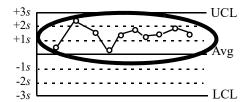
Rule R 4S (called Test 12 in JMP) is triggered when one measurement is greater than two standard deviations from the mean and the previous measurement is greater than two standard deviations from the mean in the opposite direction such that the difference is greater than 4 standard deviations.



Rule 4 1S (called Test 13 in JMP) is triggered when four consecutive measurements are more than one standard deviation from the mean.



Rule 10 X (called Test 14 in JMP) is triggered when ten consecutive points are on one side of the mean.



## **Control Chart Builder Right-Click Axis Options**

**Remove Graph** Removes the entire graph.

**Remove** Removes a variable.

**Note:** If there is more than one chart type on the graph, a submenu listing the different charts is displayed. You can select which chart to remove.

For more information about the Axis Settings, Revert Axis, Add or Remove Axis Label, Save to Column Property, and Edit options, see *Using JMP*.

## **Work with Control Limits**

Control limits are based on the performance of your process and tell you about the variability in your process. Upper control limits (UCLs), center lines, and lower control limits (LCLs) are calculated from the data when a control chart is created. You can use these calculated control limits to indicate when your process has changed.

It is important to note that control limits are different from specification limits, which are often used in capability analysis.

Table 3.9	Control Limits vers	sus Specification Limits
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Control Limits	Specification Limits
Calculated from data	Defined by the customer or design
Based on variability	Based on system requirements
The voice of the process	The voice of the customer

## **Example of Control Limits**

In this example, consider a company's printing process. Variations can cause distortion in the line, including skew, thickness, and length problems. In this example, we will consider the length of the line. A line is considered good if it has a printed length of 16 cm +/- 0.2 cm. Any longer and the sentence might run off of the page. Any shorter and there would be a lot of wasted space on the page. For every print run, the first and last books are taken for measurement. The line lengths are measured on a specified page in the middle of each book.

You want to know: Is this process in control (stable)? Are we getting consistent print quality? What happens when we make improvements to the printing process? Does quality improve? To answer these questions, we need to create control charts and use control limits.

This example is in three parts. In most cases, you would start with "Create the Baseline Control Chart", where you let JMP calculate the control limits for you. Then, to apply these control limits to new data, you would either "Specify Control Limits" or "Specify Multiple Sets of Control Limits" (for phase data).

#### **Create the Baseline Control Chart**

First, examine whether the existing process is in control. If it is, we can use the control limits created by JMP as our baseline or historical limits.

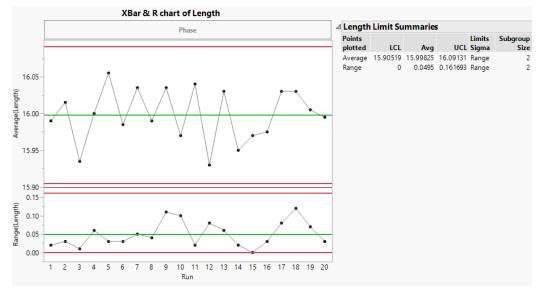
Select Help > Sample Data Library and open Quality Control/Line Length.jmp.

- 2. Select Analyze > Quality and Process > Control Chart Builder.
- 3. Drag Length to the **Y** zone.

An Individual and Moving Range chart of Length appears. This chart is appropriate if you have no natural subgrouping in your data. However, in this example, there is a natural subgrouping, which is each print run.

4. Drag Run to the **Subgroup** zone (at bottom).

Figure 3.10 XBar and R Chart of Line Length by Print Run



Three lines are drawn horizontally across the XBar and R charts. These are the calculated LCL (lower control limit), Avg (average) and UCL (upper control limit).

Ideally, we would like for all of our points to fall within the control limits, and we would like for the points to fall randomly within these limits. Looking at the graph, we see that no points fall outside of the control limits, and there does not appear to be a pattern to the points. To investigate further, perform Western Electric tests to check for patterns and trends that would cause these tests to fail. (The Western Electric tests are also referred to as Nelson tests.)

In the XBar chart, right-click and select Warnings > Tests > All Tests.

Notice that no points were circled or flagged. This means that our process is in control or stable.

If we had determined that our process was not in control, we would investigate out of control points or work to alter our process so that it is in control. For this example, since the process is already in control or stable, we can skip that step. Now, you can use these

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control limits with new data. Proceed to "Specify Control Limits", or "Specify Multiple Sets of Control Limits" (to see an example with phase data).

## **Specify Control Limits**

Since we established that the process is in control, we can use these historical limits with new data to see how the new data compares to the existing process. To use historical limits, we need to specify control limits instead of having JMP calculate them.

There are several ways to specify control limits in JMP:

- "Set Control Limits Option"
- "Add a Column Property"
- "Use the Get Limits Option"
- "Exclude Rows"

#### **Set Control Limits Option**

One simple way to specify control limits is to use the Set Control Limits option in Control Chart Builder.

- Select Help > Sample Data Library and open Quality Control/New Length Data.jmp. This is the table that contains your new data.
- 2. Select Analyze > Quality and Process > Control Chart Builder.
- 3. Drag Length to the **Y** zone.
- 4. Drag Run to the **Subgroup** zone (at bottom).
- 5. Right-click in the Average (XBar) chart and select **Limits > Set Control Limits**.
- 6. Enter these limits:
  - LCL 15.90519
  - Avg 15.99825
  - UCL 16.09131

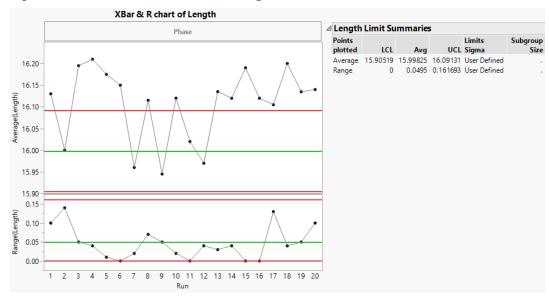
These are the historical limits from the Average (XBar) chart in Figure 3.10.

- 7. Click **OK**.
- 8. Right-click in the Range (R) chart and select **Limits > Set Control Limits**.
- 9. Enter these limits:
  - LCL 0
  - Avg 0.0495
  - UCL 0.161693

These are the historical limits from the Range (R) chart in Figure 3.10.

#### 10. Click **OK**.

Figure 3.11 XBar and R Chart of Line Length with Historical Limits



Rather than calculating limits from the data, JMP used the historical control limits that you defined. In the Length Limit Summaries table, notice that the Limits Sigma now says User Defined. Many points now fall outside of the limits. Also, the averages are higher than those of the baseline process. This process appears different from the original process that we used to calculate the baseline control limits.

## Add a Column Property

Another way to specify control limits is to add the Control Limits column property to a column in your new data table.

- 1. Select **Help > Sample Data Library** and open Quality Control/New Length Data.jmp. This is the table that contains your new data.
- 2. Select the Length column and click **Cols > Column Info**.
- 3. Click Column Properties > Control Limits.
- 4. XBar is selected, so enter these fixed limits for the Average (XBar) chart:
  - Avg 15.99825
  - LCL 15.90519
  - UCL 16.09131

These are the historical limits from the Average (XBar) chart in Figure 3.10.

Leave the value for Subgroup Size as missing. This value is not used in the Control Chart Builder platform.

- 5. Click **XBar > R**. Enter these fixed limits for the Range (R) chart:
  - Avg 0.0495
  - LCL 0
  - UCL 0.161693

These are the historical limits from the Range (R) chart in Figure 3.10.

Leave the value for Subgroup Size as missing. This value is not used in the Control Chart Builder platform.

6. Click **OK**.

You have entered control limits for XBar and R charts for the Length column. Now you can create a control chart.

- 7. Select Analyze > Quality and Process > Control Chart Builder.
- 8. Drag Length to the **Y** zone.
- 9. Drag Run to the **Subgroup** zone (at bottom).

The control chart is identical to Figure 3.11.

## Use the Get Limits Option

The Get Limits method of specifying control limits is the most flexible. You should use this method in the following cases:

- If you have control limits for many different processes
- If you have different control limits for each phase (see "Specify Multiple Sets of Control Limits")

To use the Get Limits method, you need a data table that defines your historical limits. For more information about how to create a limits table, see "Saving and Retrieving Limits".

**Note:** When no subgroup variable is specified, the Get Limits option uses the subgroup size (\_Sample Size) from the limits table. Also, when the limits are missing in the file, JMP also looks for the sigma (\_Std Dev). When no LCL or UCL are specified in the limits file (if both the average and sigma are found, and the subgroup size is constant), the option sets the limits based on the average, subgroup size, and sigma.

In this example, a limits data table has already been created.

- Select Help > Sample Data Library and open Quality Control/New Length Data.jmp.
   This is the table that contains your new data.
- 2. Select Analyze > Quality and Process > Control Chart Builder.

- 3. Drag Length to the Y zone.
- 4. Drag Run to the **Subgroup** zone (at bottom).
- 5. Click the Control Chart Builder red triangle and select **Get Limits**.
- 6. Select **Other** and click **OK**.
- 7. Navigate and open the limits data table for this example, called Length Limits.jmp. By default, the file is located here:
  - On Windows: C:\Program Files\SAS\JMP\16\Samples\Data\Quality Control
  - On macOS: \Library\Application Support\JMP\16\Samples\Data\Quality Control

The control chart is identical to Figure 3.11.

#### **Exclude Rows**

Another way to specify control limits is to exclude rows in a data table. One advantage to this method is that you can see both the historical data and new data in the same graph. This can help to visualize and investigate differences when they occur between the data collection periods.

To use this method, you must meet the following criteria:

- New and old data must reside in the same data table.
- Historical data and new data must all have equal subgroup sizes.
- All new data must be excluded in the data table (using Rows > Exclude/Unexclude).

In this example, new data have already been excluded.

- Select Help > Sample Data Library and open Quality Control/Combined.jmp.
   This table contains old and new data, and the rows corresponding to the new data are excluded.
- 2. Select Analyze > Quality and Process > Control Chart Builder.
- Drag Length to the Y zone.
- 4. Drag Run to the **Subgroup** zone (at bottom).

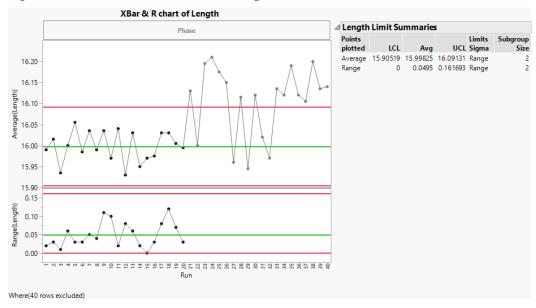


Figure 3.12 XBar and R Chart of Line Length with Excluded Data

JMP uses only the unexcluded rows (historical data) to create the control limits. The new data (excluded data) are plotted on the graph (dimmed), but these data were not used in any of the calculations.

## **Specify Multiple Sets of Control Limits**

In this example, you want to set different control limits for different phases of a process. The column property, set control limits, and excluded row state methods will not work in this situation because these methods are limited to only one set of control limits for the entire chart. For a control chart with phases, you need to use the get limits method.

In the printing company, the goal is to reduce the variability of the force needed to break the bond between paper and the book spine for three different sites. Each site has different machines, different operators, and is also located in different countries; therefore, each site has a unique set of historical limits. For all three sites, the company does the following:

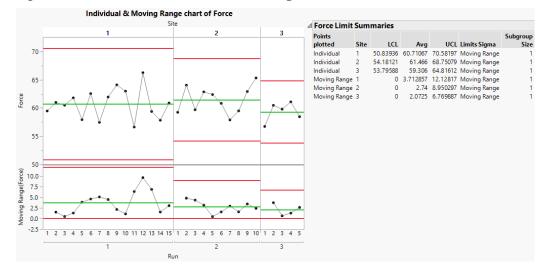
- 1. Creates a baseline control chart based on the existing process data.
- 2. Changes the process, based on a designed experiment.
- 3. Gathers data from the new process.
- 4. Creates a new control chart based on the new process data.

The goal is to plot the new data on a control chart using historical limits from the old process. In this way, the printing company can compare the new process to the old process limits.

## **Create a Control Chart Based on Existing Process**

- Select Help > Sample Data Library and open Quality Control/Phase Historical Data.jmp.
   This table contains the existing process data for all three sites.
- 2. Select Analyze > Quality and Process > Control Chart Builder.
- 3. Drag Force to the **Y** zone.
- 4. Drag Run to the **Subgroup** zone (at bottom).
- 5. Drag Site to the **Phase** zone.

Figure 3.13 Baseline Control Chart for Existing Data



## Create a Control Chart Based on Updated Process

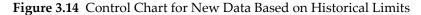
 From the report in Figure 3.13, click the Control Chart Builder red triangle and select Save Limits > in New Table.

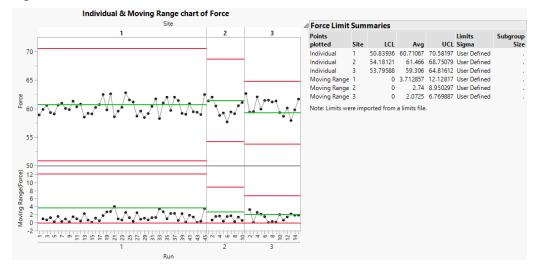
This creates a limits table.

- 2. Save this new limits table to any location, so you can access it later.
- Select Help > Sample Data Library and open Quality Control/Phase New Data.jmp.
   This data was collected from all three sites after the change was made to the process.
- 4. Select Analyze > Quality and Process > Control Chart Builder.
- 5. Drag Force to the **Y** zone.
- 6. Drag Run to the **Subgroup** zone (at bottom).
- 7. Drag Site to the **Phase** zone.

8. Click the Control Chart Builder red triangle and select **Get Limits**. Open the limits table that you saved in step 2.

This applies the historical limits to the new data in the Control Chart Builder report.





Now you can see how the new data (after the process change) compare with the historical process limits (before the process change). None of the points fall outside of the control limits for either the location or dispersion chart. The goal was to reduce variability. Looking at the moving range chart, you can see that most points fall below the average line. For sites 1 and 2, it is clear that the variability of force needed to break the bond between pages and the book spine has been decreased. The decrease at Site 3 is not as strong as at sites 1 and 2. The improvements to the printing process appear to have succeeded in reducing the variability.

# Excluded and Hidden Samples in Control Chart Builder

The following bullets summarize the use of excluded and hidden samples in control chart builder:

Excluded subgroups are not used in the calculations of control limits, and appear on the
chart as dimmed points by default. If the Show Excluded Region option is not selected, the
points for the excluded subgroups do not appear in the chart, are treated as missing in
Tests for Special Causes, and are not included in the count of points for Tests for Special
Causes.

**Control Chart Builder** 

- Hidden observations are used in the calculations of control limits, but do not appear in the chart.
- Rows that are both hidden and excluded are included in the count of points for Tests for Special Causes when the Test Excluded Subgroups option is selected. An excluded row can be labeled with a special cause flag. A hidden point cannot be labeled. If the flag for a Tests for Special Causes test is on a hidden point, it will not appear in the chart.
- For partially excluded subgroups, if one or more observations within a subgroup is
  excluded, and at least one observation within the subgroup is included, the excluded
  observation is not included in the calculations of either the point statistic or the limits.
- Checks for negative and non-integer data happen on the entire data (even excluded values).
- Tests apply to all excluded subgroups only when the Test Excluded Subgroups option is selected.

# **Additional Examples of Control Chart Builder**

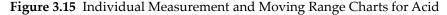
**Note:** In this section, some examples show the Control Panel while others do not. To show or hide the Control Panel, select Show Control Panel from the Control Chart Builder red triangle menu.

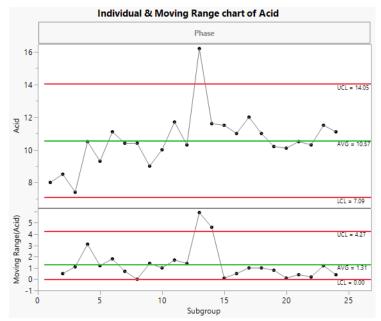
- "Individual Measurement and Moving Range Charts Example"
- "XBar and R Chart Phase Example"
- "XBar and S Charts with Varying Subgroup Sizes Example"
- "Run Chart Example"
- "P chart Example"
- "NP chart Example"
- "C chart Example"
- "U chart Example"
- "G chart Example"
- "T chart Example"
- "Three Way Control Chart Example"
- "Example of Multiple Control Charts"

## **Individual Measurement and Moving Range Charts Example**

The Pickles.jmp data in the Quality Control sample data folder contains the acid content for vats of pickles. Because the pickles are sensitive to acidity and produced in large vats, high acidity ruins an entire pickle vat. The acidity in four vats is measured each day at 1, 2, and 3 PM. The data table records day, time, and acidity measurements.

- 1. Select **Help > Sample Data Library** and open Quality Control/Pickles.jmp.
- 2. Select Analyze > Quality and Process > Control Chart Builder.
- 3. Drag Acid to the Y role.
- Click the Control Chart Builder red triangle and select Show Limit Labels.
   This option labels the control limits and averages in both charts.





The individual measurement and moving range charts monitor the acidity in each vat produced (subgroup of size 1). Vat 13 has an acidity above the upper control limit of 14.05.

You can also view a Median Moving Range chart. Continue with the following steps to change the charts to use median moving ranges.

- 5. In the Limits[1] outline, change the **Sigma** setting to **Median Moving Range**.
- 6. In the Limits[2] outline, change the **Sigma** setting to **Median Moving Range**.

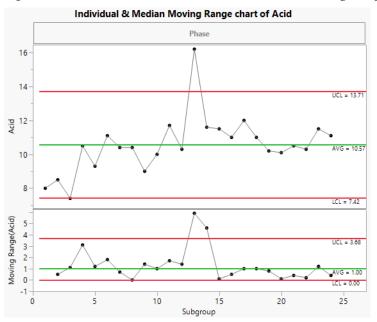


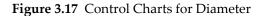
Figure 3.16 Individual Measurement and Median Moving Range Charts for Acid

The limits in the individual measurement and median moving range charts use the median moving range as the sigma, rather than the average moving range. This results in slightly narrower control limits for Acid.

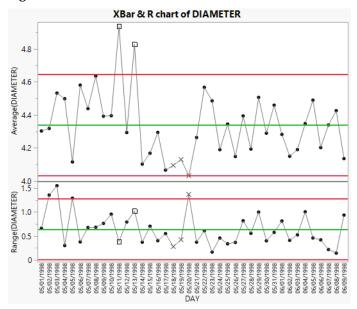
## **XBar and R Chart Phase Example**

A manufacturer of medical tubing collected tube diameter data for a new prototype. The data was collected over the past 40 days of production. After the first 20 days (phase 1), some adjustments were made to the manufacturing equipment. Analyze the data to determine whether the past 20 days (phase 2) of production are in a state of control.

- 1. Select **Help > Sample Data Library** and open Quality Control/Diameter.jmp.
- 2. Select Analyze > Quality and Process > Control Chart Builder.
- 3. Drag DIAMETER to the **Y** role.
- 4. Drag DAY to the **Subgroup** role (at bottom).



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The first 20 days appear to have high variability, and in the Average chart, there are three observations that are outside of the control limits. An adjustment was made to the manufacturing equipment and new control limits were incorporated.

To compute separate control limits for each phase:

- 5. Drag Phase to the **Phase** role.
- 6. In the Average chart, right-click and select **Warnings > Test Beyond Limits**.
- 7. In the Limits[1] outline, select **Shade Zones**.

Additional Examples of Control Chart Builder

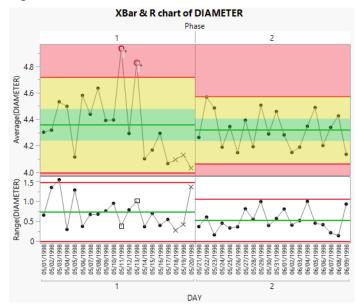


Figure 3.18 Control Charts for each Phase

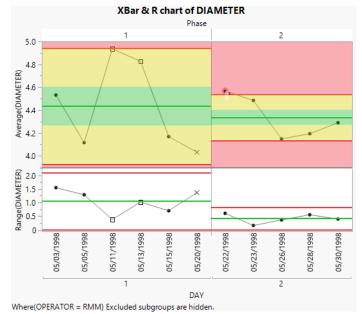
Including the Phase variable means that the control limits for phase 2 are based only on the data for phase 2. None of the phase 2 observations are outside the control limits. This is highlighted by including the zone shading on the chart. Therefore, you can conclude that the process is in control after the adjustments were made.

#### Filter the Control Chart by Another Variable

This data table, Diameter.jmp, contains a column for the operator of the machine for each sample. You can use the Local Data Filter with Control Chart Builder to show the data for a subset of operators.

- 8. Click the **Control Chart Builder** red triangle and deselect **Show Excluded Region**. Turning off the Show Excluded Region option indicates that the subgroups that are excluded by settings in the Local Data Filter no longer appear on the horizontal axis of the control chart as you make selections in the Local Data Filter. As a result, you see only the portion of the data that are of interest.
- 9. Click the **Control Chart Builder** red triangle and select **Local Data Filter**.
- 10. In the Local Data Filter, click on OPERATOR and click the + button.
- 11. In the Local Data Filter, select the bar labeled RMM.

Figure 3.19 XBar and R Chart of Diameter for Operator RMM



The XBar and R charts now show only the points for the RMM operator, as denoted by the Where() statement below the charts. The limits for both phases have been adjusted to reflect that the observations for the other three operators have been excluded.

# **XBar and S Charts with Varying Subgroup Sizes Example**

This example uses the Coating.jmp data table. This quality characteristic of interest is the Weight 2 column.

- 1. Select **Help > Sample Data Library** and open Quality Control/Coating.jmp.
- 2. Select Analyze > Quality and Process > Control Chart Builder.
- 3. Drag Weight 2 to the Y role.
- 4. Drag Sample to the **Subgroup** role (at bottom).

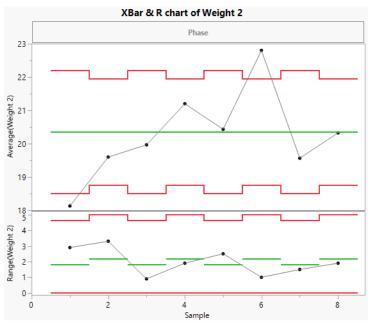


Figure 3.20 XBar and S Charts for Varying Subgroup Sizes

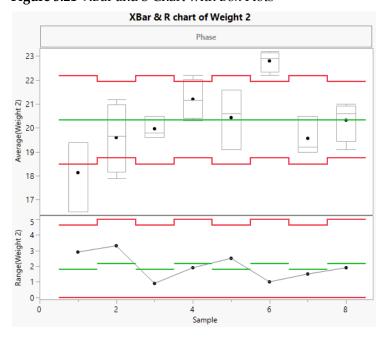
Weight 2 has several missing values in the data, so the chart has uneven limits. Although each sample has the same number of observations, samples 1, 3, 5, and 7 each have a missing value.

Instead of viewing a line connecting the averages of each sample, you can switch to viewing box plots at each sample.

- 5. In the **Points[1]** outline, deselect the **Show Connected Line** option.
- 6. In the **Points[1]** outline, select the **Box Plots** option.

Figure 3.21 XBar and S Chart with Box Plots

**Control Chart Builder** 



## **Run Chart Example**

Run charts display a column of data as a connected series of points. This example is a Run chart for the Close variable from Stock Averages.jmp.

- Select **Help > Sample Data Library** and open Stock Averages.jmp.
- Select Analyze > Quality and Process > Control Chart > Run Chart.
- 3. Select Close and click Y.
- 4. Click **OK**.

Additional Examples of Control Chart Builder

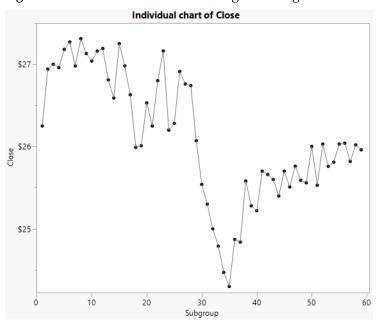


Figure 3.22 Run Chart for Stock Averages Closing Price

## P chart Example

The Washers.jmp sample data contains defect data for two different lot sizes from the *ASTM Manual on Presentation of Data and Control Chart Analysis*, American Society for Testing and Materials (1976). To view the differences between constant and variable sample sizes, you can compare charts for Lot Size and Lot Size 2.

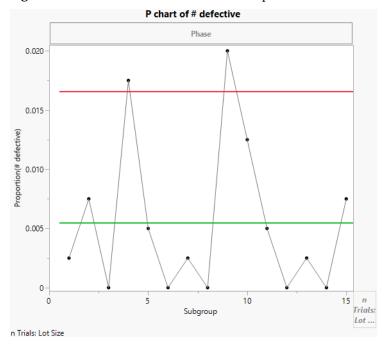
The Washers.jmp data in the Quality Control sample data folder contains defect counts of 15 lots of 400 galvanized washers. The washers were inspected for finish defects such as rough galvanization and exposed steel. If a washer contained a finish defect, it was deemed nonconforming or defective. Thus, the defect count represents how many washers were defective for each lot of size 400. Using the Washers.jmp data table, specify a sample size variable, which would allow for varying sample sizes. This data table contains all constant sample sizes.

- 1. Select **Help > Sample Data Library** and open Quality Control/Washers.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > P Control Chart.
- Select # defective and click Y.
- 4. Select Lot Size and click n Trials.
- 5. Click **OK**.
- 6. In the Limits outline, deselect the **Show Lower Limit** option.

This hides the lower limit, which is not of interest in this situation.

**Figure 3.23** P chart of # defective with sample size

Additional Examples of Control Chart Builder



To view the differences between constant and variable sample sizes, you can compare charts for Lot Size and Lot Size 2 by simply dragging the variables to the nTrials zone.

## **NP chart Example**

The Bottle Tops.jmp sample data contains simulated data from a bottle top manufacturing process. Sample is the sample ID number for each bottle. Status indicates whether the bottle top conformed to the design standards. In the Phase column, the first phase represents the time before the process adjustment. The second phase represents the time after the process adjustment. Notes on changes in the process are also included.

- Select Help > Sample Data Library and open Quality Control/Bottle Tops.jmp.
- **Select Analyze > Quality and Process > Control Chart Builder.**
- 3. Drag Sample to the **Subgroup** role.
- 4. Drag Status to the **Y** role.

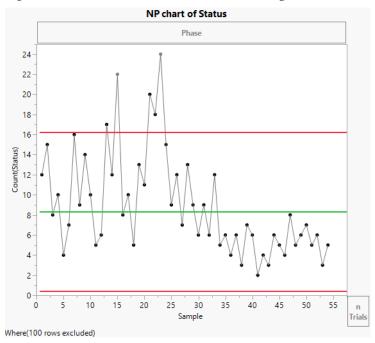


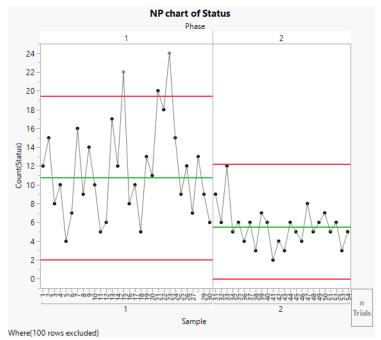
Figure 3.24 NP chart of Status (Nonconforming)

The original observations appear to have high variability and there are five observations (Samples 13, 15, 21, 22 and 23) that are outside of the upper control limit. Samples 15 and 23 note that new material and a new operator were introduced into the process, respectively. At the end of the phase, an adjustment was made to the manufacturing equipment. Therefore, the control limits for the entire series should not be used to assess the control during phase 2.

To compute separate control limits for each phase:

5. Drag Phase to the **Phase** zone.





Including the Phase variable means that the control limits for phase 2 are based only on the data for phase 2. None of the phase 2 observations are outside the control limits. Therefore, you can conclude that the process is in control after the adjustment.

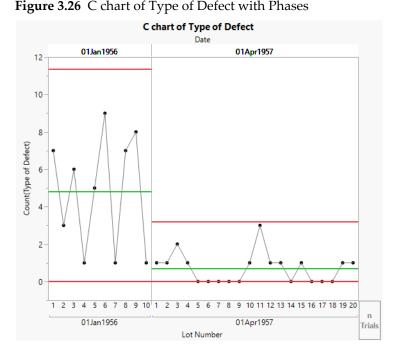
## **C** chart Example

The Cabinet Defects.jmp sample data table contains data concerning the various defects discovered while manufacturing cabinets over two time periods.

- 1. Select **Help > Sample Data Library** and open Quality Control/Cabinet Defects.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > C Control Chart.
- 3. Select Type of Defect and click Y.
- 4. Select Lot Number and click **Subgroup**.
- Select Date and click Phase.
- 6. Click **OK**.

**Control Chart Builder** 

Figure 2.26 C short of Trype of Defect with Dhases

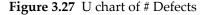


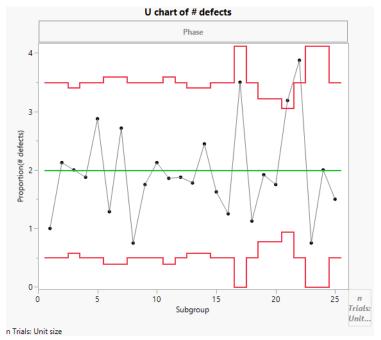
You can now view the results on the two different days. Both appear to be within limits. To examine other defect type behavior, select another defect type under the **Event Chooser > Type of Defect** and view the results as the limits are updated.

## U chart Example

The Braces.jmp data in the Quality Control sample data folder records the defect count in boxes of automobile support braces. A box of braces is one inspection unit. The number of boxes inspected (per day) is the subgroup sample size, which can vary. The U chart in Figure 3.27 is monitoring the number of brace defects per subgroup sample size. The upper and lower bounds vary according to the number of units inspected.

- 1. Select **Help > Sample Data Library** and open Quality Control/Braces.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > U Control Chart.
- 3. Select # defects and click Y.
- 4. Select Unit size and click n Trials.
- 5. Click **OK**.





Because the sample sizes are not equal across subgroups, the limits are uneven. Two of the last five samples are not within the control limits.

## **G** chart Example

A G chart is an effective way to understand whether rare events are occurring more frequently than expected and warrant an intervention. See "Rare Event Control Charts".

The Adverse Reactions.jmp sample data table contains simulated data about adverse drug events (ADEs) reported by a group of hospital patients. An ADE is any type of injury or reaction the patient suffered after taking the drug. The date of the reaction and the number of days since the last reaction were recorded.

- 1. Select **Help > Sample Data Library** and open Quality Control/Adverse Reactions.jmp.
- 2. Select Analyze > Quality and Process > Control Chart Builder.
- 3. Drag Doses since Last ADE to the **Y** role.
- Drag Date of ADE to the **Subgroup** role.
   An Individual & Moving Range chart of Doses since Last ADE appears.
- 5. In the drop-down list, select **Rare Event** instead of **Shewhart Variables**.

A G chart of Doses since Last ADE appears, showing that the number of doses given since the last event.

G chart of Doses since Last ADE

30000 - 30000 - 20000 - 10000

Figure 3.28 G chart of Doses since Last ADE

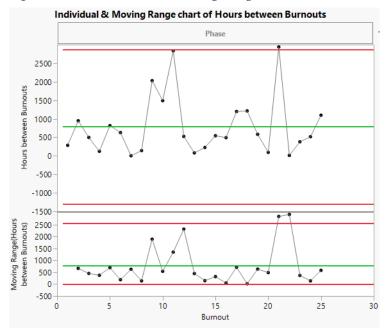
## T chart Example

T charts are used to measure the time that has elapsed since the last event. See "Rare Event Control Charts".

The Fan Burnout.jmp sample data table contains simulated data for a fan manufacturing process. The first column identifies each fan that burned out. The second column identifies the number of hours between each burnout.

- 1. Select **Help > Sample Data Library** and open Quality Control/Fan Burnout.jmp.
- 2. Select Analyze > Quality and Process > Control Chart Builder.
- 3. Drag Hours between Burnouts to the Y role.
- 4. Drag Burnout to the **Subgroup** role.

Figure 3.29 Individual and Moving Range Chart of Hours Between Burnouts



- 5. In the drop-down list, select **Rare Event** instead of **Shewhart Variables**.
- 6. Under Limits, change the **Sigma** from **Negative Binomial** to **Weibull**.

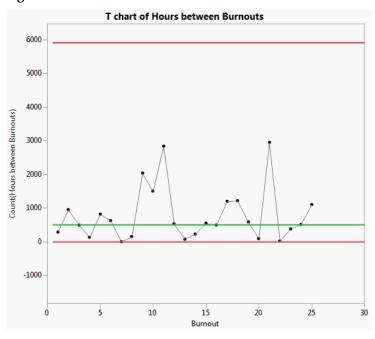


Figure 3.30 T chart of Hours Between Burnouts

In the T chart, all points appear to be within the control limits. It is clear that the Individual & Moving Range chart was inappropriate for the analysis, as the limits were too narrow.

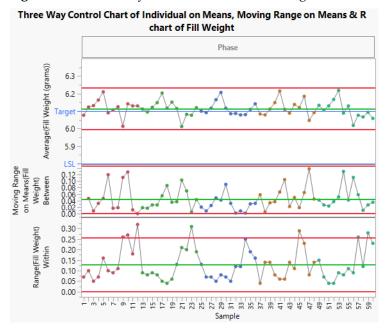
#### **Three Way Control Chart Example**

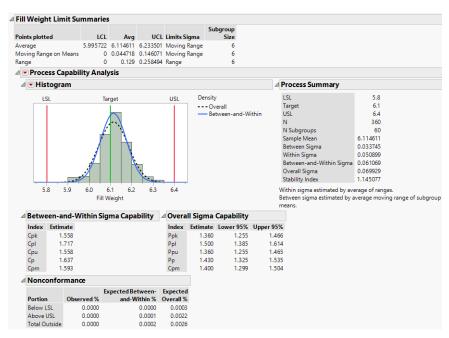
Three way control charts are useful when there is variation between batches and variation within batches.

- 1. Select **Help > Sample Data Library** and open Quality Control/Vial Fill Weights.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > Three Way Control Chart.
- 3. Select Fill Weight and click Y.
- 4. Select Sample and click **Subgroup**.
- 5. Click **OK**.

Figure 3.31 Three Way Control Chart for Fill Weight

Additional Examples of Control Chart Builder





A Moving Range chart appears between the Range and Average charts. The limits on the Average (XBar) chart are now calculated using the moving range between each sample.

**Control Chart Builder** 

## **Example of Multiple Control Charts**

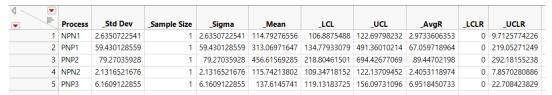
You can create multiple control charts in the same window using the New Y Chart option in the interactive workspace or by specifying multiple processes in a specific control chart launch window. In this example, use the I/MR control chart launch window and then save the control limits to a new data table.

- 1. Select **Help > Sample Data Library** and open Semiconductor Capability.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > IMR Control Chart.
- 3. Click the triangle next to Processes to show all of the processes.
- 4. Select the first five processes and click Y.
- Click **OK**.

If you scroll through the report window, there are Individual and Moving Range control charts for all five selected processes. Since the processes have a Spec Limits column property, there are also Process Capability Analysis reports for each process.

Click the Control Chart Builder red triangle and select Save Limits > in New Tall Table.

Figure 3.32 New Tall Table



The control limits are saved to a new data table, with a row for each Y variable and a column for each statistic.

# **Statistical Details for Control Chart Builder**

#### Notes:

- Control limits are calculated using a sigma multiplier, *K*, which is set to 3 by default. To change the default value of *K*, use the KSigma preference in File > Preferences > Platforms > Control Chart Builder.
- For sample sizes up to n = 50, JMP uses control chart constants  $d_2(n)$  and  $d_3(n)$  that are defined in Table 2 of Harter (1960). For samples with a sample size greater than 50, JMP

Statistical Details for Control Chart Builder

uses the control chart constant values for sample size 50 in both the sigma and control limit calculations.

- "Control Limits for XBar and R Charts"
- "Control Limits for XBar and S Charts"
- "Control Limits for Individual Measurement and Moving Range Charts"
- "Control Limits for P and NP Charts"
- "Control Limits for U Charts and C Charts"
- "Levey-Jennings Charts"
- "Control Limits for G Charts"
- "Control Limits for T Charts"
- "Sigma Calculations for Three Way Control Charts"

#### Control Limits for XBar and R Charts

JMP generates control limits for XBar and R charts using the following formulas:

LCL for XBar chart = 
$$\bar{X}_{vv} - \frac{\hat{K\sigma}}{\sqrt{n_i}}$$

UCL for XBar chart = 
$$\bar{X}_w + \frac{\hat{K\sigma}}{\sqrt{n_i}}$$

LCL for R chart = 
$$\max \left( d_2(n_i) \hat{\sigma} - K d_3(n_i) \hat{\sigma}, 0 \right)$$

UCL for R chart = 
$$d_2(n_i)\sigma + Kd_3(n_i)\sigma$$

Center line for R chart: By default, the center line for the  $i^{th}$  subgroup indicates an estimate of the expected value of  $R_i$ . This value is computed as  $d_2(n_i)\hat{\sigma}$ , where  $\hat{\sigma}$  is an estimate of  $\sigma$ .

The standard deviation for XBar and R charts is estimated using the following formula:

$$\hat{\sigma} = \frac{\frac{R_1}{d_2(n_1)} + \dots + \frac{R_N}{d_2(n_N)}}{N}$$

where:

 $\overline{X}_w$  = weighted average of subgroup means

K = the sigma multiplier and is set to 3 by default

 $\sigma$  = process standard deviation

 $n_i$  = sample size of  $i^{th}$  subgroup

 $d_2(n)$  is the expected value of the range of n independent normally distributed variables with unit standard deviation

 $d_3(n)$  is the standard deviation of the range of n independent normally distributed variables with unit standard deviation

 $R_i$  is the range of  $i^{th}$  subgroup

*N* is the number of subgroups for which  $n_i \ge 2$ .

#### **Control Limits for XBar and S Charts**

JMP generates control limits for XBar and S charts using the following formulas:

LCL for XBar chart = 
$$\bar{X}_w - \frac{\hat{K\sigma}}{\sqrt{n_i}}$$

UCL for XBar chart = 
$$\bar{X}_w + \frac{\hat{K\sigma}}{\sqrt{n_i}}$$

LCL for S chart = 
$$\max \left( c_4(n_i) \hat{\sigma} - Kc_5(n_i) \hat{\sigma}, 0 \right)$$

UCL for S chart = 
$$c_4(n_i)\hat{\sigma} + Kc_5(n_i)\hat{\sigma}$$

Center line for S chart: By default, the center line for the  $i^{\text{th}}$  subgroup indicates an estimate of the expected value of  $s_i$ . This value is computed as  $c_4(n_i)\hat{\sigma}$ , where  $\hat{\sigma}$  is an estimate of  $\sigma$ .

The estimate for the standard deviation for XBar and S charts is:

$$\hat{\sigma} = \frac{\frac{s_1}{c_4(n_1)} + \dots + \frac{s_N}{c_4(n_N)}}{N}$$

where:

 $\overline{X}_{yy}$  = weighted average of subgroup means

K = the sigma multiplier and is set to 3 by default

 $\sigma$  = process standard deviation

 $n_i$  = sample size of  $i^{th}$  subgroup

 $c_4(n)$  is the expected value of the standard deviation of n independent normally distributed variables with unit standard deviation

 $c_5(n)$  is the standard error of the standard deviation of n independent normally distributed variables with unit standard deviation

*N* is the number of subgroups for which  $n_i \ge 2$ 

 $s_i$  is the sample standard deviation of the  $i^{th}$  subgroup

# Control Limits for Individual Measurement and Moving Range Charts

Control limits for Individual Measurement charts are computed as follows:

LCL for Individual Measurement Chart =  $\bar{X} - \hat{K\sigma}$ 

UCL for Individual Measurement Chart =  $\bar{\chi} + \hat{\kappa \sigma}$ 

Control limits for Individual Measurement charts with sigma estimated by the median moving range are computed as follows:

LCL for Individual Measurement Chart =  $\bar{X} - \hat{K\sigma}_{MMR}$ 

UCL for Individual Measurement Chart =  $\bar{X} + \hat{K\sigma}_{MMR}$ 

**Control Chart Builder** 

Control limits for Moving Range charts are computed as follows:

LCL for Moving Range Chart = 
$$\max\{d_2(n)\hat{\sigma} - Kd_3(n)\hat{\sigma}, 0\}$$

UCL for Moving Range Chart = 
$$d_2(n)\hat{\sigma} + Kd_3(n)\hat{\sigma}$$

Control limits for Median Moving Range charts are computed as follows:

$$LCL_{MMR} = max(0, MMR - Kd_3(n) \hat{\sigma}_{MMR})$$

$$UCL_{MMR} = MMR + Kd_3(n) \hat{\sigma}_{MMR}$$

The standard deviation for Individual Measurement and Moving Range charts is estimated as follows:

$$\hat{\sigma} = \frac{\overline{MR}}{d_2(n)}$$

The standard deviation for Individual Measurement and Moving Range charts when using the median is estimated as follows:

$$\hat{\sigma}_{MMR} = MMR/0.954$$

where:

 $\overline{X}$  = the mean of the individual measurements

K = the sigma multiplier and is set to 3 by default

 $\overline{MR}$  = the mean of the nonmissing moving ranges computed as

$$(MR_2+MR_3+...+MR_N)/(N-1)$$
 where  $MR_i = |x_i - x_{i-1}|$ .

MMR = the median of the nonmissing moving ranges

 $\sigma$  = the process standard deviation

 $d_2(n)$  = expected value of the range of n independent normally distributed variables with unit standard deviation.

 $d_3(n)$  = standard deviation of the range of n independent normally distributed variables with unit standard deviation

**Note:** Moving Range charts in Control Chart Builder use a range span of n = 2.

#### **Control Limits for P and NP Charts**

The lower and upper control limits, LCL, and UCL, respectively, are computed using the following formulas:

P chart LCL = 
$$\max(\bar{p} - K \sqrt{\bar{p}(1-\bar{p})/n_i}, 0)$$

P chart UCL = 
$$\min(\bar{p} + K\sqrt{\bar{p}(1-\bar{p})/n_i}, 1)$$

NP chart LCL = 
$$\max(n_i \bar{p} - K_{\alpha} / n_i \bar{p} (1 - \bar{p}), 0)$$

NP chart UCL = 
$$\min(n_i \bar{p} + K \sqrt{n_i \bar{p}(1-\bar{p})}, n_i)$$

where:

 $\bar{p}$  is the average proportion of nonconforming items taken across subgroups

$$\bar{p} = \frac{n_1 p_1 + \dots + n_N p_N}{n_1 + \dots + n_n} = \frac{X_1 + \dots + X_N}{n_1 + \dots + n_N}$$

 $n_i$  is the number of items in the  $i^{th}$  subgroup

*K* is the sigma multiplier and is set to 3 by default

#### **Control Limits for U Charts and C Charts**

The lower and upper control limits, LCL, and UCL, are computed using the following formulas:

U chart LCL = 
$$\max(\overline{u} - K_{\lambda}/\overline{u/n_{i}}, 0)$$

U chart UCL = 
$$\bar{u} + K \sqrt{\bar{u}/n_i}$$

C chart LCL = 
$$\max(n_i \overline{u} - K \sqrt{n_i \overline{u}}, 0)$$

C chart UCL = 
$$n_i \overline{u} + K \sqrt{n_i \overline{u}}$$

The limits vary with  $n_i$ .

 $u_i$  is the number of nonconformities per unit in the  $i^{th}$  subgroup. In general,  $u_i = c_i/n_i$ .

*K* is the sigma multiplier and is set to 3 by default

 $c_i$  is the total number of nonconformities in the  $i^{th}$  subgroup

 $n_i$  is the number of inspection units in the  $i^{th}$  subgroup

 $\bar{u}$  is the average number of nonconformities per unit taken across subgroups. The

quantity  $\bar{u}$  is computed as a weighted average

$$\overline{u} = \frac{n_1 u_1 + \dots + n_N u_N}{n_1 + \dots + n_N} = \frac{c_1 + \dots + c_N}{n_1 + \dots + n_N}$$

*N* is the number of subgroups

## **Levey-Jennings Charts**

Levey-Jennings charts show a process mean with control limits based on a long-term sigma. The control limits are placed at K\*s distance from the center line, where K = 3 by default.

The standard deviation, *s*, for the Levey-Jennings chart is calculated the same way standard deviation is in the Distribution platform.

$$s = \sqrt{\sum_{i=1}^{N} \frac{(y_i - \bar{y})^2}{N - 1}}$$

See Levey and Jennings (1950); Westgard (2002).

#### **Control Limits for G Charts**

The negative binomial distribution is an extension of the geometric (Poisson) distribution and allows for over-dispersion relative to the Poisson. The negative binomial distribution can be used to construct both exact and approximate control limits for count data. Approximate control limits can be obtained based on a chi-square approximation to the negative binomial. All data is used as individual observations regardless of subgroup size.

Statistical Details for Control Chart Builder

Let X have a negative binomial distribution with parameters  $(\mu, k)$ . Then:

$$P(X \le r) \sim P\left(\chi_v^2 \le \frac{2r+1}{1+uk}\right)$$

where:

 $\chi^2_v$  is a chi-square variate with  $v = 2\mu/(1+\mu k)$  degrees of freedom.

Based on this approximation, approximate upper and lower control limits can be determined. For a nominal level  $\alpha$  Type 1 error probability in one direction, an approximate upper control limit is a limit UCL such that the following equation is true:

$$P(X > \text{UCL}) = 1 - P\left(\chi_v^2 \le \frac{2\text{UCL} + 1}{1 + \mu k}\right) = \alpha$$

Likewise, an approximate lower control limit, LCL, is a limit such that the following equation is true:

$$P(X < LCL) = 1 - P\left(\chi_v^2 \ge \frac{2LCL + 1}{1 + \mu k}\right) = \alpha$$

Thus, an approximate level lower and upper control limits, LCL and UCL, respectively, are computed using the following formulas:

UCL = 
$$\frac{\chi^2_{v, 1-\alpha}(1+\mu k)-1}{2}$$

$$LCL = \max \left\{ 0, \frac{\chi^2_{v, \alpha}(1 + \mu k) - 1}{2} \right\}$$

where:

 $\chi^2_{v,\,1-\alpha}(\chi^2_{v,\,\alpha})$  is the upper (lower) percentile of the chi-square distribution with  $v=2\mu/(1+\mu k)$  degrees of freedom. Negative lower control limits can be set to zero. For more information about the negative binomial control limits, see Hoffman (2003).

**Control Chart Builder** 

#### **Control Limits for T Charts**

The estimates of the shape and scale parameters are calculated from the data and used to obtain the percentiles of the Weibull distribution.

**Note:** Subgroups with a response value of zero are given a weight of zero when estimating the Weibull distribution parameters.

Define the following quantities:

p1 = normalDist(-K) for Normal (0,1)

p2 = normalDist(0) for Normal (0,1)

p3 = normalDist(K) for Normal (0,1)

Then the limits are calculated using the following formulas:

LCL = Weibull Quantile (p1,  $\beta$ ,  $\alpha$ )

CL = Weibull Quantile (p2,  $\beta$ ,  $\alpha$ )

UCL = Weibull Quantile (p3,  $\beta$ ,  $\alpha$ )

where:

 $\beta$  is the shape parameter and  $\alpha$  is the scale parameter for the Weibull Quantile function K is the sigma multiplier and is set to 3 by default

For more information about the Weibull Quantile function, see **Help > Scripting Index**.

# Sigma Calculations for Three Way Control Charts

#### Within Sigma Based on Average of Ranges

The within sigma estimate for three way control charts that is estimated using the average of ranges can be used for the Individual on Means, Moving Range on Means and R chart.

$$\hat{\sigma}_{\text{within}} = \frac{\frac{R_1}{d_2(n_1)} + \dots + \frac{R_N}{d_2(n_N)}}{N}$$

The formula uses the following notation:

 $R_i$  = range of  $i^{th}$  subgroup

 $n_i$  = sample size of  $i^{th}$  subgroup

 $d_2(n_i)$  = expected value of the range of  $n_i$  independent normally distributed variables with unit standard deviation

Statistical Details for Control Chart Builder

N = number of subgroups for which  $n_i \ge 2$ 

#### Within Sigma Based on Average of Unbiased Standard Deviations

The within sigma estimate for three way control charts that is estimated using the average of unbiased standard deviations can be used for the Individual on Means, Moving Range on Means, and S chart.

$$\hat{\sigma}_{\text{within}} = \frac{\frac{s_1}{c_4(n_1)} + \dots + \frac{s_N}{c_4(n_N)}}{N}$$

The formula uses the following notation:

 $s_i$  = sample standard deviation of the i<sup>th</sup> subgroup

 $n_i$  = sample size of  $i^{th}$  subgroup

 $c_4(n_i)$  = expected value of the standard deviation of  $n_i$  independent normally distributed variables with unit standard deviation

N = number of subgroups for which  $n_i \ge 2$ 

#### Between Sigma

The between sigma estimate for three way control charts is estimated using the moving range of subgroup means.

$$\hat{\sigma}_{\text{between}} = \sqrt{\left(\frac{\overline{MR}}{d_2(2)}\right)^2 - \frac{\hat{\sigma}^2 \text{ within}}{H}}$$

The formula uses the following notation:

 $\overline{MR}$  = the mean of the nonmissing moving ranges computed as

$$(MR_2+MR_3+...+MR_N)/(N-1)$$
 where  $MR_i = |y_i - y_{i-1}|$ .

 $d_2(2)$  = expected value of the range of two independent normally distributed variables with unit standard deviation.

$$H = \frac{N}{\frac{1}{n_1} + \frac{1}{n_2} + \dots + \frac{1}{n_N}}$$
, the harmonic mean of subgroup sample sizes.

**Note:** If between Sigma is estimated as a negative value, it is set to 0.

#### Between-and-Within Sigma

The between-and-within sigma estimate for three way control charts is estimated using a combination of the within sigma and between sigma estimates.

$$\hat{\sigma}_{between-and-within} = \sqrt{\hat{\sigma}_{within}^2 + \hat{\sigma}_{between}^2}$$

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# **Measurement Systems Analysis**

#### **Evaluate a Continuous Measurement Process Using the EMP Method**

The Measurement Systems Analysis (MSA) platform assesses the precision, consistency, and bias of a measurement system. Before you can study the process itself, you need to make sure that you can accurately and precisely measure the process. If most of the variation that you see comes from the measuring process itself, then you are not reliably learning about the process. Use MSA to find out how your measurement system is performing.

This chapter covers the EMP method. The Gauge R&R method is described in "Variability Gauge Charts".

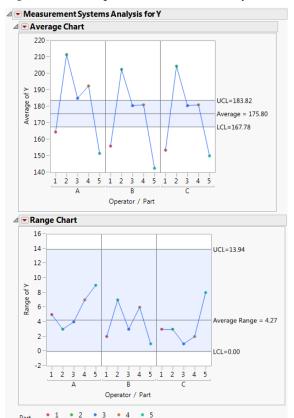


Figure 4.1 Example of a Measurement System Analysis

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# **Overview of Measurement Systems Analysis**

The EMP (Evaluating the Measurement Process) method in the Measurement Systems Analysis platform is largely based on the methods presented in Donald J. Wheeler's book *EMP III Using Imperfect Data* (2006). The EMP method provides visual information and results that are easy to interpret and helps you improve your measurement system to its full potential.

The Gauge R&R method analyzes how much of the variability is due to operator variation (reproducibility) and measurement variation (repeatability). Gauge R&R is available for many combinations of crossed and nested models, regardless of whether the model is balanced. See "Variability Gauge Charts".

Within the Six Sigma DMAIC methodology, MSA (Measurement System Analysis) addresses the Measure phase and process behavior charts (or control charts) address the Control phase. MSA helps you predict and characterize future outcomes. You can use the information gleaned from MSA to help you interpret and configure your process behavior charts.

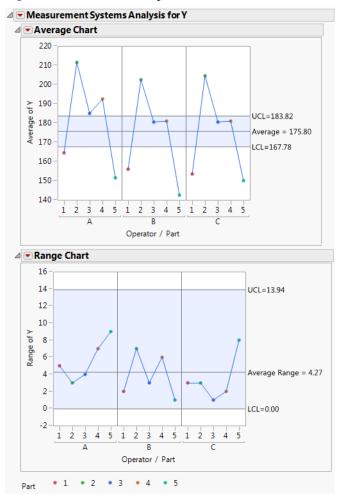
For more information about Control Charts, see "Control Chart Builder".

# **Example of Measurement Systems Analysis**

In this example, three operators measured the same five parts. See how the measurement system is performing, based on how much variation is found in the measurements.

- 1. Select **Help > Sample Data Library** and open Variability Data/Gasket.jmp.
- Select Analyze > Quality and Process > Measurement Systems Analysis.
- 3. Assign Y to the Y, Response role.
- 4. Assign Part to the **Part, Sample ID** role.
- Assign Operator to the X, Grouping role.
   Notice that the MSA Method is set to EMP, the Chart Dispersion Type is set to Range, and the Model Type is set to Crossed.
- 6. Click **OK**.

**Figure 4.2** MSA Initial Report



The Average Chart shows the average measurements for each operator and part combination. In this example, the means of the part measurements are generally beyond the control limits. This is a desirable outcome, because it indicates that you can detect part-to-part variation.

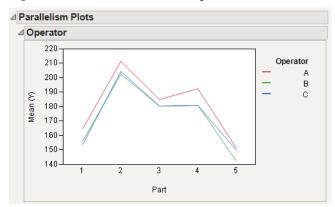
The Range Chart shows the variability for each operator and part combination. In this example, the ranges are within the control limits. This is a desirable outcome, because it indicates that the operators are measuring parts in the same way and with similar variation.

The color coding for each part is shown in the legend below the charts.

7. Click the red triangle next to Measurement Systems Analysis for Y and select **Parallelism Plots**.

Example of Measurement Systems Analysis

Figure 4.3 Parallelism Plot for Operator and Part

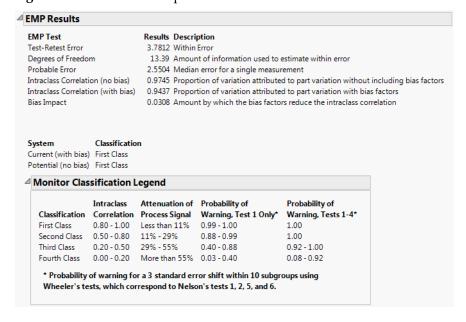


The Parallelism Plots chart shows the average measurements for each part by operator. Because the lines are generally parallel and there is no major crossing, you conclude that there is no interaction between operators and parts.

**Tip:** Interactions indicate a serious issue that requires further investigation.

8. Click the red triangle next to Measurement Systems Analysis for Y and select **EMP Results**.

Figure 4.4 EMP Results Report



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The EMP Results report computes several statistics to help you assess and classify your measurement system. The Intraclass Correlation indicates the proportion of the total variation that you can attribute to the part.

From the EMP Results report, you can conclude the following:

- The Intraclass Correlation values are close to 1, indicating that most of the variation is coming from the part instead of the measurement system.
- The classification is First Class, meaning that the strength of the process signal is weakened by less than 11%.
- There is at least a 99% chance of detecting a warning using Test 1 only.
- There is 100% chance of detecting a warning using Tests 1-4.

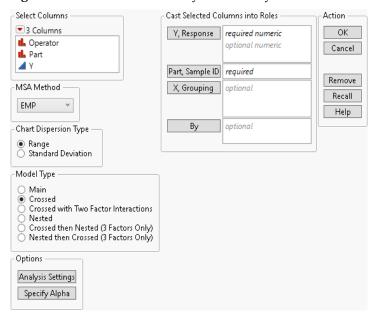
**Note:** For more information about tests and detecting process shifts, see "Shift Detection Profiler".

There is no interaction between operators and parts, and there is very little variation in your measurements (the classification is First Class). Therefore, you conclude that the measurement system is performing quite well.

# **Launch the Measurement Systems Analysis Platform**

Launch the Measurement Systems Analysis platform by selecting **Analyze > Quality and Process > Measurement Systems Analysis**.

Figure 4.5 The Measurement Systems Analysis Window



For more information about the options in the Select Columns red triangle menu, see *Using IMP*.

The Measurement Systems Analysis window contains the following features:

**Select Columns** Lists all of the variables in your current data table. Move a selected column into a role.

**MSA Method** Select the method to use: **EMP** (Evaluating the Measurement Process) or **Gauge R&R**. This chapter covers the **EMP** method. For more information about the **Gauge R&R** method, see "Variability Gauge Charts".

**Chart Dispersion Type** Designates the type of chart for showing variation. Select the **Range** option or the **Standard Deviation** option.

**Note:** For the **EMP** method, the chart dispersion type determines how the statistics in the EMP Results report are calculated. If the **Range** option is selected, and you have a one factor or a two factor, balanced, crossed model, the statistics in this report are based on ranges. Otherwise, the statistics in this report are based on standard deviations.

**Model Type** Designates the model type:

**Main** Variables with nominal or ordinal modeling types are treated as main effects.

**Crossed** The model is crossed when every level of every factor occurs with every level of every other factor.

**Crossed with Two Factor Interactions** The model is crossed when each level of two factors occurs with every level of the other factor.

**Nested** The model is nested when all levels of a factor appear within only a single level of any other factor.

**Cross then Nested (3 Factors Only)** The factors are crossed and then nested for 3 factors.

**Nested then Crossed (3 Factors Only)** The factors are nested and then crossed for 3 factors.

**Options** Contains the following options:

**Analysis Settings** Sets the REML maximum iterations and convergence.

**Specify Alpha** Specifies the 1-alpha confidence level.

**Y, Response** The column of measurements.

**Part, Sample, ID** The column designating the part or unit.

**X, Grouping** The column(s) representing grouping variables.

**By** Identifies a column that creates a report consisting of separate analyses for each level of the variable.

#### **Data Format**

To use the Measurement Systems Analysis platform, all response measurements must be in a single response column. Sometimes, responses are recorded in multiple columns, where each row is a level of a design factor and each column is a level of a different design factor. Data that are in this format must be stacked before running the Measurement Systems Analysis platform. See *Using JMP*.

# **Measurement Systems Analysis Platform Options**

Platform options appear within the red triangle menu next to Measurement Systems Analysis. Selecting an option creates the respective graph or report in the MSA report window. Deselecting an option removes the graph or report. Choose from the following options:

- **Average Chart** A plot of the average measurement values for each combination of the part and *X* variables. The Average Chart helps you detect product variation despite measurement variation. In an Average Chart, out of control data is desirable because it detects part-to-part variation. See "Average Chart".
- **Range Chart** A plot of the variability statistic for each combination of the part and *X* variables. Appears only if you selected **Range** as the Chart Dispersion Type in the launch window. The Range Chart helps you check for consistency within subgroups. In a Range Chart, data within limits is desirable, indicating homogeneity in your error. See "Range Chart or Standard Deviation Chart".
- **Std Dev Chart** A plot of the standard deviation statistic for each combination of the part and *X* variables. Appears only if you selected **Standard Deviation** as the Chart Dispersion Type in the launch window. The Standard Deviation Chart helps you check for consistency within subgroups. In a Standard Deviation Chart, data within limits is desirable, indicating homogeneity in your error. See "Range Chart or Standard Deviation Chart".
- **Parallelism Plots** An overlay plot that reflects the average measurement values for each part. If the lines are relatively not parallel or crossing, there might be an interaction between the part and *X* variables.

**Tip:** Interactions indicate a serious issue that requires further investigation. For example, interactions between parts and operators mean that operators are measuring different parts differently, on average. Therefore, measurement variability is not predictable. This issue requires further investigation to find out why the operators do not have the same pattern or profile over the parts.

- **EMP Results** A report that computes several statistics to help you assess and classify your measurement system. See "EMP Results".
- **Effective Resolution** A report containing results for the resolution of a measurement system. See "Effective Resolution".
- **Bias Comparison** An Analysis of Means chart for testing if the *X* variables have different averages. See "Bias Comparison".
- **Test-Retest Error Comparison** An Analysis of Means for Variances or Analysis of Means Ranges chart for testing if any of the groups have different test-retest error levels. See "Test-Retest Error Comparison".

- **Shift Detection Profiler** An interactive set of charts that you can adjust to see the probabilities of getting warnings on your process behavior chart. See "Shift Detection Profiler".
- **Variance Components** A report containing the estimates of the variance components for the given model. The calculations in this report are based on variances, not ranges. Balanced data uses the EMS method. Unbalanced data uses the REML method.

**Note:** This report is similar to the Variance Components report in the Variability Chart platform, except that it does not compute Bayesian variance component estimates. See "Variance Components".

**EMP Gauge R&R Results** A report that partitions the variability in the measurements into part variation and measurement system variation. The calculations in this report are based on variances, not ranges. Because negative variance components are set to zero, values of zero could indicate outliers in your results.

**Note:** This report is similar to the Gauge R&R report in the Variability Chart platform. However, by default, the calculation for Reproducibility does not include interactions. To specify that interactions be included in the Reproducibility calculation, select the Include Interactions in Reproducibility platform preference. This preference is located in File > Preferences > Platforms > EMP Measurement Systems Analysis. For more information about Gauge R&R studies, see "About the Gauge R&R Method".

See *Using JMP* for more information about the following options:

- **Local Data Filter** Shows or hides the local data filter that enables you to filter the data used in a specific report.
- **Redo** Contains options that enable you to repeat or relaunch the analysis. In platforms that support the feature, the Automatic Recalc option immediately reflects the changes that you make to the data table in the corresponding report window.
- **Save Script** Contains options that enable you to save a script that reproduces the report to several destinations.
- **Save By-Group Script** Contains options that enable you to save a script that reproduces the platform report for all levels of a By variable to several destinations. Available only when a By variable is specified in the launch window.

### **Average Chart**

The red triangle menu next to Average Chart contains the following options:

**Show Grand Mean** Draws the overall mean of the Y variable on the chart.

**Show Connected Means** Draws lines connecting all of the average measurement values.

**Show Control Limits** Draws lines representing the Upper Control Limit (UCL) and the Lower Control Limit (LCL) and labels those values. The control limits for the Average Chart use the same calculations as an XBar control chart. See "Control Limits for XBar and R Charts".

**Show Control Limits Shading** Adds shading between the UCL and LCL.

**Show Separators** Draws vertical lines to delineate between the *X* variables.

**Show Data** Adds the data points to the chart.

**Note:** You can replace variables in the Average Chart in one of two ways: swap existing variables by dragging and dropping a variable from one axis to the other axis; or, click a variable in the Columns panel of the associated data table and drag it onto an axis.

## **Range Chart or Standard Deviation Chart**

The red triangle menu next to Range Chart or Standard Deviation Chart contains the following options:

**Show Average Dispersion** Draws the average range or standard deviation on the chart.

**Show Connected Points** Draws lines connecting all of the ranges or standard deviations.

**Show Control Limits** Draws lines representing the Upper Control Limit (UCL) and the Lower Control Limit (LCL) and labels those values. For more information about the calculations of the limits used in the Range Chart, see "Control Limits for XBar and R Charts". For more information about the calculations of the limits used in the Standard Deviation Chart, see "Control Limits for XBar and S Charts".

**Show Control Limits Shading** Adds shading between the UCL and LCL.

**Show Separators** Draws vertical lines to delineate between the *X* variables.

**Note:** You can replace variables in the Range or Standard Deviation Charts in one of two ways: swap existing variables by dragging and dropping a variable from one axis to the other axis; or, click a variable in the Columns panel of the associated data table and drag it onto an axis.

### **EMP Results**

**Note:** The statistics in this report are based on ranges in the following instances: if you selected **EMP** as the **MSA Method** and **Range** as the **Chart Dispersion Type**, and you have a one factor or a two factor, balanced, crossed model. Otherwise, the statistics in this report are based on variances.

The EMP Results report computes several statistics to help you assess and classify your measurement system. Using this report, you can determine the following:

- How your process chart is affected.
- Which tests to set.
- How much the process signal is attenuated.
- How much the bias factors are affecting your system and reducing your potential intraclass correlation coefficient.

The EMP Results report contains the following calculations:

**Test-Retest Error** Indicates measurement variation or repeatability (also known as within error or pure error).

**Degrees of Freedom** Indicates the amount of information used to estimate the within error.

**Probable Error** The median error for a single measurement. Indicates the resolution quality of your measurement and helps you decide how many digits to use when recording measurements. See "Effective Resolution".

**Intraclass Correlation** Indicates the proportion of the total variation that you can attribute to the part. If you have very little measurement variation, this number is closer to 1.

**Intraclass Correlation (no bias)** Does not take bias or interaction factors into account when calculating the results.

**Intraclass Correlation (with bias)** Takes the bias factors (such as operator, instrument, and so on) into account when calculating the results.

**Intraclass Correlation (with bias and interaction)** Takes the bias and interaction factors into account when calculating the results. This calculation appears only if the model is crossed and uses standard deviation instead of range.

**Bias Impact** The amount by which the bias factors reduce the Intraclass Correlation.

**Bias and Interaction Impact** The amount by which the bias and interaction factors reduce the Intraclass Correlation. This calculation appears only if the model is crossed and uses standard deviation instead of range.

#### Classes of Process Monitors

In order to understand the System and Classification parameters, you must first understand the Monitor Classification Legend.

Figure 4.6 Monitor Classification Legend

Correlation	Process Signal		
0.80 - 1.00	Less than 11%	Warning, Test 1 Only* 0.99 - 1.00	Warning, Tests 1-4* 1.00
0.50 - 0.80	11% - 29%	0.88 - 0.99	1.00
0.20 - 0.50	29% - 55%	0.40 - 0.88	0.92 - 1.00
0.00 - 0.20	More than 55%	0.03 - 0.40	0.08 - 0.92
)	.50 - 0.80 .20 - 0.50	.50 - 0.80	.50 - 0.80

This legend describes the following classifications: First, Second, Third, and Fourth Class. Each classification indicates the following:

- the corresponding Intraclass Correlation values
- the amount of process signal attenuation (decrease)
- the chance of detecting a 3 standard error shift within 10 subgroups, using Wheeler's test one or all four tests

Wheeler (2006) identifies four detection tests known as the Western Electric Zone Tests. Within the Shift Detection Profiler, there are eight tests that you can select from. The tests that correspond to the Wheeler tests are the first, second, fifth, and sixth tests.

**Tip:** To prevent the legend from appearing, deselect **Show Monitor Classification Legend** in the EMP Measurement Systems Analysis platform preferences.

### **Effective Resolution**

The Effective Resolution report helps you determine how well your measurement increments are working. You might find that you need to add or drop digits when recording your measurements, or your current increments might be effective as is. Note the following:

- The Probable Error calculates the median error of a measurement.
- The Current Measurement Increment reflects how many digits you are currently rounding
  to and is taken from the data as the nearest power of ten. This number is compared to the
  Smallest Effective Increment, Lower Bound Increment, and Largest Effective Increment.
  Based on that comparison, a recommendation is made.

Shift Detection Profiler

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# Large measurement increments have less uncertainty in the last digit, but large median errors. Small measurement increments have small median errors, but more uncertainty in the last digit.

Use the Shift Detection Profiler to assess the sensitivity of the control chart that you use to monitor your process. The Shift Detection Profiler estimates the probability of detecting shifts in the product mean or product standard deviation. The control chart limits include sources of measurement error variation. Based on these limits, the Shift Detection Profiler estimates the Probability of Warning. This is the probability that a control chart monitoring the process mean signals a warning over the next k subgroups.

You can set the subgroup size that you want to use for your control chart. Note the following:

- If the Subgroup Size equals one, the control chart is an Individual Measurement chart.
- If the Subgroup Size exceeds one, the control chart is an XBar-chart.

You can explore the effect of Subgroup Size on the control chart's sensitivity. You can also explore the benefits of reducing bias and test-retest error.

Figure 4.7 shows the Shift Detection Profiler report for the Gasket.jmp sample data table, found in the Variability Data folder.

Probability of Warning 161.0 8.0 0.6 0.4 10 23.039 4.4535 3.4928 Number of Part Part Bias Factors Test-Retest Subgroup Subaroups Mean Shift Std Dev Std Dev Std Dev In-Control Part Std Dev 23.03937 In-Control Chart Sigma 23.72437 False Alarm Probability 0.02667 Definition Part Mean Shift The size of the shift in the part mean Part Std Dev The part standard deviation after a shift. Bias Factors Std Dev Reproducibility (such as operators, days, instruments, interactions) standard deviation. Test-Retest Std Dev Repeatability (within) standard deviation. Test description 3 One point beyond n sigma - Wheeler's Rule 1 9 n points in a row on a single side of the center line - Wheeler's Rule 4 (when n = 8) 6 n points in a row steadily increasing or decreasing 14 n points in a row alternating up and down 2 n out of n+1 points in a row beyond 2 sigma - Wheeler's Rule 2 4 n out of n+1 points in a row beyond 1 sigma - Wheeler's Rule 3 15 n points in a row between +/- 1 sigma around the center line 8 n points in a row on both sides of the center line with none within a distance of 1 sigma Note: Tests 2, 5, and 6 apply to the upper and lower halves of the chart separately. Restore Default Settings Save Settings to Preferences

**Figure 4.7** Shift Detection Profiler for Gasket.jmp

### **Probability of Warning**

The Probability of Warning is the probability of detecting a change in the process. A change is defined by the Part Mean Shift and the Part Std Dev settings in the Shift Detection Profiler. The probability calculation assumes that the tests selected in the Customize and Select Tests outline are applied to the Number of Subgroups specified in the Profiler.

The control limits for the Individual Measurement chart (Subgroup Size = 1) and the XBar-chart (Subgroup Size > 1) are based on the In-Control Chart Sigma. The In-Control Sigma takes into account the bias factor (reproducibility) variation and the test-retest (repeatability) variation. These are initially set to the values obtained from your MSA study. The In-Control Chart Sigma also incorporates the In-Control Part Std Dev. Both of these values appear beneath the profiler, along with the False Alarm Probability, which is based on the In-Control Chart Sigma.

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**In-Control Part Std Dev** The standard deviation for the true part values, exclusive of measurement errors, for the stable process. The default value for In-Control Part Std Dev is the standard deviation of the part component estimated by the MSA analysis and found in the Variance Components report.

Often, parts for an MSA study are chosen to have specific properties and do not necessarily reflect the part-to-part variation seen in production. For this reason, you can specify the in-control part standard deviation by selecting **Change In-Control Part Std Dev** from the Shift Detection Profiler red triangle menu.

**In-Control Chart Sigma** The value of sigma used to compute control limits. This value is computed using the In-Control Part Std Dev, the Bias Factors Std Dev, and Test-Retest Std Dev specified in the Shift Detection Profiler, and the Subgroup Size. The reproducibility factors are assumed to be constant within a subgroup.

For a subgroup of size *n*, control limits are set at the following values:

 $\pm 3$ (In-Control Chart Sigma)/ $(\sqrt{n})$ 

It follows that the In-Control Chart Sigma is the square root of the sum of the squares of the following terms:

- In-Control Part Std Dev
- Bias Factors Std Dev, as specified in the Shift Detection Profiler, multiplied by  $\sqrt{n}$
- Test-Retest Std Dev, as specified in the Shift Detection Profiler

The Bias Factors Std Dev is multiplied by  $\sqrt{n}$  to account for the assumption that the reproducibility factors are constant within a subgroup.

JMP updates the In-Control Chart Sigma when you change the In-Control Part Std Dev, the Bias Factors Std Dev, the Test-Retest Std Dev, or the Subgroup Size.

**False Alarm Probability** The probability that the control chart tests signal a warning when no change in the part mean or standard deviation has occurred. JMP updates the False Alarm Probability when you change the Number of Subgroups or the tests in Customize and Select Tests.

For more information about the Variance Components report, see "Variance Components".

### Shift Detection Profiler Settings

**Number of Subgroups** The number of subgroups over which the probability of a warning is computed. If the number of subgroups is set to *k*, the profiler gives the probability that the control chart signals at least one warning based on these *k* subgroups. The Number of Subgroups is set to 10 by default. Drag the vertical line in the plot to change the Number of Subgroups.

- **Part Mean Shift** The shift in the part mean. By default, the profiler is set to detect a 1 sigma shift. The initial value is the standard deviation of the part component estimated by the MSA analysis and found in the Variance Components report. Drag the vertical line in the plot or click the value beneath the plot to change the Part Mean Shift.
- **Part Std Dev** The standard deviation for the true part values, exclusive of measurement errors. The initial value for Part Std Dev is the standard deviation of the part component estimated by the MSA analysis and is found in the Variance Components report. Drag the vertical line in the plot or click the value beneath the plot to change the Part Std Dev.
- **Bias Factors Std Dev** The standard deviation of factors related to reproducibility. Bias factors include operator and instrument. The bias factor variation does not include part and repeatability (within) variation. The initial value is derived using the reproducibility and interaction variance components estimated by the MSA analysis and is found in the Variance Components report. Drag the vertical line in the plot or click the value beneath the plot to change the Bias Factors Std Dev.
- **Test-Retest Std Dev** The standard deviation of the test-retest, or repeatability, variation in the model. The initial value is the standard deviation of the Within component estimated by the MSA analysis and is found in the Variance Components report. Drag the vertical line in the plot or click the value beneath the plot to change the Test-Retest Std Dev.
- **Subgroup Size** The sample size used for each subgroup. This is set to 1 by default. You can increase the sample size to investigate improvement in control chart performance. Increasing the sample size from 1 demonstrates what happens when you move from an Individual Measurement chart to an XBar-chart. Drag the vertical line in the plot to change the Subgroup Size.

### **Shift Detection Profiler Options**

The red triangle menu for the Shift Detection Profiler provides several options. Only one option is described here.

- **Change In-Control Part Std Dev** Specify a value for the part standard deviation for the stable process. The in-control part standard deviation should reflect the variation of the true part values, exclusive of measurement errors. Enter a new value and click OK.
  - The In-Control Part Std Dev is originally set to the standard deviation of the part component estimated by the MSA analysis, found in the Variance Components report.
  - This option is useful if the parts chosen for the EMP study were not a random sample from the process.
- **Reset Factor Grid** Displays a window for each factor allowing you to enter a specific value for the factor's current setting, to lock that setting, and to control aspects of the grid. See *Profilers*.

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**Factor Settings** Submenu that consists of the following options:

**Remember Settings** Adds an outline node to the report that accumulates the values of the current settings each time the Remember Settings command is invoked. Each remembered setting is preceded by a radio button that is used to reset to those settings. There are options to remove selected settings or all settings in the Remember Settings red triangle menu.

**Copy Settings Script** Copies the current Profiler's settings to the clipboard.

**Paste Settings Script** Pastes the Profiler settings from the clipboard to a Profiler in another report.

**Set Script** Sets a script that is called each time a factor changes. The set script receives a list of arguments of the form:

```
{factor1 = n1, factor2 = n2, ...}
For example, to write this list to the log, first define a function:
ProfileCallbackLog = Function({arg}, show(arg));
Then enter ProfileCallbackLog in the Set Script dialog.
Similar functions convert the factor values to global values:
ProfileCallbackAssign = Function({arg}, evalList(arg));
Or access the values one at a time:
ProfileCallbackAccess =
Function({arg}, f1=arg["factor1"]; f2=arg["factor2"]);
```

### **Shift Detection Profiler Legend**

This panel gives a brief description of four of the Shift Detection Profiler settings. See "Shift Detection Profiler Settings".

**Tip:** To prevent the legend from appearing, deselect **Show Shift Detection Profiler Legend** in the EMP Measurement Systems Analysis platform preferences.

#### **Customize and Select Tests**

In the Customize and Select Tests panel, select and customize the tests that you want to apply to the *k* subgroups in your control chart. The eight tests are based on Nelson (1984). For more information about the tests, see "Tests".

The Shift Detection Profiler calculations take these tests into account. The Probability of Warning and False Alarm Probability values increase as you add more tests. Because the calculations are based on a quasi-random simulation, there might be a slight delay as the profiler is updated.

The Customize and Select Tests panel has the following options:

**Restore Default Settings** If no settings have been saved to preferences, this option resets the selected tests to the first test only. The values of *n* are also reset to the values described in "Tests". If settings have been saved to preferences, this option resets the selected tests and the values of *n* to those specified in the preferences.

**Note:** You can access preferences for control chart tests by selecting **File > Preferences > Platforms > Control Chart Builder**. Custom Tests 1 through 8 correspond to the eight tests shown in Customize and Select Tests.

**Save Settings to Preferences** Saves the selected tests and the values of *n* for use in future analyses. These preferences are added to the Control Chart Builder platform preferences.

### **Bias Comparison**

The **Bias Comparison** option creates an Analysis of Means chart. This chart shows the mean values for each level of the grouping variables and compares them with the overall mean. You can use this chart to see whether an operator is measuring parts too high or too low, on average.

The red triangle menu next to Analysis of Means contains the following options:

**Set Alpha Level** Select an option from the most common alpha levels or specify any level using the **Other** selection. Changing the alpha level modifies the upper and lower decision limits.

**Show Summary Report** Shows a report containing group means and decision limits, and reports if the group mean is above the upper decision limit or below the lower decision limit.

**Display Options** Include the following options:

**Show Decision Limits** Draws lines representing the Upper Decision Limit (UDL) and the Lower Decision Limit (LDL) and defines those values.

**Show Decision Limit Shading** Adds shading between the UDL and the LDL.

**Show Center Line** Draws the center line statistic that represents the average.

**Point Options** Changes the chart display to needles, connected points, or points.

### **Test-Retest Error Comparison**

The **Test-Retest Error Comparison** option creates a type of Analysis of Means for Variances or Analysis of Means Ranges chart. This chart shows if there are differences in the test-retest error between operators. For example, you can use this chart to see whether there is an inconsistency in how each operator is measuring. The Analysis of Mean Ranges chart is displayed when ranges are used for variance components.

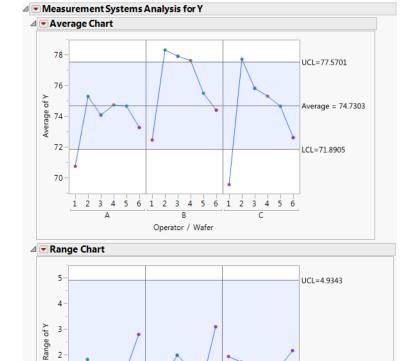
- For information about the options in the red triangle menu next to Operator Variance Test, see "Bias Comparison".
- For more information about Analysis of Means for Variances charts, see "Variance Components".

# Additional Example of Measurement Systems Analysis

In this example, three operators have measured a single characteristic twice on each of six wafers. Perform a detailed analysis to find out how well the measurement system is performing.

### **Perform the Initial Analysis**

- 1. Select **Help > Sample Data Library** and open Variability Data/Wafer.jmp.
- 2. Select Analyze > Quality and Process > Measurement Systems Analysis.
- 3. Assign Y to the Y, Response role.
- 4. Assign Wafer to the **Part, Sample ID** role.
- 5. Assign Operator to the **X, Grouping** role.
  - Notice that the **MSA Method** is set to **EMP**, the **Chart Dispersion Type** is set to **Range**, and the **Model Type** is set to **Crossed**.
- 6. Click **OK**.



5 6

Operator / Wafer

• 5

• 4

**Figure 4.8** Average and Range Charts

The Average Chart shows that some of the average part measurements fall beyond the control limits. This is desirable, indicating measurable part-to-part variation.

Average Range = 1.5106

LCL=0.0000

The Range Chart shows no points that fall beyond the control limits. This is desirable, indicating that the operator measurements are consistent within part.

#### **Examine Interactions**

5 6

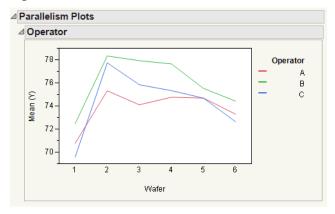
• 2

0

Wafer

Take a closer look for interactions between operators and parts. Click the red triangle next to Measurement Systems Analysis for Y and select **Parallelism Plots**.

**Figure 4.9** Parallelism Plot

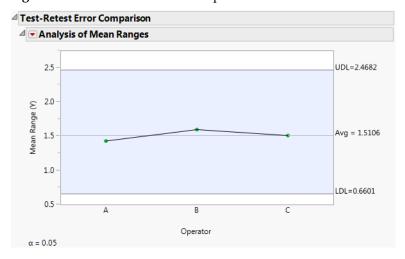


Looking at the parallelism plot by operator, you can see that the lines are relatively parallel and that there is only some minor crossing.

### **Examine Operator Consistency**

Take a closer look at the variance between operators. Click the red triangle next to Measurement Systems Analysis for Y and select **Test-Retest Error Comparison**.

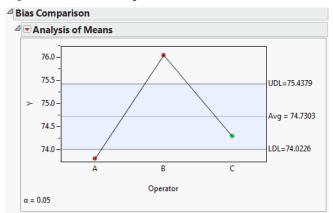
Figure 4.10 Test-Retest Error Comparison



Looking at the Test-Retest Error Comparison, you can see that none of the operators have a test-retest error that is significantly different from the overall test-retest error. The operators appear to be measuring consistently.

Just to be sure, you decide to look at the Bias Comparison chart, which indicates whether an operator is measuring parts too high or too low. Click the red triangle next to Measurement Systems Analysis for Y and select **Bias Comparison**.

Figure 4.11 Bias Comparison



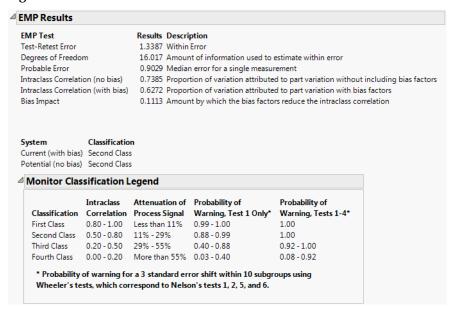
Looking at the Bias Comparison chart, you make the following observations:

- Operator A and Operator B have detectable measurement bias, as they are significantly different from the overall average.
- Operator A is significantly biased low.
- Operator B is significantly biased high.
- Operator C is not significantly different from the overall average.

### **Classify Your Measurement System**

Examine the EMP Results report to classify your measurement system and look for opportunities for improvement. Click the red triangle next to Measurement Systems Analysis for Y and select **EMP Results**.

Figure 4.12 EMP Results



The classification is Second Class, which means that there is a better than 88% chance of detecting a three standard error shift within ten subgroups, using Test one only. You notice that the bias factors have an 11% impact on the Intraclass Correlation. In other words, if you could eliminate the bias factors, your Intraclass Correlation coefficient would improve by 11%.

### Explore the Ability of a Control Chart to Detect Process Changes

Use the Shift Detection Profiler to explore the probability that a control chart will be able to detect a change in your process. Click the red triangle next to Measurement Systems Analysis for Y and select **Shift Detection Profiler**.

Additional Example of Measurement Systems Analysis





By default, the only test selected is for a point beyond the 3 sigma limits. Also note that the default Subgroup Size is 1, indicating that you are using an Individual Measurement chart.

Explore your ability to detect a shift in the mean of two part standard deviations in the 10 subgroups following the shift. Click the **Part Mean Shift** value of 2.1701 and change it to 4.34 (2.17 multiplied by 2). The probability of detecting a shift of twice the part standard deviation is 56.9%.

Next, see how eliminating bias affects your ability to detect the shift of two part standard deviations. Change the **Bias Factors Std Dev** value from 1.1256 to 0. The probability of detecting the shift increases to 67.8%.

Finally, add more tests to see how your ability to detect the two part standard deviation shift changes. In addition to the first test, select the second, fifth, and sixth tests (Wheeler's Rules 4, 2, and 3). With these four tests and no bias variation, your probability of detecting the shift is 99.9%.

You can also explore the effect of using a control chart based on larger subgroup sizes. For subgroup sizes of two or more, the control chart is an XBar-chart. Change the **Bias Factors Std Dev** value back to 1.1256 and deselect all but the first test. Set the **Subgroup Size** in the profiler to 4. The probability of detecting the two part standard deviation shift is 98.5%.

Chapter 4

#### **Examine Measurement Increments**

Finally, see how well your measurement increments are working. Click the red triangle next to Measurement Systems Analysis for Y and select **Effective Resolution**.

**Figure 4.14** Effective Resolution

Source		Value	Description
Probable Error	(PE)	0.9029	Median error for a single measurement
Current Measurement Increment	(MI)	0.01	Measurement increment estimated from data (in tenths)
Lower Bound Increment	(0.1*PE)	0.0903	Measurement increment should not be below this value
Smallest Effective Increment	(0.22*PE)	0.1986	Measurement increment is more effective above this valu
Largest Effective Increment	(2.2*PE)	1.9865	Measurement increment is more effective below this valu
Action: Drop a digit Reason: The measurement incre measurement increment bound of fewer digits.			

The Current Measurement Increment of 0.01 is below the Lower Bound Increment of 0.09, indicating that you should adjust your future measurements to record one less digit.

# Statistical Details for Measurement Systems **Analysis**

For more information about the calculations of the limits used in the Range Chart, see "Control Limits for XBar and R Charts". For more information about the calculations of the limits used in the Standard Deviation Chart, see "Control Limits for XBar and S Charts".

## Computation of Intraclass Correlation and Probable Error

Intraclass Correlation without bias is computed as follows:

$$r_{pe} = \frac{\hat{\sigma}_p^2}{\hat{\sigma}_p^2 + \hat{\sigma}_{pe}^2}$$

Intraclass Correlation with bias is computed as follows:

$$r_b = \frac{\hat{\sigma}_p^2}{\hat{\sigma}_p^2 + \hat{\sigma}_b^2 + \hat{\sigma}_{pe}^2}$$

Statistical Details for Measurement Systems Analysis

Intraclass Correlation with bias and interaction factors is computed as follows:

$$r_{int} = \frac{\hat{\sigma}_p^2}{\hat{\sigma}_p^2 + \hat{\sigma}_b^2 + \hat{\sigma}_{int}^2 + \hat{\sigma}_{pe}^2}$$

Probable Error is computed as follows:

$$Z_{0.75 \times \hat{\sigma}_{pe}}$$

Note the following:

 $\hat{\sigma}_{pe}^2$  = variance estimate for pure error

 $\hat{\sigma}_p^2$  = variance estimate for product

 $\hat{\sigma}_b^2$  = variance estimate for bias factors

 $\hat{\sigma}_{int}^2$  = variance estimate for interaction factors

 $Z_{0.75}$  = the 75% quantile of standard normal distribution

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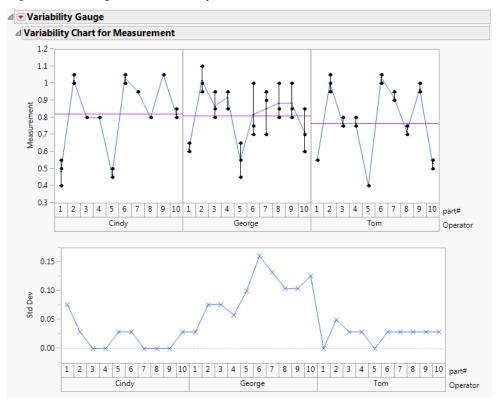
# **Variability Gauge Charts**

### **Evaluate a Continuous Measurement Process Using Gauge R&R**

Variability gauge charts analyze continuous measurements and can reveal how your measurement system is performing. You can also perform a gauge study to see measures of variation in your data.

**Tip:** This chapter covers only variability charts. For more information about attribute charts, see "Attribute Gauge Charts".

Figure 5.1 Example of a Variability Chart



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# **Overview of Variability Charts**

**Tip:** The traditional name for a variability chart is a *multi vari* chart, but because that name is not well known, the more generic term variability chart is used instead.

Just as a control chart shows variation across time in a process, a variability chart shows the same type of variation across categories such as parts, operators, repetitions, and instruments. A variability chart plots the data and means for each level of grouping factors, with all plots side by side. Along with the data, you can view the mean, range, and standard deviation of the data in each category, seeing how they change across the categories. The report options are based on the assumption that the primary interest is how the mean and variance change across the categories.

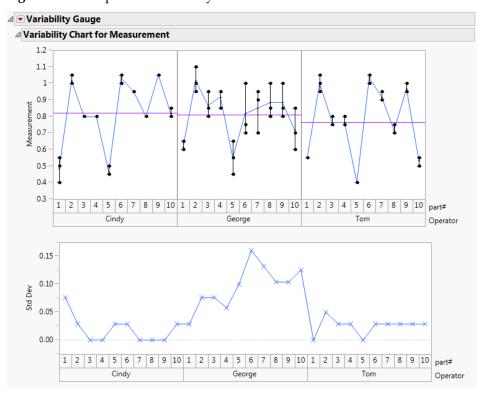
Variability charts are commonly used for measurement systems analysis such as Gauge R&R. This analysis examines how much of the variability is due to operator variation (reproducibility) and measurement variation (repeatability). Gauge R&R is available for many combinations of crossed and nested models, regardless of whether the model is balanced.

# **Example of a Variability Chart**

Suppose that you have data containing part measurements. Three operators, Cindy, George, and Tom, each took measurements of 10 parts. They measured each part three times, making a total of 90 observations. You want to identify the variation between operators.

- 1. Select Help > Sample Data Library and open Variability Data/2 Factors Crossed.jmp.
- 2. Select Analyze > Quality and Process > Variability / Attribute Gauge Chart.
- 3. For Chart Type, select Variability.
- 4. Select Measurement and click Y, Response.
- 5. Select Operator and click **X, Grouping**.
- 6. Select part# and click Part, Sample ID.
- 7. Click **OK**.
- Click the Variability Gauge red triangle and select Show Group Means and Connect Cell Means.

Figure 5.2 Example of a Variability Chart

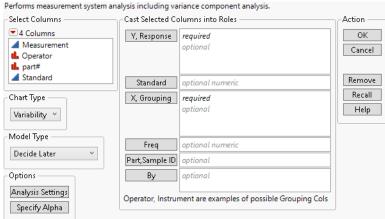


Looking at the Std Dev chart, you can see that Cindy and George have more variation in their measurements than Tom, who appears to be measuring parts the most consistently. George seems to have the most variation in his measurements, so he might be measuring parts the most inconsistently.

# Launch the Variability/Attribute Gauge Chart Platform

Launch the Variability/Attribute Gauge Chart platform by selecting **Analyze > Quality and Process > Variability/Attribute Gauge Chart**. Set the **Chart Type** to **Variability**.

Figure 5.3 The Variability/Attribute Gauge Chart Launch Window



For more information about the options in the Select Columns red triangle menu, see *Using IMP*.

**Chart Type** Choose between a variability gauge analysis (for a continuous response) or an attribute gauge analysis (for a categorical response, usually "pass" or "fail").

**Note:** The content in this chapter covers only the **Variability** chart type. For more information about the **Attribute** chart type, see "Attribute Gauge Charts".

**Model Type** Choose the model type (**Main Effect, Crossed, Nested**, and so on). See "Statistical Details for Variance Components".

**Analysis Settings** Specify the method for computing variance components. See "Analysis Settings".

**Specify Alpha** Specify the alpha level used by the platform.

- **Y, Response** Specify the measurement column. Specifying more than one *Y* column produces a separate variability chart for each response.
- **Standard** Specify a standard or reference column that contains the "true" or known values for the measured part. Including this column enables the **Bias** and **Linearity Study** options. These options perform analysis on the differences between the observed measurement and the reference or standard value. See "Bias Report" and "Linearity Study".
- **X, Grouping** Specify the classification columns that group the measurements. If the factors form a nested hierarchy, specify the higher terms first. If you are doing a gauge study, specify the operator first and then the part.
- **Freq** Identifies the data table column whose values assign a frequency to each row. Can be useful when you have summarized data.
- **Part, Sample ID** Identifies the part or sample that is being measured.
- **By** Identifies a column that creates a report consisting of separate analyses for each level of the variable.

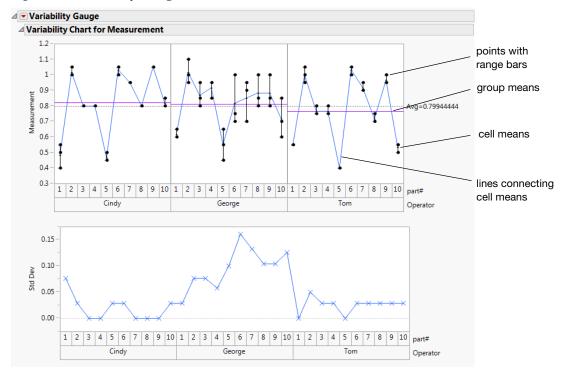
#### **Data Format**

To use the Variability Chart platform, all response measurements must be in a single response column. Sometimes, responses are recorded in multiple columns, where each row is a level of a design factor and each column is a level of a different design factor. Data that are in this format must be stacked before running the Variability Chart platform. See *Using JMP*.

# The Variability Gauge Chart

The variability chart and the standard deviation chart show patterns of variation. You can use these charts to identify possible groups of variation (within subgroups, between subgroups, over time). If you notice that any of these sources of variation are large, you can then work to reduce the variation for that source.

Follow the instructions in "Example of a Variability Chart" to produce the results shown in Figure 5.4.



**Figure 5.4** Variability Gauge Chart

The charts show the response on the *y*-axis and a multilevel, categorized *x*-axis.

In Figure 5.4, the Measurement chart shows the range of measurements for each operator by part. Each measurement appears on the chart. Maximum and minimum bars indicate the range of values for each cell, and a cell means bar indicates the median value for each combination of values. The Std Dev chart plots the standard deviation of the measurements taken on each part by operator.

You can add features to the charts, as illustrated in Figure 5.4. See "Variability Gauge Platform Options".

To replace variables in charts, do one of the following:

- Swap existing variables by dragging a variable from one axis label to the other axis label. When you drag a variable over a chart or click an axis label, the axis labels are highlighted. This indicates where to drop the variable.
- Click a variable in the Columns panel of the associated data table and drag it onto an axis label.

In other platforms, rows that are excluded in the associated data table still appear on the charts or plots. However, in variability charts, excluded rows do not appear on the charts.

# Variability Gauge Platform Options

Use the red triangle options to modify the appearance of the chart, perform Gauge R&R analysis, and compute variance components.

**Note:** Figure 5.4 illustrates some of these options.

**Tip:** To set the default behavior of these options, select **File > Preferences > Platforms > Variability Chart**.

**Vertical Charts** Changes the layout to horizontal or vertical.

**Variability Chart** Shows or hides the variability chart.

**Show Points** Shows or hides the points for individual rows.

**Show Range Bars** Shows or hides the bars indicating the minimum and the maximum value of each cell.

**Show Cell Means** Shows or hides the mean mark for each cell.

**Connect Cell Means** Connects or disconnects cell means within a group of cells.

**Show Separators** Shows or hides the separator lines between levels of the **X**, **Grouping** variables.

**Show Group Means** (Available only if you have two or more X, Grouping variables or one X, Grouping variable and one Part, Sample ID variable.) Shows or hides the mean for groups of cells, represented by a horizontal solid line. A window appears, prompting you to select one of the grouping variables.

**Show Grand Mean** Shows or hides the overall mean, represented by a gray dotted line across the entire graph.

**Show Grand Median** Shows or hides the overall median, represented by a blue dotted line across the entire graph.

**Show Box Plots** Shows or hides box plots.

**Mean Diamonds** Shows or hides mean diamonds. The confidence intervals use the within-group standard deviation for each cell.

**XBar Control Limits** Shows or hides lines at the UCL and LCL on the variability chart. For more information about the calculations of these limits, see "Statistical Details for Control Chart Builder".

- **Points Jittered** Adds some random noise to the plotted points so that coincident points do not plot on top of one another.
- **Show Standard Mean** (Available only if you have specified a **Standard** variable.) Shows or hides the mean of the standard column.
- **Variability Summary Report** Shows or hides a report that gives the mean, standard deviation, coefficient of variation (CV), standard error of the mean, lower and upper confidence intervals, and the minimum, maximum, and number of observations.
- **Std Dev Chart** Shows or hides a separate graph that shows cell standard deviations across category cells.
- **Mean of Std Dev** Shows or hides a line at the mean standard deviation on the Std Dev chart.
- **S Control Limits** Shows or hides lines showing the LCL and UCL in the Std Dev chart. For more information about the calculations of these limits, see "Statistical Details for Control Chart Builder".
- **Group Means of Std Dev** Shows or hides the mean lines on the Std Dev chart.
- **Heterogeneity of Variance Tests** Performs a test for comparing variances across groups. See "Heterogeneity of Variance Tests".
- **Variance Components** Estimates the variance components for a specific model. Variance components are computed for these models: main effects, crossed, nested, crossed then nested (three factors only), and nested then crossed (three factors only). See "Variance Components".
- **Gauge Studies** Contains the following options:
  - **Gauge R&R** Interprets the first factors as grouping columns and the last factor as Part, and creates a gauge R&R report using the estimated variance components. (Note that there is also a Part field in the launch window). See "Gauge R&R Option".
  - **Discrimination Ratio** Characterizes the relative usefulness of a given measurement for a specific product. It compares the total variance of the measurement with the variance of the measurement error. See "Discrimination Ratio".
  - **Misclassification Probabilities** Shows probabilities for rejecting good parts and accepting bad parts. See "Misclassification Probabilities".
  - **Bias Report** Shows the average difference between the observed values and the standard. A graph of the average biases and a summary table appears. This option is available only when you specify a Standard variable in the launch window. See "Bias Report".

- **Linearity Study** Performs a regression using the standard values as the X variable and the bias as the Y variable. This analysis examines the relationship between bias and the size of the part. Ideally, you want the slope to equal 0. A nonzero slope indicates that your gauge performs differently with different sized parts. This option is available only when you specify a Standard variable in the launch window. See "Linearity Study".
- **Gauge R&R Plots** Shows or hides Mean Plots (the mean response by each main effect in the model) and Std Dev plots. If the model is purely nested, the graphs appear with a nesting structure. If the model is purely crossed, interaction graphs appear. Otherwise, the graphs plot independently at each effect. For the standard deviation plots, the red lines connect  $\sqrt{\text{mean weighted variance}}$  for each effect.
- **AIAG Labels** Enables you to specify that quality statistics should be labeled in accordance with the AIAG standard, which is used extensively in automotive analyses.

See *Using JMP* for more information about the following options:

- **Local Data Filter** Shows or hides the local data filter that enables you to filter the data used in a specific report.
- **Redo** Contains options that enable you to repeat or relaunch the analysis. In platforms that support the feature, the Automatic Recalc option immediately reflects the changes that you make to the data table in the corresponding report window.
- **Save Script** Contains options that enable you to save a script that reproduces the report to several destinations.
- **Save By-Group Script** Contains options that enable you to save a script that reproduces the platform report for all levels of a By variable to several destinations. Available only when a By variable is specified in the launch window.

### **Heterogeneity of Variance Tests**

**Note:** See "Example of the Heterogeneity of Variance Test".

The **Heterogeneity of Variance Tests** option performs a test for comparing variances across groups. The test is an Analysis of Means for Variances (ANOMV) based method. This method indicates whether any of the group standard deviations are different from the square root of the average group variance.

To be robust against non-normal data, the method uses a permutation simulation to compute decision limits. For more information about this method, see Wludyka and Sa (2004). Because the method uses simulations, the decision limits can be slightly different each time. To obtain the same results each time, press Ctrl+Shift, select the option, and then specify the same random seed.

The red triangle menus for the test reports contain the following options:

**Set Alpha Level** Sets the alpha level for the test.

**Show Summary Report** Shows or hides a summary report for the test. The values in the report are the same values that are shown in the plot.

**Display Options** Shows or hides the decision limits, shading, center line, and needles.

### **Variance Components**

The **Variance Components** option models the variation from measurement to measurement. The response is assumed to be a constant mean plus random effects associated with various levels of the classification.

**Note:** Once you select the **Variance Components** option, if you did not select the **Model Type** in the launch window (if you selected **Decide Later**), you are prompted to select the model type. For more information about model types, see "Launch the Variability/Attribute Gauge Chart Platform".

Figure 5.5 Example of the Variance Components Report

Analysis of \	/aria	nce				
Source	DF	SS	Mean Squ	ıare	F Ratio	Prob > F
Operator	2	0.054889	0.02	744	1.3150	0.2931
part#	9	2.633583	0.29	262	14.0209	<.0001*
Operator*part#	18	0.375667	0.02	2087	5.0425	<.0001*
Within	60	0.248333	0.00	414		
Total	89	3.312472	0.03	3722		
Variance Components						
		Var				Sqrt(Va
Component	Com	ponent	% of Total	20	40 60 80	Comp
Operator	0.0	0021914	0.5461			0.0148
part#	0.0	3019444	75.2			0.1737
Operator*part#	0.0	0557716	13.9			0.0746
Within	0.0	0413889	10.3			0.0643
Total	0.0	4012963	100.0			0.2003

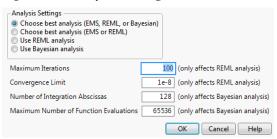
The Analysis of Variance report appears only if the EMS method of variance component estimation is used. This report shows the significance of each effect in the model.

The Variance Components report shows the estimates themselves. See "Statistical Details for Variance Components".

### **Analysis Settings**

From the launch window, click **Analysis Settings** to choose the method for computing variance components.

Figure 5.6 Analysis Settings Window



**Choose best analysis (EMS, REML, or Bayesian)** Chooses the best analysis from EMS, REML, or Bayesian, using the following logic:

- If the data are balanced, and if no variance components are negative, the EMS (expected mean squares) method is used to estimate the variance components.
- If the data are unbalanced, the REML (restricted maximum likelihood) method is used, unless a variance component is estimated to be negative, then the Bayesian method is used.
- If any variance component is estimated to be negative using the EMS method, the Bayesian method is used.
- If there is confounding in the variance components, then the bounded REML method is used, and any negative variance component estimates are set to zero.

**Choose best analysis (EMS or REML)** Chooses the best analysis from EMS or REML, using the same logic as the **Choose best analysis (EMS, REML, or Bayesian)** option. However, this option never uses the Bayesian method, even for negative variance components. The bounded REML method is used and any negative variance component is forced to be 0.

**Use REML analysis** Uses the bounded REML method, even if the data are balanced. The bounded REML method can handle unbalanced data and forces any negative variance component to be 0.

**Use Bayesian analysis** Uses the Bayesian method. The Bayesian method can handle unbalanced data and forces all variances components to be positive and nonzero. If there is confounding in the variance components, then the bounded REML method is used, and any negative variance component estimates are set to zero. The method implemented in JMP computes the posterior means using a modified version of Jeffreys' prior. See Portnoy (1971) and Sahai (1974).

**Maximum Iterations** (Applicable only for the REML method.) For difficult problems, you might want to increase the number of iterations. Increasing this value means that JMP will try more times to find a solution in the optimization phase.

**Convergence Limit** (Applicable only for the REML method.) For problems where you want greater precision, you might want to change the convergence limit to be smaller.

Decreasing this value means that JMP will find the solution to a higher level of accuracy in the optimization phase. However, this can increase the time taken to find a solution. Providing a larger convergence value returns quicker results, but is less precise.

**Number of Iteration Abscissas** (Applicable only for the Bayesian method.) For greater accuracy, you might want to increase the number of iteration abscissas. However, this can increase the time taken to find a solution. Providing a smaller number returns quicker results, but is less precise.

**Maximum Number of Function Evaluations** (Applicable only for the Bayesian method.) For greater accuracy, you might want to increase the maximum number of function evaluations. However, this can increase the time taken to find a solution. Providing a smaller number returns quicker results, but is less precise.

## About the Gauge R&R Method

The Gauge R&R method analyzes how much of the variability in your measurement system is due to operator variation (reproducibility) and measurement variation (repeatability). Gauge R&R studies are available for many combinations of crossed and nested models, regardless of whether the model is balanced.

**Tip:** Alternatively, you can use the EMP method to assess your measurement system. See "Measurement Systems Analysis".

Before performing a Gauge R&R study, you collect a random sample of parts over the entire range of part sizes from your process. Select several operators at random to measure each part several times. The variation is then attributed to the following sources:

- The *process variation*, from one part to another. This is the ultimate variation that you want to be studying if your measurements are reliable.
- The variability inherent in making multiple measurements, that is, *repeatability*. In Table 5.1, this is called the *within variation*.
- The variability due to having different operators measure parts—that is, *reproducibility*.

A Gauge R&R analysis then reports the variation in terms of repeatability and reproducibility.

**Table 5.1** Definition of Terms and Sums in Gauge R&R Analysis

Variances Sums	Term and Abbreviation	Alternate Term
V(Within)	Repeatability (EV)	Equipment Variation

<b>Table 5.1</b> Definition of Terms and Sums in Gauge R&R Analysis ( <i>Continued</i> )
--

Variances Sums	Term and Abbreviation	Alternate Term
V(Operator)+V(Operator*Part)	Reproducibility (AV)	Appraiser Variation
V(Operator*Part)	Interaction (IV)	Interaction Variation
V(Within)+V(Operator)+V(Operator* Part)	Gauge R&R (RR)	Measurement Variation
V(Part)	Part Variation (PV)	Part Variation
V(Within)+V(Operator)+ V(Operator*Part)+V(Part)	Total Variation (TV)	Total Variation

A Shewhart control chart can identify processes that are going out of control over time. A variability chart can also help identify operators, instruments, or part sources that are systematically different in mean or variance.

### **Gauge R&R Option**

The **Gauge R&R** option shows measures of variation interpreted for a gauge study of operators and parts.

Once you select the **Gauge R&R** option, if you have not already selected the model type, you are prompted to do so. Then, modify the Gauge R&R specifications.

**Note:** The Platform preferences for Variability include the Gauge R&R Specification Dialog option. The preference is selected by default. Deselect the preference to use the spec limits that are defined in the data table.

### **Enter/Verify Gauge R&R Specifications**

The Enter/Verify Gauge R&R Specifications window contains these options:

**Choose tolerance entry method** Choose how to enter the tolerance:

Select **Tolerance Interval** to enter the tolerance directly, where tolerance = USL – LSL.

Select **LSL** and/or **USL** to enter the specification limits and then have JMP calculate the tolerance.

**K, Sigma Multiplier K** is a constant value that you choose to multiply with sigma. For example, you might type 6 so that you are looking at 6\*sigma or a 6 sigma process.

**Tip:** Modify the default value of **K** by selecting **File > Preferences > Platforms > Variability Chart**.

**Tolerance Interval, USL-LSL** Enter the tolerance for the process, which is the difference between the upper specification limits and the lower specification limits.

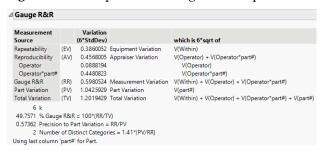
**Spec Limits** Enter upper and lower specification limits. See *Using JMP*.

**Historical Mean** Computes the tolerance range for one-sided specification limits, either USL-Historical Mean or Historical Mean-LSL. If you do not enter a historical mean, the grand mean is used.

**Historical Sigma** Enter a value that describes the variation (you might have this value from history or past experience).

### The Gauge R&R Report

Figure 5.7 Example of the Gauge R&R Report



Full Gauge R&R Report

Reduced Gauge R&R Report

**Note:** To generate the reduced Gauge R&R report, select **File > Preferences > Platforms > Variability Chart > Reduced Gauge R&R Report**.

In this example, the values in the Variation column are the square roots of sums of variance components scaled by the value of k (6 in this example).

Table 5.2 shows guidelines for measurement variation, as suggested by Barrentine (1991).

 Table 5.2 Acceptable Percent Measurement Variation

< 10%	excellent
11% to 20%	adequate
21% to 30%	marginally acceptable
> 30%	unacceptable

#### Note the following:

- If you have provided a **Tolerance Interval** in the Enter/Verify Gauge R&R Specifications window, a % of Tolerance column appears in the Gauge R&R report. This column is computed as 100\*(Variation/Tolerance). Also, a Precision-to-Tolerance ratio appears at the bottom of the report. This ratio represents the proportion of the tolerance or capability interval that is lost due to gauge variability.
- If you have provided a **Historical Sigma** in the Enter/Verify Gauge R&R Specifications window, a % Process column appears in the Gauge R&R report. This column is defined as 100\*(Variation/(K\*Historical Sigma)).
- The Number of Distinct Categories (NDC) is defined as (1.41\*(PV/RR)), rounded down to the nearest integer.

### **Discrimination Ratio**

The discrimination ratio characterizes the relative usefulness of a given measurement for a specific product. Generally, when the discrimination ratio is less than 2, the measurement cannot detect product variation, implying that the measurement process needs improvement. A discrimination ratio greater than 4 adequately detects unacceptable product variation, implying that the production process needs improvement.

See "Statistical Details for the Discrimination Ratio".

# **Misclassification Probabilities**

Due to measurement variation, good parts can be rejected and bad parts can be accepted. This is called misclassification. Misclassification rates decrease as measurement variability decreases. When you select the **Misclassification Probabilities** option, you are prompted to select the model type and enter specification limits if you have not already done so.

Figure 5.8 Example of the Misclassification Probabilities Report

Misclassification Probabilities			
Description	Probability		
P(Good part is falsely rejected)	0.0802		
P(Bad part is falsely accepted)	0.2787		
P(Part is good and is rejected)	0.0735		
P(Part is bad and is accepted)	0.0235		
P(Part is good)	0.9157		

The misclassification probabilities are based on the joint probability function of Y, the measured value of the part, and X, the true value of the part. The joint probability density function used is a bivariate normal distribution. To understand the descriptions, define the following probabilities:

```
\delta = P[(LSL \leq X \leq USL) and (Y < LSL or Y > USL)]

\beta = P[(X < LSL or X > USL) and (LSL \leq Y \leq USL)]

\pi = P(LSL \leq X \leq USL)
```

#### **Descriptions**

**P(Good part is falsely rejected)** The conditional probability that a part is rejected given that it is a good part, or  $\delta/\pi$ .

**P(Bad part is falsely accepted)** The conditional probability that a part is accepted given that it is a bad part, or  $\beta/(1-\pi)$ .

**P(Part is good and is rejected)** The joint probability that a part is good and that it is rejected, or  $\delta$ .

**P(Part is bad and is accepted)** The joint probability that a part is bad and that it is accepted, or  $\beta$ .

**P(Part is good)** The probability that a part is good, or  $\pi$ .

For more information, see "Statistical Details for the Misclassification Probabilities" as well as Burdick et al. (2005).

## **Bias Report**

The **Bias Report** shows a graph for Overall Measurement Bias with a summary table and a graph for Measurement Bias by Standard with a summary table. The average bias, or the differences between the observed values and the standard values, appears for each level of the X variable. A *t* test for the bias is also given.

The **Bias Report** option is available only when a **Standard** variable is provided in the launch window.

The Measurement Bias Report red triangle menu contains the following options:

**Confidence Intervals** Calculates confidence intervals for the average bias for each part and places marks on the Measurement Bias Report by Standard plot.

**Measurement Error Graphs** Produces a graph of Measurement Error versus all grouping columns together. There are also graphs of Measurement Error by each grouping column separately.

## **Linearity Study**

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The **Linearity Study** performs a regression analysis using the standard variable as the X variable and the bias as the Y variable. This analysis examines the relationship between bias and the size of the part. Ideally, you want to find a slope of zero. If the slope is significantly different from zero, you can conclude that there is a significant relationship between the size of the part or variable measured as a standard and the ability to measure.

The **Linearity Study** option is available only when a **Standard** variable is provided in the launch window.

The report shows the following information:

- Bias summary statistics for each standard.
- An ANOVA table that tests if the slope of the line is equal to zero.
- The line parameters, including tests for the slope (linearity) and intercept (bias). The test
  for the intercept is useful only if the test on the slope fails to reject the hypothesis of slope =
  0.
- The equation of the line appears directly beneath the graph.

The Linearity Study red triangle menu contains the following options:

**Set Alpha Level** Changes the alpha level that is used in the bias confidence intervals.

**Linearity by Groups** Produces separate linearity plots for each level of the **X**, **Grouping** variables that you specified in the launch window.

# Additional Examples of Variability Charts

- "Example of the Heterogeneity of Variance Test"
- "Example of the Bias Report Option"

#### **Example of the Heterogeneity of Variance Test**

Suppose that you have data containing part measurements. Three operators (Cindy, George, and Tom) each took measurements of 10 parts. They measured each part three times, making a total of 90 observations. You want to examine the following:

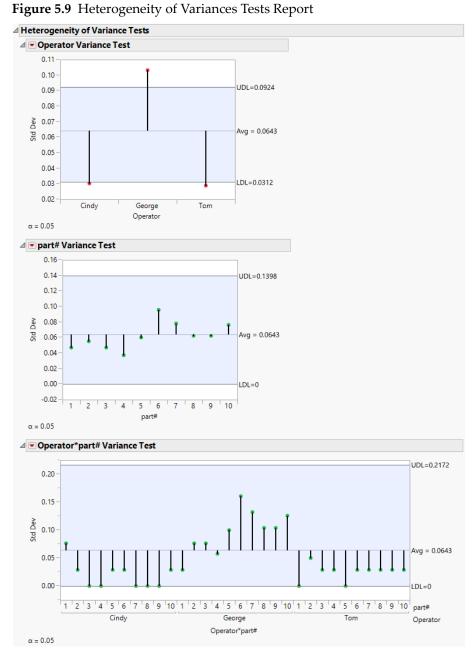
- whether the variance of measurements for each operator are the same or different
- whether the variance for each part is the same or different
- whether the variance for each Operator\*part combination is the same or different

Ideally, you want all of the variances for each of the groups to be considered the same statistically.

- 1. Select Help > Sample Data Library and open Variability Data/2 Factors Crossed.jmp.
- 2. Select Analyze > Quality and Process > Variability / Attribute Gauge Chart.
- 3. Select Measurement and click **Y**, **Response**.
- 4. Select Operator and click **X**, **Grouping**.
- 5. Select part# and click **Part, Sample ID**.
- 6. Click **OK**.
- 7. Click the Variability Gauge red triangle and select **Heterogeneity of Variance Tests**.
- 8. Select Crossed.
- 9. Click **OK**.

Chapter 5

Quality and Process Methods



**Note:** Because the method uses simulations, the decision limits can be slightly different each time.

In the Operator Variance test, all three levels exceed the upper and lower decision limits. From this, you conclude that each operator has a different variability from the square root of the average group variance. You might want to examine why the variation between each operator is different.

For the part# Variance test and the interaction (Operator\*part#) Variance test, none of the levels exceed the decision limits. From this, you conclude that the variances are not statistically different from the square root of the average group variance. Each part has a similar variance to the other parts, and each Operator\*part# combination has similar variance to the other Operator\*part# combinations.

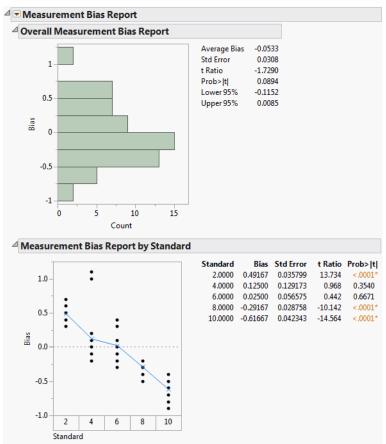
## **Example of the Bias Report Option**

**Note:** These data come from the Automotive Industry Action Group (2002).

Assume that as a plant supervisor, you are introducing a new measurement system into your process. As part of the Production Part Approval Process (PPAP), the bias and linearity of the measurement system needs to be evaluated. Five parts were chosen throughout the operating range of the measurement system, based on documented process variation. Each part was measured by layout inspection to determine its reference value. Each part was then measured twelve times by the lead operator. The parts were selected at random during the day. In this example, you want to examine the overall bias and the individual measurement bias (by standard).

- 1. Select **Help > Sample Data Library** and open Variability Data/MSALinearity.jmp.
- 2. Select Analyze > Quality and Process > Variability / Attribute Gauge Chart.
- 3. Select Response and click **Y**, **Response**.
- Select Standard and click Standard.
- Select Part and click X, Grouping.
- 6. Click OK.
- Click the Variability Gauge red triangle and select Gauge Studies > Bias Report.





The bias (Response minus Standard) is calculated for every measurement. The Overall Measurement Bias Report shows a histogram of the bias and a t test to see whether the average bias is equal to 0. You can see that the Average Bias is not zero, it is -0.0533. However, zero is contained within the confidence interval (-0.1152,0.0085), which means that the Average Bias is not significantly different from 0. Using a significance level of 0.05, you can see that the p-value is greater than 0.05, which also shows that the Average Bias is not significantly different from 0.

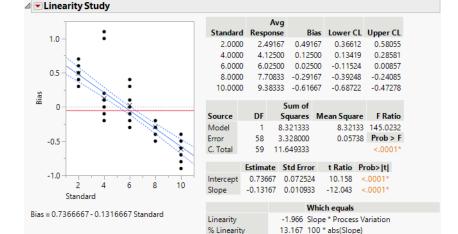
The Measurement Bias Report by Standard shows average bias values for each part. The bias averages are plotted on the graph along with the actual bias values for every part, so that you can see the spread. In this example, part number 1 (with a standard value of 2) is biased high and parts 4 and 5 (with standard values of 8 and 10) are biased low.

**Tip:** To see confidence intervals for the bias, right-click in the table and select **Columns > Lower 95% and Upper 95%**.

#### **Example of a Linearity Study**

Using the same data and scenario as the **Bias Report** option, you can now examine the linearity to determine whether there is a significant relationship between the size of the parts and the operator's ability to measure them.

- 1. Select **Help > Sample Data Library** and open Variability Data/MSALinearity.jmp.
- Select Analyze > Quality and Process > Variability / Attribute Gauge Chart.
- 3. Select Response and click Y, Response.
- 4. Select Standard and click **Standard**.
- Select Part and click X, Grouping.
- 6. Click **OK**.
- Click the Variability Gauge red triangle and select Gauge Studies > Linearity Study.
- 8. In the window that prompts you to Specify Process Variation, type 14.9286. The value 14.9286 is 6 times the standard deviation of the response, 2.488105.



Avg Bias

R-Squared Alpha

Process Variation

% Bias

**Figure 5.11** Linearity Study

#### Note the following:

• The slope is -0.131667. This value appears as part of the equation below the graph, and also in the third table.

0.714

0.050

-0.053 Bias averaged over all parts

14.929 Entered on dialog

0.357 100 \* abs(Avg Bias) / Process Variation

• The *p*-value associated with the test on the slope is quite small, <.0001. The *t* test for the slope is testing whether the bias changes with the standard value.

Because the *p*-value is small, you can conclude that there is a significant linear relationship between the size of the parts and the operator's ability to measure them. You can also see this in the graph. If the part or standard value is small, the bias is high, and vice versa.

## **Statistical Details for Variability Charts**

- "Statistical Details for Variance Components"
- "Statistical Details for the Discrimination Ratio"
- "Statistical Details for the Misclassification Probabilities"

#### **Statistical Details for Variance Components**

The exact model type that you choose depends on how the data was collected. For example, are the operators measuring the same parts (in which case you have a crossed design) or are they measuring different parts (in which case you have a nested design)? To illustrate, in a model where B is nested within A, multiple measurements are nested within both B and A, and there are  $na \bullet nb \bullet nw$  measurements, the following statements hold:

- na random effects are due to A
- na•nb random effects due to each nb B levels within A
- $na \cdot nb \cdot nw$  random effects due to each nw levels within B within A:

$$y_{ijk} = u + Za_i + Zb_{ij} + Zw_{ijk} .$$

The Zs are the random effects for each level of the classification. Each Z is assumed to have a mean of zero and to be independent from all other random terms. The variance of the response *y* is the sum of the variances due to each *z* component:

$$Var(y_{ijk}) = Var(Za_i) + Var(Zb_{ij}) + Var(Zw_{ijk})$$
.

Table 5.3 shows the supported models and what the effects in the model would be.

**Table 5.3** Models Supported by the Variability Charts Platform

Model	Factors	Effects in the Model
Main Effects	1	A
	2	A, B
	unlimited	and so on, for more factors

 Table 5.3 Models Supported by the Variability Charts Platform (Continued)

Model	Factors	Effects in the Model
Crossed	1	A
	2	A, B, A*B
	3	A, B, A*B, C, A*C, B*C, A*B*C
	4	A, B, A*B, C, A*C, B*C, A*B*C, D, A*D, B*D, A*B*D, C*D, A*C*D, B*C*D, A*B*C*D,
	unlimited	and so on, for more factors
Nested	1	A
	2	A, B(A)
	3	A, B(A), C(A,B)
	4	A, B(A), C(A,B), D(A,B,C)
	unlimited	and so on, for more factors
Crossed then Nested	3	A, B, A*B, C(A,B)
Nested then Crossed	3	A, B(A), C, A*C, C*B(A)

#### **Statistical Details for the Discrimination Ratio**

The discrimination ratio compares the total variance of the measurement, M, with the variance of the measurement error, E. The discrimination ratio is computed for all main effects, including nested main effects. The discrimination ratio, D, is computed as follows:

$$D = \sqrt{2\left(\frac{P}{T-P}\right) + 1}$$

where:

P = estimated variance for a factor

T = estimated total variance

#### Statistical Details for the Misclassification Probabilities

This section describes the computations for the probabilities in the Misclassification Probabilities report. The misclassification probabilities are based on the joint probability function of Y, the measured value of the part, and X, the true value of the part. The joint probability distribution function  $F_{YX}(y, x)$  uses a bivariate normal distribution with mean vector  $[\mu, \mu]$  and the following covariance matrix:

$$\begin{bmatrix} \gamma_P + \gamma_M & \gamma_P \\ \gamma_P & \gamma_P \end{bmatrix}$$

where  $\gamma_P$  is the part-to-part variation,  $\gamma_M$  is the measurement variation, and  $\mu$  is the grand mean. These quantities can be found or derived from quantities in the report window. Specifically,  $\gamma_P + \gamma_M$  is equal to the square of Total Variation (TV) divided by 6:  $(\text{TV}/6)^2$  and  $\gamma_P$  is equal to the square of Part Variation (PV) divided by 6:  $(\text{PV}/6)^2$ . The correlation  $\rho_{YX}$  between Y and X is defined as the square root of  $\gamma_P/(\gamma_P + \gamma_M)$ .

Next, define the following probabilities:

```
\delta = P[(LSL \leq X \leq USL) and (Y < LSL or Y > USL)]

\beta = P[(X < LSL or X > USL) and (LSL \leq Y \leq USL)]

\pi = P(LSL \leq X \leq USL)
```

These probabilities can be expressed in terms of the joint probability distribution function  $F_{YX}(y, x)$  and the marginal probability distribution functions for Y and X:  $F_{Y}(y)$  and  $F_{X}(x)$ :

```
\begin{split} \delta &= F_{YX}(\text{LSL, USL}) - F_{YX}(\text{LSL, LSL}) - F_{YX}(\text{USL, USL}) + F_{YX}(\text{USL, LSL}) + F_{X}(\text{USL}) - F_{X}(\text{LSL}) \\ \beta &= F_{YX}(\text{USL, LSL}) - F_{YX}(\text{LSL, LSL}) - F_{YX}(\text{USL, USL}) + F_{YX}(\text{LSL, USL}) + F_{Y}(\text{USL}) - F_{Y}(\text{LSL}) \\ \pi &= F_{X}(\text{USL}) - F_{X}(\text{LSL}) \\ P(\text{Good part is falsely rejected}) &= \delta/\pi \\ P(\text{Bad part is falsely accepted}) &= \beta/(1-\pi) \\ P(\text{Part is good and is rejected}) &= \delta \\ P(\text{Part is bad and is accepted}) &= \beta \\ P(\text{Part is good}) &= \pi \end{split}
```

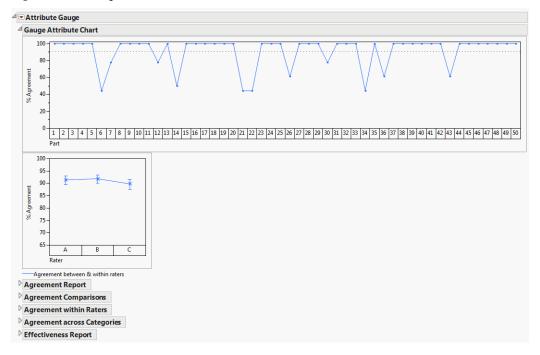
## **Attribute Gauge Charts**

#### **Evaluate a Categorical Measurement Process Using Agreement Measures**

Attribute charts analyze categorical measurements and can help show you measures of agreement across responses, such as raters. In *attribute data*, the variable of interest has a finite number of categories. Typically, data has only two possible results, such as pass or fail. You can examine aspects such as how effective raters were at classifying a part, how much they agreed with each other, and how much they agreed with themselves over the course of several ratings.

**Tip:** This chapter covers only attribute charts. For more information about variability charts, see "Variability Gauge Charts".

Figure 6.1 Example of an Attribute Chart



### **Contents**

Overview of Attribute Gauge Charts
Example of an Attribute Gauge Chart
Launch the Variability/Attribute Gauge Chart Platform
The Attribute Gauge Chart and Reports
Agreement Reports
Effectiveness Report
Attribute Gauge Platform Options
Statistical Details for Attribute Gauge Charts
Statistical Details for the Agreement Report

## **Overview of Attribute Gauge Charts**

Before you create an attribute gauge chart, your data should be formatted using the following guidelines:

- In order to compare agreement among raters, each rater in the data table must be in a separate column. These columns are then assigned to the **Y**, **Response** role in the launch window. In Figure 6.2, each rater (A, B, and C) is in a separate column.
- Responses in the different columns can be character (pass or fail) or numeric (0 or 1). In Figure 6.2, rater responses are numeric (0 for pass, 1 for fail). All response columns must have the same data type.
- Any other variables of interest that you might want to use as X, Grouping variables should
  appear stacked in one column each (see the Part column in Figure 6.2). You can also define
  a Standard column, which produces reports that compare raters with the standard. The
  Standard column and response columns must have the same data type.

Locked File C:\Progra Part Standard Code Α В C RefValue Attribute Chart 1 1 1 + 1 1 1 0.476901 2 1 1 + 0.476901 3 1 1 + 1 1 1 0.476901 Columns (7/0) 4 2 1 + 1 1 0.509015 5 2 1 0.509015 Part 6 2 1 0.509015 Standard 7 3 0 -0 0 0 0.576459 Code II, A 8 3 0 -0 0 0 0.576459 🔥 B 9 3 0 -0 0 0 0.576459 ıl. C 10 4 0 -0 0 0 0.566152 RefValue 0 -4 0 0.566152

**Figure 6.2** Attribute Gauge Data

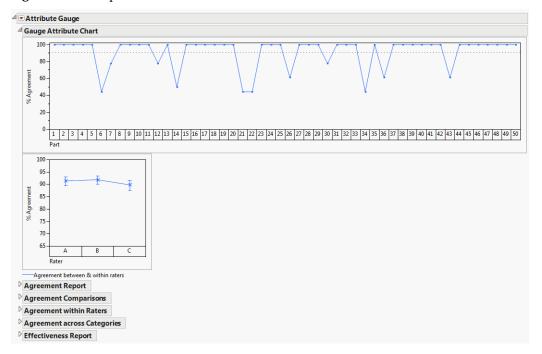
## **Example of an Attribute Gauge Chart**

Suppose that you have data containing pass or fail ratings for parts. Three raters, identified as A, B, and C, each noted a 0 (pass) or a 1 (fail) for 50 parts, three times each. You want to examine how effective the raters were in correctly classifying the parts, and how well the raters agreed with each other and with themselves over the course of the ratings.

- 1. Select **Help > Sample Data Library** and open Attribute Gauge.jmp.
- Select Analyze > Quality and Process > Variability / Attribute Gauge Chart.
- 3. For **Chart Type**, select **Attribute**.

- 4. Select A, B, and C and click **Y, Response**.
- 5. Select Standard and click **Standard**.
- 6. Select Part and click X, Grouping.
- 7. Click **OK**.

Figure 6.3 Example of an Attribute Chart



The first chart (Part) shows how well the raters agreed with each other for each part. For example, here you can see that the percent agreement dropped for part 6, 12, 14, 21, 22, and so on. These parts might have been more difficult to categorize.

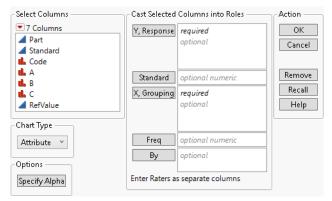
The second chart (Rater) shows each rater's agreement with him or herself and the other raters for a given part, summed up over all of the parts. In this example, it looks like the performance of the raters is relatively similar. Rater C had the lowest agreement, but the difference is not major (about 89% instead of 91%).

- 8. Open the Effectiveness Report and scroll down to the Conformance Report. You can see that 0 = non-conform (fail) and a 1 = conform (pass). However in this data, it is exactly the opposite: 0 is a pass and 1 is a fail. Reverse this setting.
- 9. Click the Conformance Report red triangle and select **Change Conforming Category**.

# Launch the Variability/Attribute Gauge Chart Platform

Launch the Variability/Attribute Gauge Chart platform by selecting **Analyze > Quality and Process > Variability/Attribute Gauge Chart**. Set the **Chart Type** to **Attribute**.

Figure 6.4 The Variability/Attribute Gauge Chart Launch Window



For more information about the options in the Select Columns red triangle menu, see *Using IMP*.

**Chart Type** Choose between a variability gauge analysis (for a continuous response) or an attribute gauge analysis (for a categorical response, usually "pass" or "fail").

**Note:** The content in this chapter covers only the **Attribute** chart type. For more information about the **Variability** chart type, see "Variability Gauge Charts".

**Specify Alpha** Specify the alpha level used by the platform.

- **Y, Response** Specify the columns of ratings given by each rater. You must specify more than one rating column.
- **Standard** Specify a standard or reference column that contains the "true" or known values for the part. In the report window, an Effectiveness Report and an additional section in the Agreement Comparisons report appear, which compare the raters with the standard.
- **X, Grouping** Specify the classification columns that group the measurements. If the factors form a nested hierarchy, specify the higher terms first.
- **Freq** Identifies the data table column whose values assign a frequency to each row. Can be useful when you have summarized data.

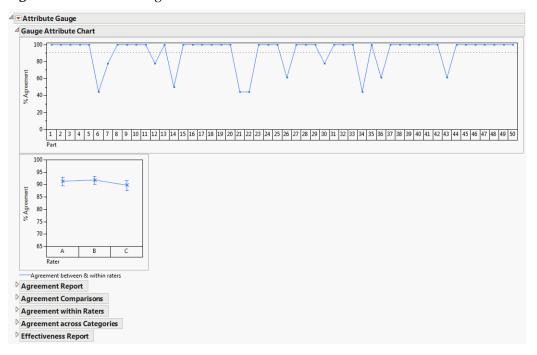
**By** Identifies a column that creates a report consisting of separate analyses for each level of the variable.

# The Attribute Gauge Chart and Reports

Attribute gauge chart plots the percent Agreement, which is a measurement of rater agreement for every part in the study. The agreement for each part is calculated by comparing the ratings for every pair of raters for all ratings of that part. See "Statistical Details for Attribute Gauge Charts".

Follow the instructions in "Example of an Attribute Gauge Chart" to produce the results shown in Figure 6.5.

Figure 6.5 Attribute Gauge Chart



The first chart in Figure 6.5 uses all X grouping variables (in this case, the Part) on the x-axis. The second chart uses all Y variables on the x-axis (typically, and in this case, the Rater).

In the first graph, you can look for parts with a low percent Agreement value, and
investigate to determine why raters do not agree about the measurement of that particular
part.

The Attribute Gauge Chart and Reports

In the second graph, you can look for raters with a low percent Agreement value, and
investigate to determine why they do not agree with the other raters or with themselves.

For information about additional options, see "Attribute Gauge Platform Options".

## **Agreement Reports**

**Note:** The Kappa value is a statistic that expresses agreement. The closer the Kappa value is to 1, the more agreement there is. A Kappa value closer to 0 indicates less agreement.

The Agreement Report shows agreement summarized for each rater and overall agreement. This report is a numeric form of the data presented in the second chart in the Attribute Gauge Chart report (Figure 6.5).

The Agreement Comparisons report shows each rater compared with all other raters, using Kappa statistics. The rater is compared with the standard only if you have specified a Standard variable in the launch window.

The Agreement within Raters report shows the number of items that were inspected. The confidence intervals are score confidence intervals, as suggested by Agresti and Coull (1998). The Number Matched is the sum of the number of items inspected, where the rater agreed with him or herself on each inspection of an individual item. The Rater Score is the Number Matched divided by the Number Inspected.

The Agreement across Categories report shows the agreement in classification over that which would be expected by chance. It assesses the agreement between a fixed number of raters when classifying items.

Figure 6.6 Agreement Reports

△ Agreement Report 95% Rater % Agreement Lower CI Upper CI Α 91.4286 89.5082 93.0248 В 91.9048 90.0502 C 89.8095 87.6057 91.6588 95% Number Number 95% Inspected Matched % Agreement Lower CI Upper CI 50 39 78.000 64.758 87.246 Agreement Comparisons Compared Standard Rater with Rater Kappa Error В 0.8629 0.0442 0.0547 Α C 0.7761 В C 0.7880 0.0537 Compared Standard Rater with Standard Kappa Δ Standard 0.8788 0.0416 В Standard 0.9230 0.0338 Standard 0.7740 0.0551 Agreement within Raters Number Number 95% Rater Inspected Matched Rater Score Lower CI Upper CI 50 42 Α 84.0000 71.4858 91.6626 В 50 45 90.0000 78.6398 95.6524 50 C 40 80.0000 66.9629 88.7562

.6 .8

## **Effectiveness Report**

0

1

Overall

△ Agreement across Categories

Kappa

0.7936

0.7936

0.7936

The Effectiveness Report appears only if you have specified a Standard variable in the launch window. For a description of a Standard variable, see "Launch the Variability/Attribute Gauge Chart Platform". This report compares every rater with the standard.

Standard

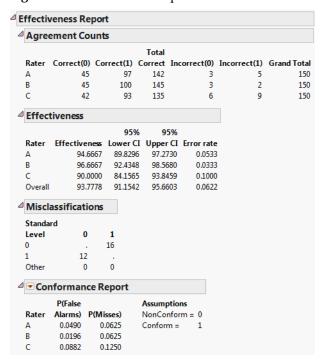
Error

0.0236

0.0236

0.0236

Figure 6.7 Effectiveness Report



The Agreement Counts table shows cell counts on the number correct and incorrect for every level of the standard. In Figure 6.7, the standard variable has two levels, 0 and 1. Rater A had 45 correct responses and 3 incorrect responses for level 0, and 97 correct responses and 5 incorrect responses for level 1.

Effectiveness is defined as the number of correct decisions divided by the total number of opportunities for a decision. For example, say that rater A sampled every part three times. On the sixth part, one of the decisions did not agree (for example, pass, pass, fail). The other two decisions would still be counted as correct decisions. This definition of effectiveness is different from the MSA 3<sup>rd</sup> edition. According to MSA, all three opportunities for rater A on part six would be counted as incorrect. Including all of the inspections separately gives you more information about the overall inspection process.

In the Effectiveness table, 95% confidence intervals are given about the effectiveness. These are score confidence intervals. It has been demonstrated that score confidence intervals provide increased coverage probability, particularly where observations lie near the boundaries. See Agresti and Coull (1998).

The Misclassifications table shows the incorrect labeling. The rows represent the levels of the standard or accepted reference value. The columns contain the levels given by the raters.

#### **Conformance Report**

The Conformance Report shows the probability of false alarms and the probability of misses. The Conformance Report appears only when the rating has two levels (such as pass or fail, or 0 or 1).

The following descriptions apply:

**False Alarm** The part is determined to be non-conforming, when it actually is conforming.

**Miss** The part is determined to be conforming, when it actually is not conforming.

**P(False Alarms)** The number of parts that have been incorrectly judged to be nonconforming divided by the total number of parts that are judged to be conforming.

**P(Miss)** The number of parts that have been incorrectly judged to be conforming divided by the total number of parts that are actually nonconforming.

The Conformance Report red triangle menu contains the following options:

**Change Conforming Category** Reverses the response category that is considered conforming.

**Calculate Escape Rate** Calculates the Escape Rate, which is the probability that a non-conforming part is produced and not detected. The Escape Rate is calculated as the probability that the process will produce a non-conforming part times the probability of a miss. You specify the probability that the process will produce a non-conforming part, also called the Probability of Nonconformance.

**Note:** Missing values are treated as a separate category in this platform. To avoid this separate category, exclude rows of missing values in the data table.

# **Attribute Gauge Platform Options**

The Attribute Gauge red triangle menu contains the following options:

**Attribute Gauge Charts** Shows or hides the gauge attribute chart and the efficiency chart.

**Show Agreement Points** Shows or hides the agreement points on the charts.

**Connect Agreement Points** Connects the agreement points in the charts.

**Agreement by Rater Confid Intervals** Shows or hides the agreement by rater confidence intervals on the efficiency chart.

- **Show Agreement Group Means** Shows or hides the agreement group means on the gauge attribute chart. This option is available when you specify more than one X, Grouping variable.
- **Show Agreement Grand Mean** Shows or hides the overall agreement mean on the gauge attribute chart.
- **Show Effectiveness Points** Shows or hides the effectiveness points on the charts.
- **Connect Effectiveness Points** Draws lines between the effectiveness points in the charts.
- **Effectiveness by Rater Confid Intervals** Shows or hides confidence intervals on the second chart in the Attribute Gauge Chart report (Figure 6.5).
- **Effectiveness Report** Shows or hides the Effectiveness report. This report compares every rater with the standard, using the Kappa statistic.
- See *Using JMP* for more information about the following options:
- **Local Data Filter** Shows or hides the local data filter that enables you to filter the data used in a specific report.
- **Redo** Contains options that enable you to repeat or relaunch the analysis. In platforms that support the feature, the Automatic Recalc option immediately reflects the changes that you make to the data table in the corresponding report window.
- **Save Script** Contains options that enable you to save a script that reproduces the report to several destinations.
- **Save By-Group Script** Contains options that enable you to save a script that reproduces the platform report for all levels of a By variable to several destinations. Available only when a By variable is specified in the launch window.

# **Statistical Details for Attribute Gauge Charts**

For the first chart in Figure 6.5 that plots all **X**, **Grouping** variables on the x-axis, the percent Agreement is calculated as follows:

% Agreement for part 
$$i = \frac{\sum\limits_{l=1}^{K} \left(\text{number of responses for level } l\right)}{\binom{N_i}{2}}$$

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For the second chart in Figure 6.5 that plots all **Y**, **Response** variables on the *x*-axis, the percent Agreement is calculated as follows:

% Agreement for rater 
$$k = \frac{\displaystyle\sum_{i=1}^{n} \left(\displaystyle\sum_{j=1}^{r_i} \text{ number of uncounted matching levels}\right)}{\displaystyle\sum_{i=1}^{n} \left(\displaystyle\sum_{j=1}^{r_i} N_i - j\right)}$$

Note the following:

- *n* = number of parts (grouping variables)
- $r_i$  = number of reps for part i (i = 1,...,n)
- m = number of raters
- k = number of levels
- $N_i = m \times r_i$ . Number of ratings on part i (i = 1,...,n). This includes responses for all raters, and repeat ratings on a part. For example, if part i is measured 3 times by each of 3 raters, then  $N_i$  is  $3 \times 3 = 9$ .

For example, consider the following table of data for three raters, each having three replicates for one part.

**Table 6.1** Three Replicates for Raters A, B, and C

	Α	В	С
1	1	1	1
2	1	1	0
3	0	0	0

Using this table, you can make these calculations:

% Agreement = 
$$\frac{\binom{4}{2} + \binom{5}{2}}{\binom{9}{2}} = \frac{16}{36} = 0.444$$

% Agreement [rater A] = percent Agreement [rater B] = 
$$\frac{4+3+3}{8+7+6} = \frac{10}{21} = 0.476$$
 and

Statistical Details for Attribute Gauge Charts

% Agreement [rater C] = 
$$\frac{4+3+2}{8+7+6} = \frac{9}{21} = 0.4286$$

## Statistical Details for the Agreement Report

The simple Kappa coefficient is a measure of inter-rater agreement.

$$\hat{\kappa} = \frac{P_0 - P_e}{1 - P_e}$$

where:

$$P_0 = \sum_{i} p_{ii}$$

and:

$$P_e = \sum_{i} p_{i.} p_{.i}$$

If you view the two response variables as two independent ratings of the *n* parts, the Kappa coefficient equals +1 when there is complete agreement of the raters. When the observed agreement exceeds chance agreement, the Kappa coefficient is positive, and its magnitude reflects the strength of agreement. Although unusual in practice, Kappa is negative when the observed agreement is less than the chance agreement. The minimum value of Kappa is between -1 and 0, depending on the marginal proportions.

Estimate the asymptotic variance of the simple Kappa coefficient with the following equation:

$$var = \frac{A + B - C}{(1 - P_{\rho})^2 n}$$

where:

$$A = \sum_{i} p_{ii} \left[ 1 - (p_{i.} + p_{.i})(1 - \hat{\kappa}) \right]$$

$$B = (1 - \hat{\kappa})^2 \sum_{i \neq j} \sum_{j} p_{ij} (p_{.i} + p_{j.})^2$$

and:

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$$C = \left[\hat{\kappa} - P_e(1 - \hat{\kappa})\right]^2$$

The Kappas are plotted and the standard errors are also given.

**Note:** The Kappa statistics in the Attribute Chart platform are shown even when the levels of the variables are unbalanced.

Categorical Kappa statistics (Fleiss 1981) are found in the Agreement Across Categories report.

Given the following assumptions:

- n = number of parts (grouping variables)
- m = number of raters
- k = number of levels
- $r_i$  = number of reps for part i (i = 1,...,n)
- $N_i = m \times r_i$ . Number of ratings on part i (i = 1, 2,...,n). This includes responses for all raters, and repeat ratings on a part. For example, if part i is measured 3 times by each of 2 raters, then  $N_i$  is  $3 \times 2 = 6$ .
- $x_{ij}$  = number of ratings on part i (i = 1, 2,...,n) into level j (j = 1, 2,...,k)

The individual category Kappa is defined as follows:

$$\hat{\kappa_j} = 1 - \frac{\sum\limits_{i=1}^{n} x_{ij}(N_i - x_{ij})}{\sum\limits_{i=1}^{n} N_i(N_i - 1)} \qquad \text{where} \qquad \frac{\sum\limits_{j=1}^{n} x_{ij}}{\sum\limits_{i=1}^{n} N_i} \qquad \bar{q}_j = 1 - \bar{p}_j$$

The overall Kappa is defined as follows:

$$\hat{\bar{\kappa}} = \frac{\sum_{j=1}^{k} \bar{q}_{j} \bar{p}_{j} \hat{\kappa}_{j}}{\sum_{j=1}^{k} \bar{p}_{j} \bar{q}_{j}}$$

The variance of  $\hat{\kappa}_i$  and  $\hat{\kappa}$  are calculated as follows:

$$\operatorname{var}(\hat{\kappa}_j) = \frac{2}{nN(N-1)}$$

$$\operatorname{var}(\hat{\kappa}) = \frac{2}{\left(\sum_{j=1}^{k} \bar{p}_{j} \bar{q}_{j}\right)^{2} nN(N-1)} \times \left[\left(\sum_{j=1}^{k} \bar{p}_{j} \bar{q}_{j}\right)^{2} - \sum_{j=1}^{k} \bar{p}_{j} \bar{q}_{j} (\bar{q}_{j} - \bar{p}_{j})\right]$$

The standard errors of  $\hat{\kappa}_j$  and  $\hat{\kappa}_j$  are shown only when there are an equal number of ratings per part (for example,  $N_i = N$  for all i = 1,...,n).

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Chapter 6 Quality and Process Methods

# **Process Capability**

#### Measure the Variability of a Process over Time

Process capability analysis, used in process control, measures how well a process is performing compared to given specification limits. A good process is one that is stable and consistently produces product that is well within specification limits. A capability index is a measure that relates process performance, summarized by process centering and variability, to specification limits.

Graphical tools such as a goal plot and box plots give you quick visual ways of identifying which process or product characteristics are within specifications. Individual detail reports display a capability report for each variable in the analysis. The analysis enables you to identify variation relative to the specifications or requirements; this enables you to achieve increasingly higher conformance values.

You can specify subgroups to compare the overall variation of the process to the within subgroup variation. You can compute capability indices for processes that produce measurements that follow various distributions. For data that follow none of the specified distributions, you can compute nonparametric capability indices.

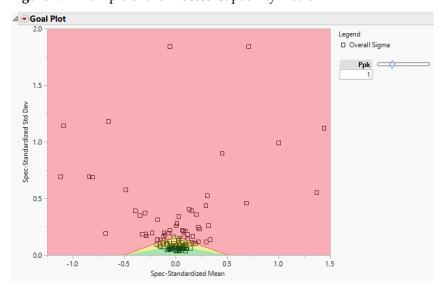


Figure 7.1 Example of the Process Capability Platform

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## Overview of the Process Capability Platform

The Process Capability platform provides the tools needed to measure the compliance of a process to given specifications. By default, JMP shows a Goal Plot, Capability Box Plots, and a Capability Index Plot for the variables that you fit with normal distributions. Capability indices for nonnormal variables are plotted on the Capability Index Plot. You can add normalized box plots, summary reports, and individual detail reports for the variables in your analysis.

You can supply specification limits in several ways:

- in the data table, using a column property
- by requesting the Spec Limits Dialog in the launch window
- by loading the limits from a specification limits data table
- using the Manage Spec Limits utility (Analyze > Quality and Process > Manage Spec Limits)

You can specify two-sided, one-sided, or asymmetric specification limits.

**Note:** The Process Capability platform expands significantly on the Capability analyses that are available through Analyze > Distribution and through Analyze > Quality and Process > Control Chart.

#### **Capability Indices**

A capability index is a ratio that relates the ability of a process to produce product that meets specification limits. The index relates estimates of the mean and standard deviation of the quality characteristic to the specification limits. Within estimates of capability are based on an estimate of the standard deviation constructed from within-subgroup variation. Overall estimates of capability use an estimate of standard deviation constructed from all of the process data. See "Capability Indices for Normal Distributions" and "Variation Statistics".

Estimates of the mean or standard deviation are well-defined only if the processes related to centering or spread are *stable*. Therefore, interpretation of within capability indices requires that process spread is stable. Interpretation of overall capability indices requires that both process centering and spread are stable.

Capability indices constructed from small samples can be highly variable. The Process Capability platform provides confidence intervals for most capability indices. Use these to determine the range of potential values for your quality characteristic's actual capability.

**Note:** When confidence intervals are not provided (for example, for nonnormal distributions) you can use the Simulate feature to construct confidence intervals. For an example, see "Simulation of Confidence Limits for a Nonnormal Process Ppk".

Guidelines for values of capability indices can be found in Montgomery (2013). The minimum recommended value is 1.33. Six Sigma initiatives aim for much higher capability levels that correspond to extremely low rates of defective parts per million.

#### **Capability Indices for Nonnormal Processes**

The Process Capability platform constructs capability indices for process measurements with the following distributions: Normal, Beta, Exponential, Gamma, Johnson, Lognormal, Mixture of 2 Normals, Mixture of 3 Normals, SHASH, and Weibull. A Best Fit option determines the best fit among these distributions and provides capability indices for this fit. The platform also provides a Nonparametric fit option that gives nonparametric estimates of capability.

For the nonnormal methods, estimates are constructed using two approaches: the ISO/Quantile method (Percentiles) and the Bothe/Z-scores method (Z-Score). For more information about these methods, see "Capability Indices for Nonnormal Distributions: Percentile and Z-Score Methods".

**Note:** Process Capability analysis for individual responses is accessible through Analyze > Quality and Process > Control Chart Builder. However, nonnormal distributions are available only in the Process Capability platform.

#### Overall and Within Estimates of Sigma

Most capability indices in the Process Capability platform can be computed based on estimates of the *overall* (long-term) variation and the *within*-subgroup (short-term) variation. If the process is stable, these two measures of variation should yield similar results since the overall and within subgroup variation should be similar. The normalized box plots and summary tables can be calculated using either the overall or the within-subgroup variation. See "Additional Examples of the Process Capability Platform" for examples of capability indices computed for stable and unstable processes.

You can specify subgroups for estimating within-subgroup variation in the launch window. You can specify a column that defines subgroups or you can select a constant subgroup size. For each of these methods, you can choose to estimate the process variation using the average of the unbiased standard deviations or using the average of the ranges. If you do not specify subgroups, the Process Capability platform constructs a within-subgroup estimate of the process variation using a moving range of subgroups of size two. Finally, you can specify a historical sigma to be used as an estimate of the process standard deviation.

Process Capability

#### **Capability Index Notation**

The Process Capability platform provides two sets of capability indices. See "Capability Indices for Normal Distributions" for more information about the calculation of the capability indices.

- Cpk, Cpl, Cpu, Cp, and Cpm. These indices are based on a within-subgroup (short-term) estimate of the process standard deviation.
- Ppk, Ppl, Ppu, Pp, and Cpm. These indices are based on an overall (long-term) estimate of
  the process standard deviation. Note that the process standard deviation does not exist if
  the process is not stable. See Montgomery (2013).

The Process Capability platform uses the appropriate AIAG notation for capability indices: Ppk labeling denotes an index constructed from an overall variation estimate and Cpk denotes an index constructed from a within-subgroup variation estimate.

**Note:** The AIAG (Ppk) Labeling platform preference is selected by default. You can change the reporting to use Cp notation only by deselecting this preference under Process Capability.

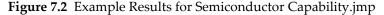
For more information about process capability analysis, see Montgomery (2013) and Wheeler (2004).

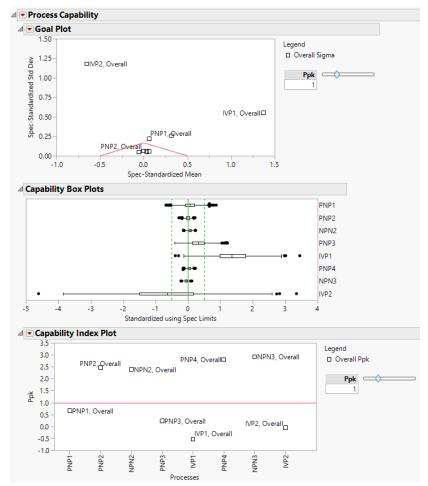
# Example of the Process Capability Platform with Normal Variables

This example uses the Semiconductor Capability.jmp sample data table. The variables represent standard measurements that a semiconductor manufacturer might make on a wafer as it is being processed. Specification limits for the variables have been entered in the data table through the Column Properties > Spec Limits property.

- 1. Select **Help > Sample Data Library** and open Semiconductor Capability.jmp.
- 2. Select Analyze > Quality and Process > Process Capability.
- 3. Click the white triangle next to Processes to view all of the continuous variables.
- 4. Select PNP1, PNP2, NPN2, PNP3, IVP1, PNP4, NPN3, and IVP2, and click Y, Process.
- 5. Click **OK**.
- 6. Click the Goal Plot red triangle and select **Label Overall Sigma Points**.
- 7. Click the Capability Index Plot red triangle and select **Label Overall Sigma Points**.

Example of the Process Capability Platform with Normal Variables





The Goal Plot shows the spec-normalized mean shift on the *x*-axis and the spec-normalized standard deviation on the *y*-axis for each variable. The triangular region defined by the red lines in the bottom center of the plot is the goal triangle. It defines a region of capability index values. You can adjust the goal triangle using the Ppk slider to the right of the plot. When the slider is set to 1, note that PNP1, PNP3, IVP1, and IVP2 are outside of the goal triangle and possibly out of specification.

The Capability Box Plots report shows a box plot for each variable in the analysis. The values for each column are centered by their target value and scaled by the specification range. In this example, all process variables have both upper and lower specification limits, and these are symmetric about the target value. It follows that the solid green line shows where the target should be and the dashed lines represent the specification limits.

It appears that the majority of points for IVP1 are above its upper specification limit (USL), and the majority of points for IVP2 are less than its target. PNP2 seems to be on target with all data values inside the specification limits.

The Capability Index Plot plots the Ppk values for each variable. Four variables come from very capable processes, with Ppk values of 2 or more. Four variables have Ppk values below 1.

# **Example of the Process Capability Platform with Nonnormal Variables**

The Process Measurements.jmp data table contains measurements made on seven different processes used to construct a product. For each process, specification limits are saved as column properties. You begin by examining the distributions of your process data. You see that the distributions are not normal. Then you use the nonnormal capability features of the Process Capability platform to compute capability indices.

#### View the Distributions

- Select Help > Sample Data Library and open Process Measurements.jmp.
- Select Analyze > Distribution.
- 3. Select all seven columns from the **Select Columns** list and click **Y, Columns**.
- Check the box next to Histograms Only.
- Click **OK**.

For most processes, the histograms show evidence that the theoretical distribution of measurements is skewed and does not follow a normal distribution. Therefore, for each process, you find the best fitting distributions among all of the available parametric distributions.

#### Perform a Capability Analysis

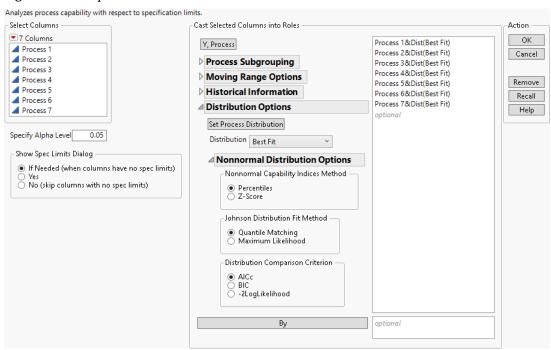
- Select Analyze > Quality and Process > Process Capability.
- Select all seven columns from the Columns list and click Y, Process.
- 3. Select all seven columns in the **Y, Process** list.
- Open the Distribution Options panel and select Best Fit from the Distribution list.
- Click Set Process Distribution.

The suffix &Dist(Best Fit) is added to each variable name in the Y, Process list. The Best Fit option specifies that the best-fitting parametric distribution should be fit to each variable. The available parametric distributions are Normal, Beta, Exponential, Gamma, Johnson,

Lognormal, Mixture of 2 Normals, Mixture of 3 Normals, SHASH, and Weibull (Figure 7.3).

Open the Nonnormal Distribution Options outline. Note that the Nonnormal Capability
Indices Method is set to Percentiles, the Johnson Distribution Fitting Method is set to
Quantile Matching, and the Distribution Comparison Criterion is set to AICc.

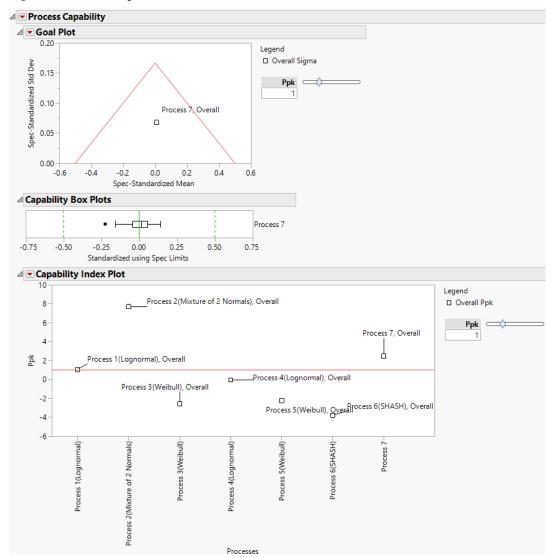
Figure 7.3 Completed Launch Window



The Quantile Matching method is the default method used for fitting Johnson distributions because of its stability and speed as compared to Maximum Likelihood. Note that Maximum Likelihood is used in the Distribution platform.

- 7. Click **OK**.
- 8. Click the Goal Plot red triangle and select **Label Overall Sigma Points**.
- 9. Click the Capability Index Plot red triangle and select **Label Overall Sigma Points**.

Figure 7.4 Initial Report with Variables Labeled



**Note:** Click a label in the plot and drag it to make the plot more interpretable. Click the right side frame of the Capability Index Plot and drag it to the right to make the labels easier to distinguish.

The Goal Plot shows only one point and it corresponds to Process 7. The Capability Box Plots report shows a single box plot for Process 7. This is because the best fit for Process 7 is a normal distribution.

10. To the right of the Capability Index Plot, set the Ppk value to 2.

Example of the Process Capability Platform with Nonnormal Variables

The Capability Index Plot shows Ppk values for all seven processes. Only two processes, Process 2 and Process 7, have capability values that exceed 2. Note that the best fitting nonnormal distributions are shown in parentheses to the right of the variable names in the Capability Index Plot. The best fitting distribution for Process 7 is not shown because it is a normal distribution.

- 11. Click the Process Capability red triangle and select **Individual Detail Reports**.

  Because you requested Best Fit in the launch window, the Compare Distributions option has been selected from each distribution's red triangle menu.
- 12. Scroll to the report entitled **Process 4(Lognormal) Capability**.

Figure 7.5 Individual Detail Report for Process 4

Distribution Selected 

Histogram - Compare Distributions ✓ Normal Density Beta USL Normal ✓ Exponential **✓** Gamma Exponential Gamma ✓ Johnson Johnson Su ✓ Lognormal LogNormal Mixture of 2 Normals Mixture of 2 Normals ✓ Mixture of 3 Normals ○ Mixture of 3 Normals ✓ SHASH SHASH ✓ Weibull Weibull Nonparametric 20 25 Process 4 △ Comparison Details Distribution AICc BIC -2Loglikelihood LogNormal 496.16461 501.25124 492.0409 492.39731 SHASH 500.81837 510.81799 Gamma 506.77272 511.85935 502.64901 Exponential 507.48585 510.05021 505.44504 508.71393 513.80056 Weibull 504.59022 Johnson Su 509.02745 519.02708 500.6064 Mixture of 3 Normals 512.25109 531.51003 494.66867 Mixture of 2 Normals 518.1443 530.53185 507.506 603.94892 609.03555 599.82521 LSL 3 Density LSL Target USL Target 10 --- Overall USL 25 100 N Sample Mean 4.60538 Sample Std Dev 4.880206 0 5 10 15 20 25 Process 4 △ Overall Sigma Capability △ Parameter Estimates Index Estimate Parameter Estimate μ 1.0743138 Ppk -0.026 Scale Ppl -0.026 Shape σ 0.9674923 0.438 Ppu Pp 0.414 0.220 △ Nonconformance Expected Portion Observed % Overall % Below LSL 50.0000 51.0018 Above USL 0.0000 1.3325 Total Outside 50.0000

The title of the report for Process 4 indicates that the capability calculations are based on a lognormal fit. All of the check boxes in the Compare Distributions report, except the boxes

Example of the Process Capability Platform with Nonnormal Variables

for Nonparametric and Beta, are checked, indicating that these nine distributions are fit. (This is because you requested a Best Fit in the launch window.) The button that is selected in the Selected column indicates that the Lognormal distribution is the distribution that is used in the remainder of the Process 4(Lognormal) Capability report to estimate capability and nonconformance.

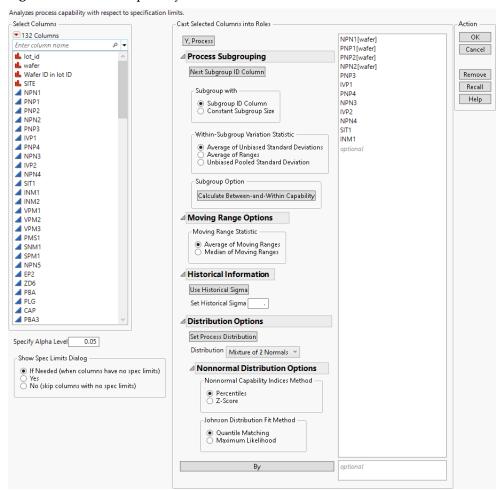
The Compare Distributions report enables you to compare the nine distributional fits. The Histogram - Compare Distributions report gives a visual assessment of the fit and the Comparison Details report shows fit statistics for the selected distributions. Both the plot and the fit statistics indicate that the lognormal distribution gives the best fit among the selected distributions.

The Individual Detail Report information that is shown by default includes a histogram showing the estimated best-fit distribution, a summary of the process information, capability indices based on an overall estimate of sigma, parameter estimates for the fitted lognormal distribution, and observed and expected nonconformance levels.

# **Launch the Process Capability Platform**

Launch the Process Capability Platform by selecting Analyze > Quality and Process > Process Capability. In Figure 7.6, which uses the Semiconductor Capability.jmp data table, all outlines and panels have been opened.

Figure 7.6 Process Capability Launch Window



For more information about the options in the Select Columns red triangle menu, see *Using JMP*.

The Process Capability launch window contains the following outlines and options:

- "Process Selection"
- "Process Subgrouping"

Launch the Process Capability Platform

- "Moving Range Options"
- "Historical Information"
- "Distribution Options"
- "Other Specifications"

After you click OK in the launch window, the Spec Limits window appears unless one of the following occurs:

- All of the columns contain specification limits.
- You selected **No (skip columns with no spec limits)** on the launch window.

The Spec Limits window also appears if you select Yes on the launch window. Otherwise, the Process Capability report window appears.

#### **Process Selection**

Select the process variables to include in the capability analysis.

**Y, Process** Assigns the variables that you want to analyze.

#### Notes:

- The Transform menu is not available for the Select Column list in the Process Capability launch window. Right-click a column heading in the data table and select **New Formula Column** to create a transform column for use in Process Capability. See *Using JMP* for more information about creating new formula columns.
- Reference columns for virtually joined tables are not available in the Process Capability platform.

# **Process Subgrouping**

This group of options enables you to assign each variable in the Y, Process list a subgroup ID column or a constant subgroup size.

## Create Subgroups Using an ID Column

- 1. Select a variable or variables in the Y, Process list.
- 2. Select **Subgroup ID Column** from the **Subgroup with** options.
- 3. Select a subgroup ID column in the Select Columns list.
- 4. Click Nest Subgroup ID Column.

The subgroup ID column appears in brackets to the right of the variable names in the Y, Process list.

**Process Capability** 

#### Create Subgroups Using a Constant Subgroup Size

- 1. Select a variable or variables in the Y, Process list.
- 2. Select **Constant Subgroup Size** from the **Subgroup with** options.
- 3. Enter the subgroup size next to **Set Constant Subgroup Size**.
- 4. Click Subgroup by Size.

The subgroup size appears in brackets to the right of the variable names in the Y, Process list.

- **Nest Subgroup ID Column** (Available when you select Subgroup ID Column.) Assigns a column that you select from the Select Columns list to define the subgroups for the selected Y, Process columns.
- **Subgroup by Size** (Available when you select Constant Subgroup Size.) Assigns the subgroup size that you specify in the Set Constant Subgroup Size box to define the subgroups for the selected Y, Process columns.
- **Set Constant Subgroup Size** (Available when you select Constant Subgroup Size.) Specify the constant subgroup size for the selected Y, Process columns. You need to assign this value using Subgroup by Size.
- **Within-Subgroup Variation Statistic** (Available when Process Subgrouping is used.) Specifies if the within-subgroup estimate of standard deviation is calculated using standard deviations or ranges.
- **Calculate Between-and-Within Capability** (Available when Process Subgrouping is used.) Specifies that the between-and-within subgroup estimate of the standard deviation should be used in the capability analysis.

# **Moving Range Options**

Use this outline to specify which moving range statistic is used in the within sigma estimate when subgrouping is not used.

**Note:** When you specify subgrouping and click **Calculate Between-and-Within Capability**, use the Moving Range Options outline to specify which moving range statistic is used in the between sigma estimate.

**Average of Moving Range** Uses the mean of the moving ranges to estimate sigma. The moving range is the difference between two consecutive points.

**Median of Moving Range** Uses the median of the moving ranges to estimate sigma.

Launch the Process Capability Platform

#### **Historical Information**

Use this outline to assign historically accepted values of the standard deviation to variables in the Y, Process list.

- 1. Select a variable or variables in the Y, Process list.
- 2. Enter a value next to Set Historical Sigma.
- 3. Select Use Historical Sigma to assign that value to the selected variables.

The specified value appears in parentheses in the expression "&Sigma()" to the right of the variable names in the Y, Process list.

**Note:** If you set a historical sigma, then subgroup assignments for the selected process variable are no longer relevant and are removed.

# **Distribution Options**

Unless otherwise specified, all Y, Process variables are analyzed using the assumption that they follow a normal distribution. Use the Distribution Options outline to assign other distributions or calculation methods to variables in the Y, Process list and to specify options related to nonnormal calculations.

- The available distributions are the Normal, Beta, Exponential, Gamma, Johnson,
  Lognormal, Mixture of 2 Normals, Mixture of 3 Normals, SHASH, and Weibull
  distributions. Except for Johnson distributions, maximum likelihood estimation is used to
  fit distributions. See "Johnson Distribution Fit Method".
- The Best Fit option determines the best fit among the available distributions and applies this fit.
- The Nonparametric option fits a distribution using kernel density estimation.

For more options related to nonnormal fits, see "Nonnormal Distribution Options".

#### Specify a Distribution

- 1. Select a variable or variables in the Y, Process list.
- 2. Select a distribution from the Distribution list.
- 3. Select Set Process Distribution to assign that distribution to the selected variables.

The specified distribution appears in parentheses in the expression "&Dist()" to the right of the variable names in the Y, Process list.

**Note:** If you select a distribution other than Normal, you cannot assign a Subgroup ID column or a Historical Sigma. These selections are not supported by the methods used to calculate nonnormal capability indices. See "Capability Indices for Nonnormal Distributions: Percentile and Z-Score Methods".

#### **Nonnormal Distribution Options**

- **Nonnormal Capability Indices Method** Specifies the method used to compute capability indices for nonnormal distributions. See "Capability Indices for Nonnormal Distributions: Percentile and Z-Score Methods".
- **Johnson Distribution Fit Method** Specifies the method used to find the best-fitting Johnson distribution. Before estimating the parameters, the best-fitting family of distributions is determined from among the Johnson Su, Sb, and Sl families. The procedure described in Slifker and Shapiro (1980) is used to find the best-fitting family.
  - **Quantile Matching** The default method. It is more stable and faster than Maximum Likelihood. Quantile Matching Parameter estimates, assuming the best-fitting family, are obtained using a quantile-matching approach. See Slifker and Shapiro (1980).
  - **Maximum Likelihood** Parameters for the best-fitting family are determined using maximum likelihood.
- **Distribution Comparison Criterion** (Available when a Best Fit Distribution is selected.) Specify the criterion that you want to use in determining a Best Fit. This criterion also determines the ordering of distributions in the Comparison Details report. See "Order by Comparison Criterion".

## **Other Specifications**

- **By** Produces a separate report for each level of the By variable. If more than one By variable is assigned, a separate report is produced for each possible combination of the levels of the By variables.
- **Specify Alpha Level** Specifies the significance level for confidence limits.
- **Show Spec Limits Dialog** Specifies how to handle columns that do not have specification limits.

Chapter 7
Quality and Process Methods

**Note:** It is good practice to ensure that specification limits for all process variables are specified as Spec Limits column properties or to load specification limits from a Limits Data table (see "Limits Data Table"). Otherwise, you can specify limits interactively in the Spec Limits window that appears after you click OK in the launch window (unless you select **No (skip columns with no spec limits)** on the launch window).

# **Entering Specification Limits**

The lower specification limit (LSL), upper specification limit (USL), and target define the lower bound, upper bound, and target value for a quality process.

There are several ways to enter specification limits:

- Enter limits in the Spec Limits window after selecting columns in the launch window. See "Spec Limits Window".
- Import limits from a JMP data table (known as a Limits Table). See "Limits Data Table".
- Enter limits as Spec Limits column properties in the data table. See "Spec Limits Column Property".
- If you are creating a Process Capability report by running a JSL script, enter limits in the script. See "The Process Capability Report".

Only one specification limit is required for a selected column. If only the USL is specified, the box plots and Goal Plot point are colored blue. If only the LSL is specified, the box plots and Goal Plot point are colored red.

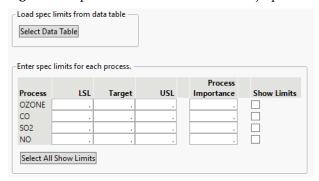
# **Spec Limits Window**

After you click OK on the launch window, the Spec Limits window appears if any of the columns do not contain limits and you did not select **No (skip columns with no spec limits)** on the launch window. The Spec Limits window also appears if you select Yes on the launch window. Figure 7.7 shows the Spec Limits window for the Cities.jmp sample data table after selecting OZONE, CO, SO2, and NO as process variables in the launch window. Enter the known specification limits and click OK to view the Process Capability report.

You can specify process importance values for each column. Process importance values provide a mechanism to sort processes in the order that you prefer. Process importance values are used to size markers in many of the graphs in the Process Capability report.

If you select the Show Limits option for a process and then save the specification limits to a column property, the Show as Graph Reference Lines option is selected in the saved Spec Limits column property. If you select the Show Limits option for a process and then save the specification limits to a new table, the Show Limits column in the new table contains a 1 for the process. The **Select All Show Limits** button selects the Show Limits option for all processes.

Figure 7.7 Spec Limits Window for Cities.jmp



#### **Limits Data Table**

You can also specify a limits data table with the **Load spec limits from data table** option from the Spec Limits window. Click the **Select Data Table** button and then select the appropriate data table that contains the specification limits for the analysis. After you select the appropriate limits table, the values populate the window. Click **OK** to view the Process Capability report.

A limits data table can be in two different formats: *tall* or *wide*. A tall limits data table has one column for the responses and the limits key words are the other columns. A wide limits data table has a column for each response with one column to label the limits keys. Either of these formats can be read using the **Load spec limits from data table** option.

A tall table contains four or five columns and has one row for each process. The first
column has a character data type and contains the names of the columns analyzed in the
Process Capability platform. The next three columns need to be named LSL, Target, and
USL. These column names can also be preceded by an underscore character. The optional
final column named Show Limits specifies if the specification limits are shown as reference
lines in select analysis plots.

Figure 7.8 Example of a Tall Specification Limits Table

▼ CitySpecLimits	1				
Locked File C:\Program Fil		Process	LSL	_Target	_USL
Notes For Spec Limits tabl	1	OZONE	0.075	0.15	0.25
	2	CO	5	7	12
▼ Columns (4/0)	3	SO2	0.01	0.04	0.09
Q	4	NO	0.01	0.025	0.04
♣ Process					
_LSL					
▲ _Target  ▲ USL					

A wide table contains three rows and one column for each column analyzed in the Process
Capability platform plus a \_LimitsKey column. In the \_LimitsKey column, the three rows
need to contain the identifiers \_LSL, \_Target, and \_USL.

**Figure 7.9** Example of a Wide Specification Limits Table

<b>•</b>					
-	_LimitsKey	OZONE	co	SO2	NO
1	_LSL	0	5	0	0
2	_Target	0.05	10	0.03	0.025
3	_USL	0.1	20	0.08	0.6

The easiest way to create a limits data table is to save results computed by the Process Capability platform. The Save options in the Process Capability red triangle menu enable you to save limits from the sample values. After entering or loading the specification limits, you can do the following:

- Select **Save > Save Spec Limits as Column Properties** to save the limits as Spec Limits column properties to the columns in the data table.
- Select Save > Save Distributions as Column Properties to save the distributions used in calculating capability as Process Capability Distribution column properties to the columns in the data table.
- Select Save > Save Spec Limits to New Table to save the limits to a new tall specification
  limits data table. If you have selected at least one nonnormal distribution, a column called
  Distribution that contains the specified distributions is also added to the limits data table.

See "Process Capability Platform Options".

# **Spec Limits Column Property**

When you perform a capability analysis, you can use Column Properties > Spec Limits to save specification limits as a column property. The Spec Limits property applies only to numeric columns.

Some processes have one-sided specifications. Some have no target. You can enter any of these that apply: a lower specification limit, an upper specification limit, a target value, or a process importance value.

Figure 7.10 displays the Spec Limits section of the Column Properties window for OZONE in the sample data table Cities.jmp.

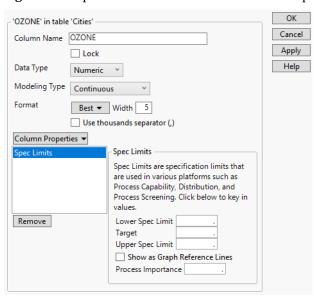


Figure 7.10 Spec Limits Section of the Column Properties Window

**Tip:** Saving specification limits as a column property ensures consistency when you repeat an analysis.

# The Process Capability Report

By default, the Process Capability platform provides the following reports:

• "Goal Plot" (provided only if at least one variable is fit with a normal distribution and shows only points for variables fit with normal distributions)

The Process Capability Report

- "Capability Box Plots" (provided only if at least one variable is fit with a normal distribution and shows only box plots for variables fit with normal distributions)
- "Capability Index Plot"

Figure 7.2 shows an example of a default Process Capability report.

Using the Process Capability red triangle menu, you can add individual detail reports, normalized box plots, and summary reports. The red triangle menu also has options for identifying out-of-spec values in your data table, creating a summary data table, changing the display order of analyzed columns, and saving out spec limits. These options are described in "Process Capability Platform Options".

You can change the default report at File > Preferences > Platforms > Process Capability. You can also make changes to the appearance of reports produced by options by selecting the relevant Process Capability topic at File > Preferences > Platforms.

#### **Goal Plot**

The Goal Plot shows, for each variable, the spec-normalized mean shift on the *x*-axis, and the spec-normalized standard deviation on the *y*-axis. It is useful for getting a quick, summary view of how the variables are conforming to specification limits. By default, the Goal Plot shows only those points for each column that are calculated using the overall sigma. Hover over each point to view the variable name and the sigma method used to calculate the point. See "Goal Plot" for more information about the calculation of the coordinates for the Goal Plot.

Note: Process variables with distributions other than Normal are not plotted on the Goal Plot.

#### **Goal Plot Points**

Points on the Goal Plot correspond to columns, not rows. Selecting a point in the Goal Plot selects the corresponding column in the data table. If process importance values are specified, the goal plot points are sized by importance.

Hover over a point in the Goal Plot to view a control chart for that process. Click the control chart to launch Control Chart Builder with the corresponding control chart and capability report.

**Note:** A control chart is not available for a process if the unbiased pooled standard deviation is chosen as the within-group variation statistic for that process.

The Process Capability Report

The points on the Goal Plot are also linked to the rows of the Goal Plot Summary Table, where each row corresponds to a column. You can select a point in the Goal Plot, right-click, and apply row states. These row states are applied to the rows of the Goal Plot Summary Table. Row states that you apply in the Goal Plot Summary Table are reflected in the Goal Plot. To see this table, select Make Goal Plot Summary Table from the Process Capability red triangle menu. See "Make Goal Plot Summary Table".

**Tip:** If you hide a point in the Goal Plot, you can show the point again by changing the corresponding row state in the Goal Plot Summary Table.

#### **Goal Plot Triangle**

The goal plot triangle appears in the center of the bottom of the Goal Plot. The slider to the right of the plot enables you to adjust the size of goal triangle in the plot.

By default, the Ppk slider and the value beneath it are set to Ppk = 1. This approximates a non-conformance rate of 0.0027, if the distribution is normal. The goal triangle represents the Ppk shown in the box. To change the Ppk value, move the slider or enter a number in the box.

JMP gives the Goal Plot in terms of Ppk values by default. You can change this preference at File > Preferences > Platforms > Process Capability. When the AIAG (Ppk) Labeling preference is unchecked, all of the Ppk labeling is changed to Cpk labeling, including the label of the slider to the right of the goal plot.

#### **Goal Plot Options**

The Goal Plot red triangle menu has the following options:

**Show Within Sigma Points** Shows or hides the points calculated using the within sigma estimate.

**Show Within or Between-and-Within Sigma Points** (Available only when Calculate Between-and-Within Capability is selected for at least one process in the launch window.) Shows or hides the points calculated using the within sigma estimate or, if specified, the between-and-within sigma estimate.

**Show Overall Sigma Points** Shows or hides the points calculated using the overall sigma estimate.

**Shade Levels** Shows or hides the Ppk level shading (Figure 7.11). When you select Shade Levels, shaded areas appear in the plot. The shaded areas depend on the relationship between *p* and Ppk, with *p* representing the value shown in the box beneath Ppk:

- Points in the red area have Ppk < p.</li>
- Points in the yellow area have p < Ppk < 2p.

Points in the green area have 2*p* < Ppk.</li>

**Label Within Sigma Points** Shows or hides labels for points calculated using the within sigma estimate.

**Label Within or Between-and-Within Sigma Points** (Available only when Calculate Between-and-Within Capability is selected for at least one process in the launch window.) Shows or hides labels for points calculated using the within sigma estimate or, if specified, the between-and-within sigma estimate.

**Label Overall Sigma Points** Shows or hides labels for points calculated using the overall sigma estimate.

**Defect Rate Contour** Shows or hides a contour representing a specified defect rate.

Figure 7.11 shows the Goal Plot for the entire data set for the Semiconductor Capability.jmp sample data table after selecting Shade Levels and Show Within Sigma Points from the Goal Plot red triangle menu.

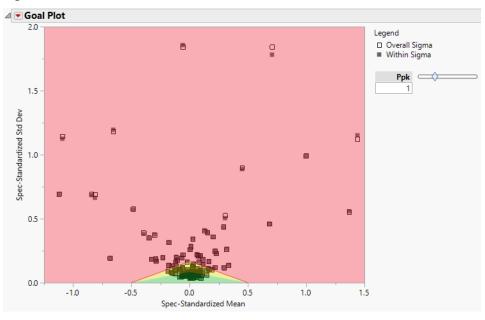


Figure 7.11 Goal Plot

#### **One-Sided or Missing Specification Limits**

When there is only one specification limit for a column, markers and colors are used in the following ways:

• If only the upper specification limit (USL) is specified, the point on the Goal Plot is represented by a right-pointing triangle and is colored blue.

- If only the lower specification limit (LSL) is specified, the point on the Goal Plot is represented by a left-pointing triangle and is colored red.
- If at least one process has only an upper specification limit, the right half of the goal triangle is blue.
- If at least one process has only a lower specification limit, the left half of the goal triangle is red.

Processes with only an upper specification limit are represented by blue and should be compared to the blue (right) side of the goal triangle. Processes with only a lower specification limit are represented by red and should be compared to the red (left) side of the goal triangle. For more information about how the coordinates of points are calculated, see "Goal Plot".

# **Capability Box Plots**

The Capability Box Plots show a box plot for each variable selected in the analysis. The values for each column are centered by their target value and scaled by the difference between the specification limits. If the target is not centered between the specification limits, the values are scaled by twice the minimum difference between the target and specification limits. For each process column  $Y_j$  (see "Notation for Goal Plots and Capability Box Plots" for a description of the notation):

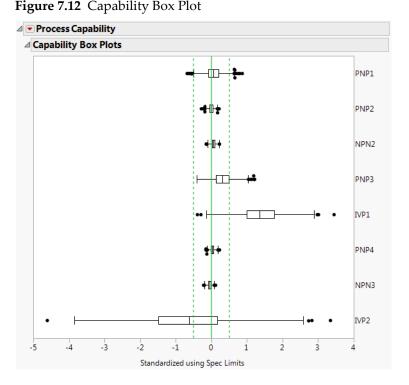
$$Z_{ij} = \frac{Y_{ij} - T_j}{2 \times \min(T_j - \text{LSL}_j, \text{USL}_j - T_j)}$$

For a process with a one-sided specification, see "One-Sided or Missing Specification Limits". For the situation where no target is specified, see "Capability Box Plots for Processes with Missing Targets".

**Note:** Process variables with distributions other than Normal are not plotted on the Capability Box Plot.

Figure 7.11 shows a Capability Box Plots report for eight variables in the Semiconductor Capability.jmp sample data table.

Element 10 Completition Description



The plot displays dotted green lines drawn at ±0.5.

- For a process with a target that is centered between its specification limits, the dotted green lines represent the standardized specification limits.
- For a process with a target that is not centered between its specification limits, one of the
  dotted green lines represents the standardized specification limit for the limit closer to the
  target. The other dotted green line represents the same distance in the opposite direction.

This plot is useful for comparing variables with respect to their specification limits. For example, in Figure 7.12, the majority of points for IVP1 are above its USL, and the majority of its points for IVP2 are less than its target. PNP2 seems to be on target with all data points in the specification limits.

#### **One-Sided or Missing Specification Limits**

When there is only one specification limit for a column, colors are used in the following ways:

- If only the upper specification limit (USL) is specified, the box plot is colored blue.
- If only the lower specification limit (LSL) is specified, the box plot is colored red.
- If at least one process has only an upper specification limit, the dotted line at 0.5 is blue.
- If at least one process has only a lower specification limit, the dotted line at -0.5 is red.

Process Capability

Suppose that only the lower specification limit is specified and that the process target is specified. The capability box plot is based on the following values for the transformed observations. See "Notation for Goal Plots and Capability Box Plots" for a description of the notation:

$$Z_{ij} = \frac{Y_{ij} - T_j}{2(T_j - LSL_j)}$$

Suppose that only the upper specification limit is specified and that the process target is specified. The capability box plot is based on the following values for the transformed observations:

$$Z_{ij} = \frac{Y_{ij} - T_j}{2(\text{USL}_j - T_j)}$$

For more information about how missing targets are handled with one-sided specification limits, see "Single Specification Limit and No Target".

# **Capability Index Plot**

The Capability Index Plot shows Ppk values for all variables that you entered as Y, Process. Each variable name appears on the horizontal axis and the Ppk values appear on the vertical axis. If you fit a nonnormal distribution, the fitted distribution name appears in the plot as a parenthetical suffix to the variable name. If process importance values are specified, the points on the capability index plot are sized by importance. A horizontal line is placed at the Ppk value that is specified by the slider to the right of the plot.

Hover over a point in the Capability Index Plot to view a control chart for that process. Click the control chart to launch Control Chart Builder with the corresponding control chart and capability report.

**Note:** A control chart is not available for a process if the unbiased pooled standard deviation is chosen as the within-group variation statistic for that process.

Figure 7.13 shows a Capability Index Plot report for the Process Measurements.jmp sample data table. Six of the variables are fit with nonnormal distributions. Process 7 is fit with a normal distribution. Points have been labeled using the Label Overall Sigma Points option that is available in the Capability Index Plot red triangle menu.

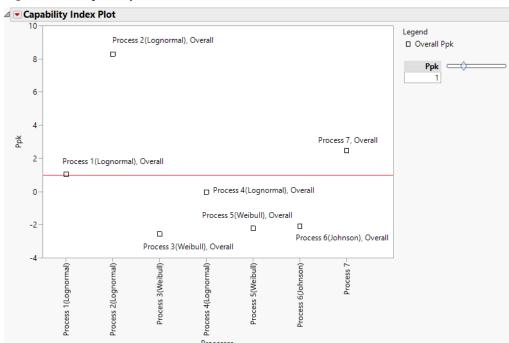


Figure 7.13 Capability Index Plot with Nonnormal Distributions

#### **Capability Index Plot Options**

The Capability Index Plot red triangle menu has the following options:

**Show Within Sigma Points** Shows or hides the points calculated using the within sigma estimate.

**Show Within or Between-and-Within Sigma Points** (Available only when Calculate Between-and-Within Capability is selected for at least one process in the launch window.) Shows or hides the points calculated using the within sigma estimate or, if specified, the between-and-within sigma estimate.

**Show Overall Sigma Points** Shows or hides the points calculated using the overall sigma estimate.

**Shade Levels** Shows or hides the Ppk level shading. When you select Shade Levels, shaded areas appear in the plot. The shaded areas depend on the relationship between *p* and Ppk, with *p* representing the value shown in the box beneath Ppk:

- Points in the red area have Ppk < p.</li>
- Points in the yellow area have p < Ppk < 2p.
- Points in the green area have 2p < Ppk.</li>

- **Label Within Sigma Points** Shows or hides labels for points calculated using the within sigma estimate.
- **Label Within or Between-and-Within Sigma Points** (Available only when Calculate Between-and-Within Capability is selected for at least one process in the launch window.) Shows or hides labels for points calculated using the within sigma estimate or, if specified, the between-and-within sigma estimate.
- **Label Overall Sigma Points** Shows or hides labels for points calculated using the overall sigma estimate.

# **Process Capability Platform Options**

The Process Capability red triangle menu contains the following options:

- **Individual Detail Reports** Shows or hides individual detail reports for each variable in the analysis. See "Individual Detail Reports".
- **Goal Plot** Shows or hides a goal plot for the data. The Goal Plot shows the spec-normalized mean shift on the *x*-axis and the spec-normalized standard deviation on the *y*-axis for each variable. See "Goal Plot". (Only variables for which you specify normal distributions are shown on the plot.)
- **Capability Box Plots** Shows or hides a capability box plot for each variable in the analysis. The values for each column are centered by their target value and scaled by twice the minimum difference between the target value and the specification limits. See "Capability Box Plots". (Box plots are shown only for variables for which you specify normal distributions.)
- **Normalized Box Plots** Provides two options for plots that show normalized box plots for each process variable. Each column is standardized by subtracting its mean and dividing by an estimate of the column's standard deviation. The box plot is constructed using quantiles for the standardized values. See "Normalized Box Plots". (Normalized box plots are shown only for variables for which you specify normal distributions.)
  - **Within Sigma Normalized Box Plots** Shows or hides a plot called Within Sigma Normalized Box Plots. The box plots are constructed using the within-subgroup estimate of standard deviation.
  - Within or Between-and-Within Sigma Normalized Box Plots (Available only when Calculate Between-and-Within Capability is selected for at least one process in the launch window.) Shows or hides a plot called Within or Between-and-Within Normalized Box Plots. The box plots are constructed using the within group estimate of the standard deviation or, if specified, the between-and-within estimate.

- Overall Sigma Normalized Box Plots Shows or hides a plot called Overall Sigma Normalized Box Plots. The box plots are constructed using the overall estimate of standard deviation.
- **Capability Index Plot** Shows overall Ppk values for all variables that you entered as Y, Process. See "Capability Index Plot".
- **Process Performance Plot** Shows or hides a four-quadrant plot of capability versus stability. Each process that has at least one specification limit is represented by a point. See "Process Performance Plot".
- **Summary Reports** Provides two options for summary reports of capability indices. See "Summary Reports".
  - Within Sigma Summary Report Shows or hides a summary report of capability indices calculated using the within-subgroup estimate of standard deviation. (Results are available only for variables with specified normal distributions.)
  - Within or Between-and-Within Sigma Summary Report (Available only when Calculate Between-and-Within Capability is selected for at least one process in the launch window.) Shows or hides a summary report of capability indices calculated using the within group estimate of the standard deviation or, if specified, the between-and-within group estimate.
  - **Overall Sigma Summary Report** Shows or hides a summary report of capability indices calculated using the overall estimate of standard deviation.

## **Action Options**

The following red triangle menu options perform actions:

- **Out of Spec Values** Provides options for the cells in the data table containing values that are out of spec.
  - **Select Out of Spec Values** Selects all rows and columns in the data table that contain at least one value that does not fall within the specification limits.
  - **Color Out of Spec Values** Colors the cells in the data table that correspond to values that are out of spec. The cell is colored blue if the value is above the USL and red if the value is below the LSL.

**Tip:** To remove colors in specific cells, select all cells of interest. Right-click in one of the cells and select Clear Color. To remove colors in all cells, deselect Color Out of Spec Values.

**Make Goal Plot Summary Table** Creates a summary table for the points plotted in the Goal Plot. This table includes the variable's name, its spec-normalized mean shift, and its

spec-normalized standard deviation. Each variable has two rows in this table: one for each sigma type (within and overall). See "Make Goal Plot Summary Table".

Order By Reorders the box plots, summary reports, and individual detail reports. You can reorder by Initial Order, Reverse Initial Order, Within Sigma Cpk Ascending, Within or Between-and-Within Sigma Cpk Ascending, Within Sigma Cpk Descending, Within or Between-and-Within Sigma Cpk Descending, Overall Sigma Ppk Ascending, or Overall Sigma Ppk Descending. The options that order by Within Sigma reorder plot elements only for variables with specified normal distributions.

**Note:** The options to order by Within or Between-and-Within Sigma are available only if Calculate Between-and-Within Capability is selected for at least one process in the launch window.

**Save** Provides options for saving specification limits and distributions.

**Save Spec Limits as Column Properties** Saves the specification limits to a column property for each variable in the analysis. If no Spec Limits column property is present, the column property is created. If a Spec Limits column property is present, the values in the column property are overwritten. See "Spec Limits Column Property".

**Save Distributions as Column Properties** Saves the distribution used in calculating capability as a Process Capability Distribution column property. See *Using JMP*.

If a column contains the Distribution property specifying a nonnormal distribution and no Process Capability Distribution property, then the Process Capability platform applies a nonnormal fit. The Process Capability platform uses the distribution specified in the Distribution column property, or a Johnson fit if that distribution is not supported in Process Capability. If a column contains the Process Capability Distribution property, then the Process Capability platform uses the distribution specified in the Process Capability Distribution column property.

**Note:** If you want to use a specific distribution in the Process Capability platform, save it as a Process Capability Distribution column property.

**Save Spec Limits to New Table** Saves the specification limits and the setting for Show Limits for each process to a limits data table in tall format. See "Limits Data Table".

**Relaunch Dialog** Opens the platform launch window and recalls the settings used to create the report.

See *Using JMP* for more information about the following options:

**Local Data Filter** Shows or hides the local data filter that enables you to filter the data used in a specific report.

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- **Redo** Contains options that enable you to repeat or relaunch the analysis. In platforms that support the feature, the Automatic Recalc option immediately reflects the changes that you make to the data table in the corresponding report window.
- **Save Script** Contains options that enable you to save a script that reproduces the report to several destinations.
- **Save By-Group Script** Contains options that enable you to save a script that reproduces the platform report for all levels of a By variable to several destinations. Available only when a By variable is specified in the launch window.

## **Individual Detail Reports**

The Individual Detail Reports option displays a capability report for each variable in the analysis.

#### **Normal Distributions**

Figure 7.14 shows the Individual Detail Report for PNP1 from the Semiconductor Capability.jmp sample data table as described in "Example of the Process Capability Platform with Normal Variables".

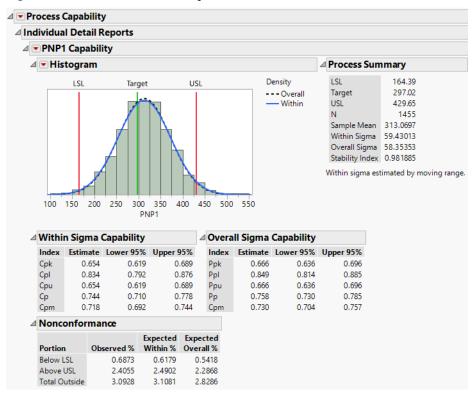


Figure 7.14 Individual Detail Report

The Individual Details report for a variable with a normal distribution shows a histogram, process summary details, and capability and nonconformance statistics. The histogram shows the distribution of the values, the lower and upper specification limits and the process target (if they are specified), and one or two curves showing the assumed distribution. The histogram in Figure 7.14 shows two normal curves, one based on the overall estimate of standard deviation and the other based on the within-subgroup estimate.

When you fit your process with a normal distribution, the Process Summary includes the *Stability Index*, which is a measure of stability of the process. The stability index is defined as follows:

(Overall Sigma/Within Sigma)

If Calculate Between-and-Within Capability is specified for a process in the launch window, the stability index for that process is defined as follows:

(Overall Sigma/Between-and-Within Sigma)

A stable process has stability index near one. Higher values indicate less stability.

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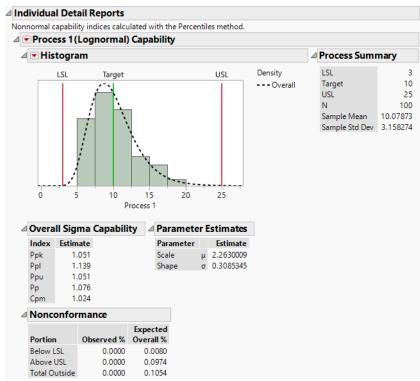
**Note:** You can change the preferences for stability assessment type in File > Preferences > Platforms > Process Capability. This changes the stability assessment type used through the Process Capability platform.

#### **Nonnormal Distributions**

**Note:** Capability indices based on within-subgroup variation and stability indices are not available for processes for which you have specified nonnormal distributions.

Figure 7.15 shows the Individual Detail Report for Process 1 from the Process Measurements.jmp sample data table as described in "Example of the Process Capability Platform with Nonnormal Variables".

Figure 7.15 Individual Detail Report for Process 1



The report opens with a note summarizing the Nonnormal Distribution Options that you selected in the launch window.

The Individual Details report for a variable with a nonnormal distribution shows a histogram, process summary details, and capability and nonconformance statistics. The histogram shows the distribution of the values, the lower and upper specification limits and the process target (if they are specified). A curve showing the fitted distribution is superimposed on the histogram. If you selected a Nonparametric distribution, the curve shown in the histogram is the nonparametric density.

The report also shows a Parameter Estimates report if you selected a nonnormal parametric distribution or a Nonparametric Density report if you selected a Nonparametric fit. See "Parameter Estimates" and "Nonparametric Density".

#### **Individual Detail Report Options**

The outline title for each variable in the Individual Detail Reports section is of the form <Variable Name> Capability. However, if you request nonnormal capability, the relevant distribution name is shown parenthetically in the outline title.

Each Capability report has a red triangle menu with the following options:

**Compare Distributions** Shows or hides the control panel for comparing distributions for the process. See "Compare Distributions".

**Process Summary** Shows or hides the summary statistics for the variable, including the overall sigma estimate, and, if you have specified a normal distribution, the within sigma estimate and the stability index. If you have specified Calculate Between-and-Within Capability for at least one process in the launch window, estimates for the between sigma and the between-and-within sigma are also included.

**Histogram** Shows or hides the histogram of the values of the variable. The histogram report includes a red triangle menu that controls the following features of the histogram:

**Show Spec Limits** Shows or hides vertical red lines on the histogram at the specification limits for the process.

**Show Target** Shows or hides a vertical green line on the histogram at the process target.

**Show Within Sigma Density** Shows or hides an approximating normal density function on the histogram with mean given by the sample mean and standard deviation given by the within estimate of sigma.

Show Between-and-Within Sigma Density (Available only when Calculate Between-and-Within Capability is selected for at least one process in the launch window.) Shows or hides an approximating normal density function on the histogram with mean given by the sample mean and standard deviation given by the between-and-within estimate of sigma.

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- **Show Overall Sigma Density** Shows or hides an approximating normal density function on the histogram with mean given by the sample mean and standard deviation given by the overall estimate of sigma.
- **Show Count Axis** Shows or hides an additional axis to the right of the histogram plot showing the count of observations.
- **Show Density Axis** Shows or hides an additional axis to the right of the histogram plot showing the density.
- **Capability Indices** Controls display of the following capability index reports:
  - **Within Sigma Capability** (Available when distribution is Normal.) Shows or hides capability indices (and confidence intervals) based on the within (short-term) sigma.
  - **Between-and-Within Sigma Capability** (Available only when distribution is Normal and Calculate Between-and-Within Capability is selected for at least one process in the launch window.) Shows or hides capability indices based on the between-and-within sigma.
  - **Within Sigma Z Benchmark** (Available when distribution is Normal.) Shows or hides Z benchmark indices based on the within (short-term) sigma.
  - **Between-and-Within Sigma Z Benchmark** (Available only when distribution is Normal and Calculate Between-and-Within Capability is selected for at least one process in the launch window.) Shows or hides Z benchmark indices based on the between-and-within sigma.
  - **Within Sigma Target Index** (Available when distribution is Normal.) Shows or hides an estimate of the target index that is based on the within (short-term) sigma.
  - **Between-and-Within Sigma Target Index** (Available only when distribution is Normal and Calculate Between-and-Within Capability is selected for at least one process in the launch window.) Shows or hides an estimate of the target index that is based on the between-and-within sigma.
  - **Overall Sigma Capability** Shows or hides capability indices (and confidence intervals) based on the overall (long-term) sigma.
  - **Overall Sigma Z Benchmark** (Available when distribution is Normal.) Shows or hides Z benchmark indices based on the overall (long-term) sigma.

**Note:** By default, the confidence intervals for the capability indices are constructed based on  $\alpha$  = 0.05. To change the default confidence level, select File > Preferences > Platforms > Process Capability.

**Nonconformance** Shows or hides the observed and expected percentages of observations below the LSL, above the USL, and outside of the specification limits. The Nonconformance table contains hidden columns for observed and expected PPM and counts.

Interactive Capability Plot Shows or hides the Interactive Capability Plot. The Interactive Capability Plot enables you to change the value of one or more summary statistics and see how the changes affect the capability analysis. There are Original and New reports that show the original and new summary statistics, capability indices, and expected PPM. Use the slider controls or text boxes to change the spec limits, mean, and overall sigma from the original values. You can also use the Mean Shift box to shift the mean by a factor of the original sigma. The Interactive Capability Plot report has the following red triangle menu options:

**Capability** Shows or hides the capability indices in the Original and New reports.

**Expected PPM** Shows or hides the expected PPM values in the Original and New reports.

**Revert to Original Values** Reverts the interactive capability plot and the summary values in the New report back to the original values.

**Save New Spec Limits as a Column Property** Saves the new specification limits as a Spec Limits column property to the column in the original data table.

**Note:** The analysis is not rerun with the new specification limits unless the Auto Recalc option is turned on.

**Parameter Estimates** (Available when a distribution other than Normal or Nonparametric is selected.) Shows or hides the Parameter Estimates report, which gives estimates for the parameters of the selected distribution.

The estimates for all except the Johnson family distributions are obtained using maximum likelihood. For more information about Johnson family fits, see "Johnson Distribution Fit Method".

The parameters and probability density functions for the normal, beta, exponential, gamma, Johnson, lognormal, and Weibull distributions are described in "Capability Indices for Nonnormal Distributions: Percentile and Z-Score Methods". These are the same parameterizations used in the Distribution platform, with the exception that Process Capability does not support threshold parameters. See *Basic Analysis*.

**Fix Parameters** (Available when a distribution other than Normal or Nonparametric is selected.) Displays a window that enables you to fix one or more parameter values in a nonnormal distribution. Enter a value in the User-defined Value column for the parameters that you would like to fix. Once you click OK, the omitted parameter values

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are re-estimated given the fixed parameter values. The re-estimated parameter values appear in the Parameter Estimates report, along with a column indicating which parameters are fixed.

**Nonparametric Density** (Available when Nonparametric is selected as the distribution.) Shows or hides the Nonparametric Density report, which gives the *kernel bandwidth* used in fitting the nonparametric distribution. The kernel bandwidth is given by the following, where *n* is the number of observations and *S* is the uncorrected sample standard deviation:

bandwidth = 
$$\frac{0.9S}{n^{1/5}}$$

#### **Compare Distributions**

The Compare Distributions report enables you to compare and apply various distributional fits. Note the following:

- Your selected distribution is indicated in the Selected column.
- The report initially shows fit statistics for your Selected distribution and other fitted distributions in the Comparison Details report. If you selected Best Fit, the Comparison Details report initially shows statistics for all parametric fits.
- Check the distributions in the Distribution list that you want to compare.
  - The probability density function for the best fitting distribution in each family that you select is superimposed on the histogram in the Histogram - Compare Distributions report.
  - If the distribution is parametric, a row for that family containing fit results is added to the Comparison Details report.
  - If Nonparametric is checked in the Distribution list, the Nonparametric Density report, showing the automatically selected kernel bandwidth, is added to the Compare Distributions report. See "Nonparametric Density".
  - You can change your selected distribution by selecting its radio button under Selected.
     The capability report is updated to show results for the selected distribution.

Figure 7.16 shows the Compare Distributions report for Process 1 in the Process Measurements.jmp sample data table. The Selected distribution, which is Lognormal, is being compared to a Normal distribution. The Comparison Details report shows fit statistics for both distributions.

To obtain probability plots, click the Compare Distributions red triangle and select Probability Plots. The points in the probability plot for the normal distribution in Figure 7.16 do not follow the line closely. This indicates a poor fit.

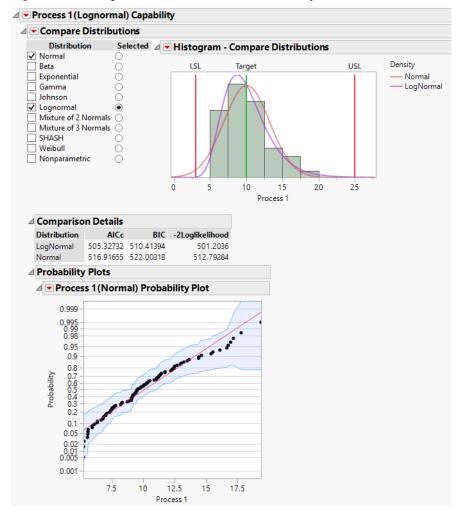


Figure 7.16 Compare Distributions with Probability Plot for Normal

#### **Compare Distributions Options**

The Compare Distributions red triangle menu contains the following options:

**Comparison Details** For each distribution, gives AICc, BIC, and -2Loglikelihood values. See *Fitting Linear Models*. (Not available for a Nonparametric fit.)

**Comparison Histogram** Shows or hides the Histogram report.

**Probability Plots** Shows or hides a report that displays probability plots for each parametric distribution that you fit (Figure 7.16). An observation's horizontal coordinate is its observed data value. An observation's vertical coordinate is the value of the quantile of the

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fitted distribution for the observation's rank. For the normal distribution, the overall estimate of sigma is used in determining the fitted distribution.

The red triangle menus associated with each Probability Plot contain the following options.

**Simultaneous Empirical Confidence Limits** Shows or hides confidence limits that have a simultaneous 95% confidence level of containing the true probability function, given that the data come from the selected parametric family. These limits have the same estimated precision at all points. Use them to determine whether the selected parametric distribution fits the data well. See Nair (1984) and Meeker and Escobar (1998).

**Simultaneous Empirical Confidence Limits Shading** Shows or hides shading of the region between the Simultaneous Empirical Confidence Limits.

**Parametric Fit Line** Shows or hides the line that shows the predicted probabilities for the observations based on the fitted distribution.

Parametric Fit Confidence Limits Shading Shows or hides shading of the region between parametric fit confidence intervals. The parametric fit confidence limits have confidence level (1 - Alpha), where Alpha is the value that you specify in the launch window. (Available only when the parametric fit confidence limits are meaningful and when it is possible to calculate them.)

When possible, the intervals are computed by expressing the parametric distribution F as a location-scale family, so that F(y) = G(z), where  $z = (y - \mu)/\sigma$ . The approximate standard error of the fitted location-scale component at a point is computed using the delta method. Using the standard error estimate, a Wald confidence interval for z is computed for each point. The confidence interval for the cumulative distribution function F is obtained by transforming the Wald interval using G. Note that, in some cases, special accommodations are required to provide appropriate intervals near the endpoints of the interval of process measurements.

**Order by Comparison Criterion** Orders the distributions in the Comparison Details report according to the criterion that you select. The default ordering is by AICc, unless you selected another criterion in the Distribution Comparison Criterion panel in the launch window.

## **Normalized Box Plots**

The Normalized Box Plots options show or hide box plots that have been normalized using the specified sigma in the title. When drawing normalized box plots, JMP standardizes each column by subtracting the mean and dividing by the standard deviation. The box plots are formed for each column using these standardized values.

Within Sigma Normalized Box Plots

PNP1[wafer]

PNP2[wafer]

NPN2[wafer]

PNP4[wafer]

PNP4[wafer]

NPN3[wafer]

NPN8[wafer]

Standardized using Mean and Within Std Dev

Figure 7.17 Within Sigma Normalized Box Plot

Figure 7.17 shows the Within Sigma Normalized Box Plot for a selection of the process variables in the Semiconductor Capability.jmp sample data table using wafer as a subgroup variable.

The green vertical lines represent the specification limits for each variable normalized by the mean and standard deviation of each variable. The gray dotted vertical lines are drawn at  $\pm 0.5$ , since the data is standardized to a standard deviation of 1.

## **Process Performance Plot**

The Process Performance Plot option shows or hides a four-quadrant plot of capability versus stability. Each process that has specification limits is represented by a point. If process importance values are specified, the points are sized by importance. The horizontal coordinate of each point equals the stability index of the process and the vertical coordinate of each point equals the overall Ppk capability of the process. The plot is divided into four shaded quadrants based on the following default boundaries:

- A stability index that exceeds 1.25 indicates that the process is unstable.
- A Ppk that is smaller than 1.0 indicates that the process is not capable.

Additionally, there is a red line on the graph that indicates where the Cpk value is 1. The boundaries that define the four quadrants can be adjusted using the Ppk and Stability Index slider controls to the right of the plot. You can also set preferences for your desired Capability and Stability boundaries, as well as stability assessment type in

File > Preferences > Platforms > Process Performance Plot and

File > Preferences > Platforms > Process Capability.

The legend contains descriptions of the shaded regions. If any of the processes are missing a lower or upper specification limit, the legend also shows the markers used for those processes. If the markers do not appear in the legend, then all of the processes in the plot contain both lower and upper specification limits. See "One-Sided or Missing Specification Limits".

Hover over a point in the Process Performance Plot to view a control chart for that process. Click the control chart to launch Control Chart Builder with the corresponding control chart and capability report.

**Note:** A control chart is not available for a process if the unbiased pooled standard deviation is selected as the within-group variation statistic for that process.

The Process Performance Plot red triangle menu contains the following option:

**Label Points** Shows or hides labels for each point in the Process Performance Plot.

**Show Within Cpk Curve** Shows or hides the within Cpk curve in the Process Performance Plot.



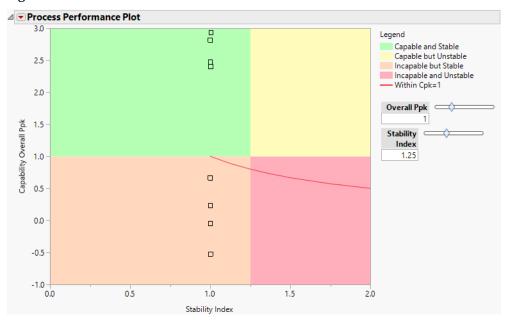


Figure 7.18 shows the Process Performance Plot for a selection of the process variables in the Semiconductor Capability.jmp sample data table using wafer as a subgroup variable.

# **Summary Reports**

The Summary Report options show or hide a table that contains the following statistics for each variable: LSL, Target, USL, Sample Mean, various Sigma estimates, Stability Index, Cpk, Cpl, Cpu, Cp, Cpm, and Nonconformance statistics. If there is at least one nonmissing process importance value, an Importance column is also included in the Summary Report. These statistics are calculated using the sigma estimate specified in the report title. The columns for Stability Index, Cpk, Cpl, Cpu, and Cp are colored as green, yellow, and red to indicate adequate, marginal, and poor stability or capability. This color coding scheme matches what you would see in the Process Performance graph.

**Note:** You can change the preferences for stability assessment type in File > Preferences > Platforms > Process Capability. This changes the stability assessment type used through the Process Capability platform.

Figure 7.19 shows a subset of columns for both summary reports as described in "Example of the Process Capability Platform with Normal Variables". The following optional columns are available for this report:

- Confidence intervals for Cpk, Cpl, Cpu, CP, and Cpm
- Expected and observed PPM statistics (outside, below LSL, above USL)

**Note:** The expected PPM statistics are the percentages you would expect to see based on the distribution chosen. By default, the distribution is normal. The observed PPM statistics are the percentages based on the actual data.

- Sample standard deviation
- The sample size (N), the minimum, and the maximum.
- Target Index

**Note:** Target Index is only available in the Within Sigma Capability Summary report.

To reveal these optional columns, right-click the report and select the column names from the Columns submenu.

Note that the report (based on overall sigma) shows the overall capability indices Ppk, Ppl, Ppu, and Pp instead of the within capability indices Cpk, Cpl, Cpu, and Cp. The labeling of the overall capability indices depends on the setting of the AIAG (Ppk) Labeling preference.

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Figure 7.19 Within Sigma and Overall Sigma Capability Summary Reports

Within	Sigma Ca	pability	Summa	ry Report							
Process	LSL	Target	IISI	Sample Mean	Within Sigma	Stability Index	Cpk	Cpl	Сри	Ср	Срп
PNP1	164.39	297.02	429.65	313.0697	59.43013		0.654	0.834	0.654	0.744	0.71
PNP2	-136.12	465.44	1067.01	456.6157		1.007008	2,492	2,492	2.567	2.530	2.51
NPN2	96.59	113.75	130.9	115.7421	2.131652	0.98552	2,370	2.995	2.370	2.683	1.95
PNP3	118.68	130.29	141.9	137.6146	6.160912	0.983744	0.232	1.024	0.232	0.628	0.40
IVP1	59.62	63.41	67.2	73.78072	4.238298	0.990097	-0.518	1.114	-0.518	0.298	0.11
PNP4	-54.43	238.74	531.91	256.3756	33.22573	0.981389	2.764	3.118	2.764	2.941	2.59
NPN3	97.32	120.8	144.29	118.1352	2.362847	1.000809	2.936	2.936	3.690	3.313	2.19
IVP2	139.2	142.31	145.41	138.2432	7.406516	0.989286	-0.043	-0.043	0.323	0.140	0.12
Overall	Sigma Ca	pability	Summa	ry Report							
					Overall	Stability					
Process	LSL	Target	USL	Sample Mean	Sigma	Index	Ppk	Ppl	Ppu	Pp	Cpn
								0.040		0.750	
PNP1	164.39	297.02	429.65	313.0697	58.35353	0.981885	0.666	0.849	0.666	0.758	0.73
	164.39 -136.12	297.02 465.44	429.65 1067.01	313.0697 456.6157	58.35353 79.82589	0.981885 1.007008	2.475	2.475	2.549	2.512	0.73 2.49
PNP1				5.5.005.							
PNP1 PNP2	-136.12	465.44	1067.01	456.6157	79.82589	1.007008	2.475	2.475	2.549	2.512	2.49
PNP1 PNP2 NPN2	-136.12 96.59	465.44 113.75	1067.01 130.9	456.6157 115.7421	79.82589 2.100786	1.007008 0.98552	2.475 2.405	2.475 3.039	2.549 2.405	2.512 2.722	2.49 1.97
PNP1 PNP2 NPN2 PNP3	-136.12 96.59 118.68	465.44 113.75 130.29	1067.01 130.9 141.9	456.6157 115.7421 137.6146	79.82589 2.100786 6.060762	1.007008 0.98552 0.983744	2.475 2.405 0.236	2.475 3.039 1.041	2.549 2.405 0.236	2.512 2.722 0.639	2.49 1.97 0.40 0.11
PNP1 PNP2 NPN2 PNP3 IVP1	-136.12 96.59 118.68 59.62	465.44 113.75 130.29 63.41	1067.01 130.9 141.9 67.2	456.6157 115.7421 137.6146 73.78072	79.82589 2.100786 6.060762 4.196326	1.007008 0.98552 0.983744 0.990097	2.475 2.405 0.236 -0.523	2.475 3.039 1.041 1.125	2.549 2.405 0.236 -0.523	2.512 2.722 0.639 0.301	2.49 1.97 0.40

# **Make Goal Plot Summary Table**

The Make Goal Plot Summary Table option produces a summary data table that includes each variable's name, its spec-normalized mean shift (Spec-Standardized Mean), and its spec-normalized standard deviation (Spec-Standardized Std Dev). For each variable, there is a row for each of the sigma types.

**Note:** If a variable is fit with a distribution other than normal, the name of the fitted distribution is appended parenthetically to the variable name. The Spec-Standardized Mean and Spec-Standardized Std Dev values are not provided for nonnormal variables.

The points in the Goal Plot are linked to the rows in the Goal Plot Summary Table. If you apply row states to a point in the Goal Plot, you can change the corresponding row states in the Goal Plot Summary Table. Conversely, if you apply row states in the Goal Plot Summary Table, they are reflected on the Goal Plot.

Figure 7.20 shows the Goal Plot Summary Table for the Semiconductor Capability.jmp sample data table as described in "Example of the Process Capability Platform with Normal Variables".

**Process Capability** 

Figure 7.20	Summary	Table

	Process	Sigma Type	Spec-Standardized Mean	Spec-Standardized Std Dev
1	PNP1	Within	0.0605056038	0.2240448185
2	PNP2	Within	-0.00733452	0.0658873257
3	NPN2	Within	0.0580798256	0.0621472935
4	PNP3	Within	0.3154424678	0.2653278331
5	IVP1	Within	1.3681693325	0.5591421926
6	PNP4	Within	0.0300774244	0.0566663241
7	NPN3	Within	-0.05674621	0.0503161575
8	IVP2	Within	-0.65593547	1.1945993146
9	PNP1	Overall	0.0605056038	0.2199861461
10	PNP2	Overall	-0.00733452	0.0663490674
11	NPN2	Overall	0.0580798256	0.0612473972
12	PNP3	Overall	0.3154424678	0.2610147096
13	IVP1	Overall	1.3681693325	0.5536050447
14	PNP4	Overall	0.0300774244	0.0556117297

# Additional Examples of the Process Capability Platform

- "Process Capability for a Stable Process"
- "Process Capability for an Unstable Process"
- "Simulation of Confidence Limits for a Nonnormal Process Ppk"

# **Process Capability for a Stable Process**

In this example, you verify the assumptions that enable you to estimate PPM defective rates based on a capability analysis. You access Process Capability through Control Chart Builder and then directly. The data consist of 22 subgroups of size five. There are six missing readings, with three in each of two consecutive subgroups.

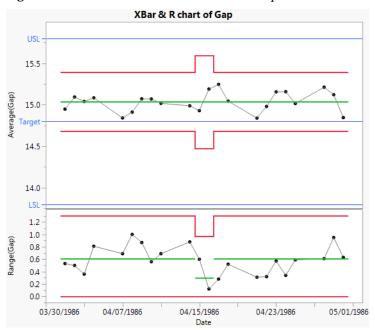
## **Process Capability through Control Chart Builder**

You can use Control Chart Builder to check process stability and the normality assumption for your process characteristic. You can also obtain Process Capability information directly within Control Chart Builder.

- 1. Select **Help > Sample Data Library** and open Quality Control/Clips2.jmp.
- 2. Select Analyze > Quality and Process > Control Chart Builder.
- 3. Drag Date to the **Subgroup** zone.

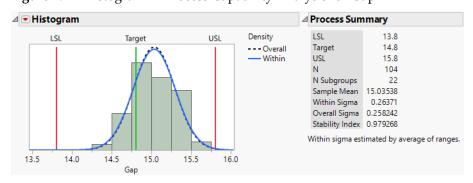
#### 4. Drag Gap to the Y zone.

Figure 7.21 XBar and R Control Chart for Gap



The control chart indicates that Gap is stable over time. Because Gap has the Spec Limits column property, a Process Capability Analysis report appears to the right of the control chart.

Figure 7.22 Histogram in Process Capability Analysis for Gap



The histogram and fitted normal blue curve suggest that the distribution of Gap is approximately normal. Although the process is stable, the distribution of Gap is shifted to the right of the specification range.

The Process Summary report shows the specification limits that are saved to the Spec Limits column property. It also shows that the estimate of sigma calculated from within-subgroup variation (Within Sigma) does not differ greatly from the overall estimate given by the sample standard deviation (Overall Sigma). Consequently, the Stability Index is near one (0.979268). This is expected because the process is stable.

Right-click in the body of the Nonconformance report and select Expected Within PPM from the Columns submenu.

Figure 7.23 Capability Indices and Nonconformance Report

Within Sigma Capability					✓ Overall Sigma Capability			
Index	Estimate	Lower 95%	Upper 9	5%	Inde	x Estimate	Lower 95%	Upper 95%
Cpk	0.966	0.805	1.1	128	Ppk	0.987	0.838	1.130
Cpl	1.562	1.314	1.8	308	Ppl	1.595	1.367	1.82
Cpu	0.966	0.805	1.1	127	Ppu	0.987	0.837	1.13
Ср	1.264	1.071	1.4	157	Pp	1.291	1.115	1.46
Cpm	0.943	0.828	1.0	158 Cpm	0.954	0.841	1.072	
Nonco	nforma	nce						
		1	Expected	Ex	pected	Expected		
Portion	Ob	served %	Within %	Ov	erall %	Within PPM		
Below LS	L	0.0000	0.0001		0.0001	1.402263		
Above US	SL	0.0000	0.1869		0.1534	1869.0329		
Total Out	tside	0.0000	0.1870		0.1535	1870.4352		

The Cpk value calculated using subgroup variation is 0.966, indicating that the process is not very capable. The Cpl value suggests good performance, but this is because the process is shifted away from the lower specification limit. Defective parts generally result from large values of Gap.

Note that the confidence interval for Cpk is wide; it ranges from 0.805 to 1.128. This occurs even though there are 104 observations. Capability indices are surprisingly variable, due to the fact that they are ratios. It is easy to reach incorrect conclusions based on the point estimate of a capability index.

The estimates of out-of-specification product given in the Nonconformance report provide a direct measure of process performance. The PPM values in the Nonconformance report indicate that Gap hardly ever falls below the lower specification limit (1.4 parts per million). However, the number of parts for which Gap falls above the upper specification limit is 1869.0 parts per million.

For an uncentered process, the Cp value indicates potential capability if the process were adjusted to be centered. If this process were adjusted to be centered at the target value of 14.8, then its capability would be 1.264, with a confidence interval from 1.071 to 1.457.

#### **Process Capability Platform**

Now that you have verified stability and normality for Gap, you can obtain additional information in the Process Capability platform.

1. Select Analyze > Quality and Process > Process Capability.

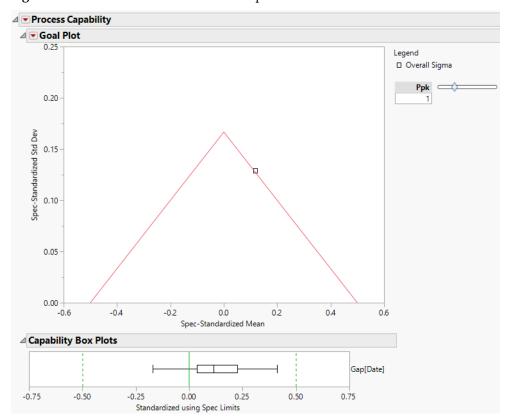
Additional Examples of the Process Capability Platform

- 2. Select Gap and click Y, Process.
- 3. Open the **Process Subgrouping** outline.
- 4. Select Date in the Select Columns list and Gap in the Roles list.
- 5. Click Nest Subgroup ID Column.

By default, the Within-Subgroup Variation Statistic selection is set to Average of Unbiased Standard Deviations. In the Control Chart Builder example ("Process Capability through Control Chart Builder"), subgroup ranges were used.

6. Click OK.

Figure 7.24 Goal Plot and Box Plot for Gap



The Goal Plot shows the Ppk index for Gap as being essentially equal to 1. The box plot shows that most values fall within specifications, but the preponderance of data values are shifted to the right within the specification range.

7. Click the Process Capability red triangle and select Individual Detail Reports.

The report is the one obtained using Control Chart Builder, except that the With

The report is the one obtained using Control Chart Builder, except that the Within Sigma is based on average standard deviations rather than average ranges. See "Histogram in

Process Capability Analysis for Gap" and "Capability Indices and Nonconformance Report".

# **Process Capability for an Unstable Process**

This example shows a case where the overall variation differs from the within variation because the process is not stable. It uses the Coating.jmp data table from the Quality Control folder of Sample Data (taken from the *ASTM Manual on Presentation of Data and Control Chart Analysis*). The process variable of interest is the Weight column, grouped into subgroups by the Sample column.

- 1. Select **Help > Sample Data Library** and open Quality Control/Coating.jmp.
- 2. Select Analyze > Quality and Process > Process Capability.
- 3. Select Weight and click Y, Process.
- 4. Open the **Process Subgrouping** outline.
- 5. Select Sample in the **Select Columns** list on the left.
- 6. Select Weight in the **Cast Selected Columns into Roles** list on the right.
- 7. Click Nest Subgroup ID Column.
- 8. Click **OK**.
- 9. Enter 16 for **LSL**, 20 for **Target**, and 24 for **USL** in the **Spec Limits** window.
- 10. Click **OK**.
- 11. Click the Goal Plot red triangle and select **Show Within Sigma Points**.
- 12. Click the Process Capability red triangle and select Individual Detail Reports.

Figure 7.25 Process Capability Report for Coating.jmp Data

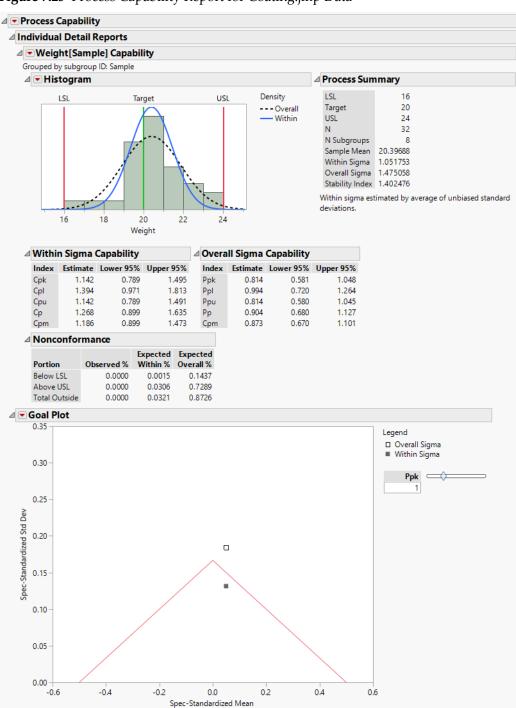


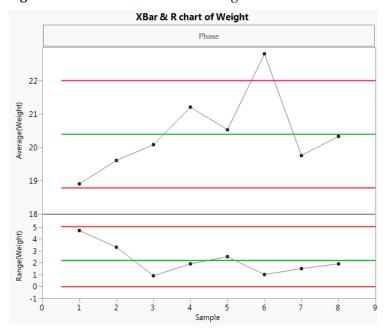
Figure 7.25 shows the resulting Process Capability report. The Goal Plot shows two points that represent the mean shift and standard deviation standardized to the specification limits. There is a legend next to the Goal Plot that identifies the two points. The Overall Sigma point is calculated using the overall sample standard deviation. The Within Sigma point is calculated using a within-subgroup estimate of the standard deviation.

The point calculated using Overall Sigma is outside the goal triangle corresponding to a Ppk of 1. This indicates that the variable Weight results in non-conforming product.

However, the point calculated using Within Sigma is inside the goal triangle. This indicates that, if the process were stable, Weight values would have a high probability of falling within the specification limits.

- 13. Hover cursor over one of the points in the Goal Plot.
- 14. Click the control chart.

Figure 7.26 XBar and R Chart for Weight



The control chart indicates that the Weight measurements are unstable. The process is affected by special causes and is unpredictable. This makes the interpretation of capability indices and nonconformance estimates highly questionable. Even estimates based on Overall Sigma are questionable, because the process is not predictable.

Additional Examples of the Process Capability Platform

The histogram in Figure 7.25 shows the distribution of the Weight values with normal density curves using both sigma estimates superimposed over the histogram. The normal curve that uses the Overall Sigma estimate is flatter and wider than the normal curve that uses the Within Sigma estimate. This normal curve is more dispersed because the estimate of Overall Sigma is inflated by the special causes that make the process unstable. If the process were stable, the narrower normal curve would reflect process behavior.

You can also compare the Cpk estimate (1.142) to the Ppk estimate (0.814). The fact that Ppk is much smaller than Cpk is additional evidence that this is an unpredictable process. The Cpk estimate is a forecast of the capability that you would achieve by bringing the process to a stable state.

**Note:** The Individual Detail Reports Cutoff preference determines whether the Individual Reports appear by default. If the preference is enabled, the Individual Reports appear by default if the number of process variables is less than or equal to the number specified in the preference. You can change this preference in Preferences > Platforms > Process Capability.

# Simulation of Confidence Limits for a Nonnormal Process Ppk

In this example, you first perform a capability analysis for the three nonnormal variables in Tablet Measurements.jmp. You then use Simulate to find confidence limits for the nonconformance percentage for the variable Purity.

#### **Nonnormal Capability Analysis**

If you prefer not to follow the steps below, you can obtain the results in this section by running the **Process Capability** table script in Tablet Measurements.jmp.

- 1. Select **Help > Sample Data Library** and open Tablet Measurements.jmp.
- 2. Select Analyze > Quality and Process > Process Capability.
- 3. Select Weight, Thickness, and Purity and click **Y**, **Process**.
- 4. Select Weight, Thickness, and Purity in the **Cast Selected Columns into Roles** list on the right.
- 5. Open the **Distribution Options** outline.
- 6. From the Distribution list, select **Best Fit**.
- 7. Click Set Process Distribution.

The **&Dist(Best Fit)** suffix is added to each column name in the list on the right.

8. Click **OK**.

A Capability Index Plot appears, showing the Ppk values. Note that only the Thickness variable appears above the line that denotes Ppk = 1. Purity is nearly on the line. Although

the number of measurements, 250, seems large, the estimated Ppk value is still quite variable. For this reason, you construct a confidence interval for the true Purity Ppk value.

**Note:** Because a Goal Plot is not shown, you can conclude that a normal distribution fit was not the best fit for any of the three variables.

9. Click the Process Capability red triangle and select **Individual Detail Reports**.

The best fits are different for each process.

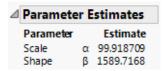
Weight: LognormalThickness: SHASHPurity: Weibull

#### **Construct the Simulation Column**

To use the Simulate utility to estimate Ppk confidence limits, you need to construct a simulation formula that reflects the fitted Weibull distribution. If you prefer not to follow the steps below, you can obtain the results in this section by running the **Add Simulation Column** table script.

1. Scroll to the Purity (Weibull) Capability report and find the Parameter Estimates report.

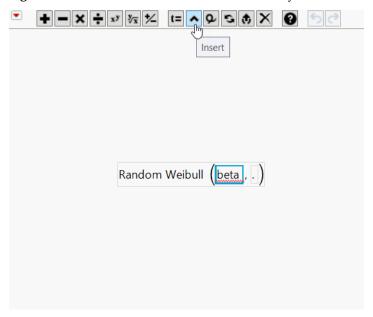
Figure 7.27 Weibull Parameter Estimates for Purity



These are the parameter estimates for the best fitting distribution, which is Weibull.

- 2. In the Tablet Measurements.jmp sample data table, select **Cols > New Columns**.
- 3. Next to **Column Name**, enter Simulated Purity.
- 4. From the Column Properties list, select Formula.
- 5. In the formula editor, select **Random > Random Weibull**.
- 6. The placeholder for **beta** is selected. Click the insertion element (^).

Figure 7.28 Formula Editor for Simulated Purity Column



This adds a placeholder for the parameter **alpha**.

- 7. In the Process Capability report, under Purity (Weibull) Capability, right-click in the Parameter Estimates report table and select **Make into Data Table**.
- 8. Copy the entry in Row 2 in the Estimate column (1589.7167836).
- 9. In the formula editor window, select the placeholder for **beta** in the **Random Weibull** formula and paste 1589.7167836 into the placeholder for **beta**.
- 10. In the data table that you created from the Parameter Estimates report, copy the entry in Row 1 in the Estimate column (99.918708989).
- 11. In the formula editor window, select the placeholder for **alpha** in the **Random Weibull** formula and paste 99.918708989 into the placeholder for **alpha**.

Figure 7.29 Completed Formula Window

Random Weibull (1589.7167836), 99.918708989)

- 12. Click **OK** in the formula editor window.
- 13. In the Tablet Measurements.jmp data table, right-click the Simulated Purity column and select **Column Properties > Spec Limits**.
- 14. Next to Lower Spec Limit, type 99.5.
- 15. Click **OK** in the New Column window.

The Simulated Purity column contains a formula that simulates values from the best-fitting distribution.

#### Simulate Confidence Intervals for Purity Ppk and Expected Percent Nonconforming

When you use Simulate, the entire analysis is run the number of times that you specify. To shorten the computing time, you can minimize the computational burden by running only the required analysis. In this example, because you are interested only in Purity with a fitted Weibull distribution, you perform only this analysis before running Simulate.

**Note:** If you do not care about computing time, you can use the same report you created in the previous section and start with step 7.

- 1. In the Process Capability report, click the Process Capability red triangle and select Relaunch Dialog.
- 2. (Optional) Close the Process Capability report.
- 3. In the launch window, from the Cast Selected Columns into Roles list, select Weight&Dist(Lognormal) and Thickness&Dist(SHASH).
- Click Remove.
- Click **OK**.
- Click the Process Capability red triangle and select Individual Detail Reports. Both Ppk and Ppl values are provided, but they are identical because Purity has only a lower specification limit.
- 7. In the Overall Sigma Capability report, right-click the **Estimate** column and select Simulate.

In the Column to Switch Out list, make sure Purity is selected. In the Column to Switch In list, make sure Simulated Purity is selected.

8. Next to **Number of Samples**, type **500**.

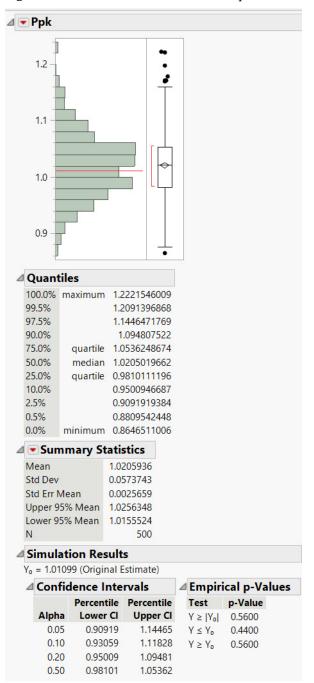
**Note:** The next step is not required. However, it ensures that you obtain exactly the simulated values shown in this example.

- 9. (Optional) Next to **Random Seed**, type **12345**.
- 10. Click **OK**.

The calculation might take several seconds. A data table entitled Process Capability Simulate Results (Estimate) appears. The Ppk and Ppl columns in this table each contain 500 values calculated based on the Simulated Purity formula. The first row, which is excluded, contains the values for Purity obtained in your original analysis. Because Purity has only a lower specification limit, the Ppk values are identical to the Ppl values.

11. In the Process Capability Simulate Results (Estimate) data table, click the green triangle next to the **Distribution** script.

Figure 7.30 Distribution of Simulated Ppk Values for Purity



**Note:** Your values may vary slightly from what is shown, depending on the decimal precision of the parameters in the Simulated Purity column formula.

Two Distribution reports are shown, one for Ppk and one for Ppl. But Purity has only a lower specification limit, so that the Ppk and Ppl values are identical. For this reason, the Distribution reports are identical.

The Simulation Results report shows that a 95% confidence interval for Ppk is 0.909 to 1.145. This indicate that the true Ppk value could be above 1.0, which would place Purity above the Ppk = 1 line in the Capability Index Plot you constructed in "Nonnormal Capability Analysis".

12. In the Process Capability report, right-click the **Expected Overall %** column in the Nonconformance report and select **Simulate**.

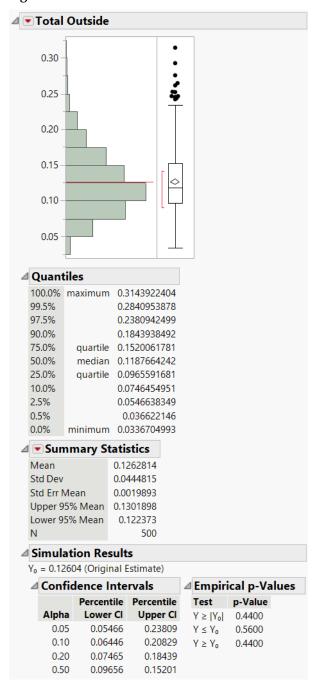
In the **Column to Switch Out** list, make sure Purity is selected. In the **Column to Switch In** list, make sure Simulated Purity is selected.

- 13. Next to **Number of Samples**, enter **500**.
- 14. (Optional) Next to Random Seed, enter 12345.
- 15. Click **OK**.

The calculation might take several seconds. A data table entitled Process Capability Simulate Results (Expected Overall %) appears. Because Purity has only a lower specification limit, the Below LSL values are identical to the Total Outside values.

16. In the Process Capability Simulate Results (Expected Overall %) data table, click the green triangle next to the **Distribution** script.

Figure 7.31 Distribution of Simulated Total Outside Values for Purity



**Note:** Your values may vary slightly from what is shown, depending on the decimal precision of the parameters in the Simulated Purity column formula.

Again, two identical Distribution reports appear. The Simulation Results report shows that a 95% confidence interval for the Expected Overall % nonconforming is 0.055 to 0.238.

# Statistical Details for the Process Capability Platform

- "Variation Statistics"
- "Notation for Goal Plots and Capability Box Plots"
- "Goal Plot"
- "Capability Box Plots for Processes with Missing Targets"
- "Capability Indices for Normal Distributions"
- "Capability Indices for Nonnormal Distributions: Percentile and Z-Score Methods"
- "Parameterizations for Distributions"

#### **Variation Statistics**

Denote the standard deviation of the process by  $\sigma$ . The Process Capability platform provides two types of capability indices. The Ppk indices are based on an estimate of  $\sigma$  that uses all of the data in a way that does not depend on subgroups. This overall estimate can reflect special cause as well as common cause variation. The Cpk indices are based on an estimate that attempts to capture only common cause variation. The Cpk indices are constructed using within-subgroup or between-and-within-subgroup estimates of  $\sigma$ . In this way, they attempt to reflect the true process standard deviation. When a process is not stable, the different estimates of  $\sigma$  can differ markedly.

# Overall Sigma

The overall sigma does not depend on subgroups. The overall estimate of  $\sigma$  is calculated as follows:

$$\hat{\sigma} = \sqrt{\frac{1}{N-1} \sum_{i=1}^{N} (y_i - \overline{y})^2}$$

Statistical Details for the Process Capability Platform

The formula uses the following notation:

N = number of nonmissing values in the entire data set

 $y_i$  = value of the  $i^{th}$  observation

 $\bar{y}$  = mean of nonmissing values in the entire data set

**Caution:** When the process is stable, the Overall Sigma estimates the process standard deviation. If the process is not stable, the overall estimate of  $\sigma$  is of questionable value, since the process standard deviation is unknown.

#### Estimates of Sigma Based on Within-Subgroup Variation

An estimate of  $\sigma$  that is based on within-subgroup variation can be constructed in one of the following ways:

- Within sigma estimated by average of ranges
- Within sigma estimated by average of unbiased standard deviations
- Within sigma estimated by moving range
- Within sigma estimated by unbiased pooled standard deviation

If you specify a subgroup ID column or a constant subgroup size on the launch window, you can specify your preferred within-subgroup variation statistic. See "Launch the Process Capability Platform". If you do not specify a subgroup ID column, a constant subgroup size, or a historical sigma, JMP estimates the within sigma using the third method (moving range of subgroups of size two).

#### Within Sigma Based on Average of Ranges

Within sigma estimated by the *average of ranges* is the same as the estimate of the standard deviation of an *XB*ar and *R* chart:

$$\hat{\sigma} = \frac{\frac{R_1}{d_2(n_1)} + \dots + \frac{R_N}{d_2(n_N)}}{N}$$

The formula uses the following notation:

 $R_i$  = range of  $i^{th}$  subgroup

 $n_i$  = sample size of  $i^{th}$  subgroup

 $d_2(n_i)$  = expected value of the range of  $n_i$  independent normally distributed variables with unit standard deviation

N = number of subgroups for which  $n_i \ge 2$ 

#### Within Sigma Based on Average of Unbiased Standard Deviations

Within sigma estimated by the *average of unbiased standard deviations* is the same as the estimate for the standard deviation in an XBar and S chart:

$$\hat{\sigma} = \frac{\frac{s_1}{c_4(n_1)} + \dots + \frac{s_N}{c_4(n_N)}}{N}$$

The formula uses the following notation:

 $n_i$  = sample size of  $i^{th}$  subgroup

 $c_4(n_i)$  = expected value of the standard deviation of  $n_i$  independent normally distributed variables with unit standard deviation

N = number of subgroups for which  $n_i \ge 2$ 

 $s_i$  = sample standard deviation of the i<sup>th</sup> subgroup

#### Within Sigma Based on Average Moving Range

Within sigma estimated by *average moving range* is the same as the estimate for the standard deviation for Individual Measurement and Moving Range charts:

$$\hat{\sigma} = \frac{\overline{MR}}{d_2(2)}$$

The formula uses the following notation:

 $\overline{MR}$  = the mean of the nonmissing moving ranges computed as  $(MR_2+MR_3+...+MR_N)/(N-1)$  where  $MR_i = |y_i - y_{i-1}|$ .

 $d_2(2)$  = expected value of the range of two independent normally distributed variables with unit standard deviation.

#### Within Sigma Based on Median Moving Range

Within sigma estimated by median moving range:

$$\hat{\sigma} = \frac{MMR}{0.954}$$

The formula uses the following notation:

MMR = the median of the nonmissing moving ranges computed as Median( $MR_2$ ,  $MR_3$ ,...,  $MR_N$ ) where  $MR_i = |y_i - y_{i-1}|$ .

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# Within Sigma Based on Unbiased Pooled Standard Deviation

Within sigma estimated by the unbiased pooled standard deviation:

$$\hat{\sigma} = \frac{\sqrt{(n_1 - 1)s_1^2 + \dots + (n_N - 1)s_N^2}}{c_4(n)\sqrt{n_1 + \dots + n_2 - N}}$$

The formula uses the following notation:

 $n_i$  = sample size of  $i^{th}$  subgroup

 $n = n_1 + ... + n_N$ , the total sample size

 $c_4(n)$  = expected value of the standard deviation of n independent normally distributed variables with unit standard deviation

N = number of subgroups for which  $n_i \ge 2$ 

 $s_i$  = sample standard deviation of the i<sup>th</sup> subgroup

#### **Estimate of Sigma Based on Between Group Variation**

#### Between Sigma Based on Moving Range

The estimate of  $\sigma$  that is based on between-subgroup variation is estimated by the moving range of subgroup means:

$$\hat{\sigma} = \sqrt{\left(\frac{\overline{MR}}{d_2(2)}\right)^2 - \frac{\hat{\sigma}^2 \text{Within}}{H}}$$

The formula uses the following notation:

 $\overline{MR}$  = the mean of the nonmissing moving ranges computed as  $(MR_2 + MR_3 + ... + MR_N)/(N-1)$  where  $MR_i = |y_i - y_{i-1}|$ .

 $d_2(2)$  = expected value of the range of two independent normally distributed variables with unit standard deviation.

 $\sigma^2_{\text{within}}$  = the specified within sigma estimate.

$$H = \frac{N}{\frac{1}{n_1} + \frac{1}{n_2} + \dots + \frac{1}{n_N}}, \text{ the harmonic mean of subgroup sample sizes.}$$

#### Estimate of Sigma Based on Between and Within Group Variation

#### Between-and-Within Sigma

The estimate of sigma that is based on the combined between and within group variation is defined as follows:

$$\hat{\sigma} = \sqrt{\hat{\sigma}_{within}^2 + \hat{\sigma}_{between}^2}$$

# **Notation for Goal Plots and Capability Box Plots**

The formulas for the Goal Plot and Capability Box Plots use the following notation:

 $Y_{ii} = i^{th}$  observation for process j

 $\overline{Y}_j$  = mean of the observations on process j

 $SD(Y_i)$  = standard deviation of the observations on process j

 $T_i$  = target value for process j

 $LSL_i$  = lower specification limit for process j

 $USL_i$  = upper specification limit for process j

# **Goal Plot**

This section provides details about the calculation of the mean shift and standard deviation standardized to specification quantities plotted in the Goal Plot. This section uses the notation defined in "Notation for Goal Plots and Capability Box Plots".

The mean shift and the standard deviation standardized to the specification limits for the i<sup>th</sup> column are defined as follows:

Spec-Standardized Mean = 
$$\frac{\overline{Y}_j - T_j}{2 \times \min(T_j - LSL_j, USL_j - T_j)}$$

Spec-Standardized Std Dev = 
$$\frac{SD(Y_j)}{2 \times \min(T_j - LSL_j, USL_j - T_j)}$$

**Note:** If either LSL<sub>i</sub> or USL<sub>i</sub> is missing, twice the distance from the target to the nonmissing specification limit is used in the denominators of the Goal Plot coordinates.

#### **Goal Plot Points for Processes with Missing Targets**

Suppose that the process has both a lower and an upper specification limit but no target. Then the formulas given in "Goal Plot" are used, replacing  $T_j$  with the midpoint of the two specification limits.

Suppose that the process has only one specification limit and no target. To obtain (x,y) coordinates for a point on the Goal Plot, the capability indices of the process are used. (See "Capability Indices for Normal Distributions" for definitions in terms of the theoretical mean and standard deviation.) For sample observations, the following relationships hold:

$$C_{pu} = \frac{\text{USL}_j - \overline{Y}_j}{3SD(Y_j)}$$

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$$C_{pl} = \frac{\overline{Y}_j - LSL_j}{3SD(Y_j)}$$

If a process has two specification limits and a target at the midpoint of the limits, then the (x,y) coordinates for the point on the Goal Plot satisfy these relationships:

$$C_{pu} = (0.5 - x)/3y$$

$$C_{pl} = (0.5 + x)/3y$$

To obtain coordinates when there is only one specification limit and no target, these relationships are used. To identify a unique point requires an assumption about the slope of the line from the origin on which the points fall. A slope of 0.5 is assumed for the case of an upper specification limit and of -0.5 for a lower specification limit. When capability values are equal to one and the Ppk slider for the goal plot triangle is set to 1, these slopes place the points on the goal plot triangle lines.

Consider the case of only an upper specification limit and no target. Using the assumption that the (x,y) coordinates fall on a line from the origin with slope 0.5, solving for x and y gives the following coordinates:

$$x = 1/(3C_{pu} + 2)$$

$$y = 1/(6C_{pu} + 4)$$

Consider the case of only a lower specification limit and no target. Using the assumption that the (x,y) coordinates fall on a line from the origin with slope -0.5, solving for x and y gives the following coordinates:

$$x = -1/(3C_{pl} + 2)$$
  
$$y = 1/(6C_{pl} + 4)$$

**Note:** If either  $C_{pu}$  or  $C_{pl}$  is less than -0.6, then it is set to -0.6 in the formulas above. At the value -2/3, the denominator for x assumes the value 0. Bounding the capability values at -0.6 prevents the denominator from assuming the value 0 or switching signs.

# **Capability Box Plots for Processes with Missing Targets**

A column with no target can have both upper and lower specification limits, or only a single specification limit. This section uses the notation defined in "Notation for Goal Plots and Capability Box Plots".

#### Two Specification Limits and No Target

When no target is specified for the  $j^{th}$  column, the capability box plot is based on the following values for the transformed observations:

$$Z_{ij} = \frac{Y_{ij} - (LSL_j + USL_j)/2}{USL_j - LSL_j}$$

# Single Specification Limit and No Target

Suppose that only the lower specification limit is specified. (The case where only the upper specification limit is specified in a similar way.)

When no target is specified for the *j*<sup>th</sup> column, the capability box plot is based on the following values for the transformed observations:

$$Z_{ij} = \frac{Y_{ij} - \overline{Y}_j}{2(\overline{Y}_j - LSL_j)}$$

**Note:** When a column has only one specification limit and no target value, and the sample mean falls outside the specification interval, no capability box plot for that column is plotted.

# **Capability Indices for Normal Distributions**

This section provides details about the calculation of capability indices for normal data.

For a process characteristic with mean  $\mu$  and standard deviation  $\sigma$ , the population-based capability indices are defined as follows. For sample observations, the parameters are replaced by their estimates:

$$Cp = \frac{USL - LSL}{6\sigma}$$

$$Cpl = \frac{\mu - LSL}{3\sigma}$$

$$Cpu = \frac{USL - \mu}{3\sigma}$$

$$Cpk = min(Cpl, Cpu)$$

$$Cpm = \frac{min(T - LSL, USL - T)}{3\sigma\sqrt{1 + \left(\frac{T - \mu}{\sigma}\right)^2}}$$

Target Index = 3(Cp - Cpk)

The formulas use the following notation:

LSL = Lower specification limit
USL = Upper specification limit

T = Target value

For estimates of Within Sigma capability,  $\sigma$  is estimated using the subgrouping method that you specified. For estimates of Overall Sigma capability,  $\sigma$  is estimated using the sample standard deviation. If either of the specification limits is missing, the capability indices containing the missing specification limit are reported as missing.

**Note:** With the default AIAG (Ppk) Labeling, the indices based on Overall Sigma are denoted by Pp, Ppl, Ppu, and Ppk. The labeling for the index Cpm does not change when Overall Sigma is used. The formulas in this section are defined using Cp labels.

# **Confidence Intervals for Capability Indices**

Confidence intervals for capability indices are available only for processes with normal distributions. Confidence intervals are calculated for both Within and Overall Sigma capability and are shown in the Individuals Detail Reports.

#### Cp

The  $100(1 - \alpha)\%$  confidence interval for Cp is calculated as follows:

$$\left(\hat{Cp}\sqrt{\frac{\chi^{2}_{\alpha/2,df}}{df}},\hat{Cp}\sqrt{\frac{\chi^{2}_{1-\alpha/2,df}}{df}}\right)$$

where

Ĉp is the estimated value for Cp

 $\chi^2_{\alpha/2,\,df}$  is the  $(\alpha/2)^{th}$  quantile of a chi-square distribution with df degrees of freedom

df is the degrees of freedom

*N* is the number of observations

*m* is the number of subgroups

For Overall Sigma capability, the degrees of freedom is equal to N - 1.

For Within Sigma capability, the degrees of freedom depends on the subgrouping and the within sigma estimation method.

- For Within Sigma capability with unbalanced subgroups, the degrees of freedom calculation is the same regardless of the within sigma estimation method. The degrees of freedom is equal to *N m*.
- For Within Sigma capability with balanced subgroups of size n = N/m, the degrees of freedom calculation depends on the within sigma estimation method.
  - When Within Sigma is estimated by the average of the unbiased standard deviations, the degrees of freedom is equal to  $f^*(N-m)$ . The scale factor f, which varies between 0.875 and 1, is defined as follows:

$$f = \frac{1}{2(n-1)\left(\frac{(n-1)}{2}\left(\frac{\Gamma(\frac{n-1}{2})}{\Gamma(\frac{n}{2})}\right)^2 - 1\right)}$$

where  $\Gamma(n)$  is the gamma function evaluated at n.

For more information, see Bissell (1990).

- When Within Sigma is estimated by the average of ranges, the degrees of freedom is calculated as  $df = 1/A - (3/16) * A + (3/64) * A^2 + 0.25$ . A is defined as follows:

Statistical Details for the Process Capability Platform

$$A = \frac{2d_3(n)^2}{m \cdot d_2(n)^2}$$

 $d_2(n)$  is the expected value of the range of n independent normally distributed variables with unit standard deviation

 $d_3(n)$  is the standard deviation of the range of n independent normally distributed variables with unit standard deviation

For more information, see David (1951).

- When Within Sigma is estimated by the unbiased pooled standard deviations, the degrees of freedom is equal to *N* - *m*.
- For Within Sigma capability with no subgroups, the degrees of freedom calculation depends on the within sigma estimation method.
  - When Within Sigma is estimated by the average moving ranges, the degrees of freedom is calculated as 0.62 \* (N 1).
  - When Within Sigma is estimated by the median moving ranges, the degrees of freedom is calculated as 0.32 \* (N 1).

For more information, see Wheeler (2004, p. 82).

# Cpk

The  $100(1 - \alpha)\%$  confidence interval for Cpk is calculated as follows:

$$\left(\hat{C}_{pk}\left[1-\Phi^{-1}_{1-\alpha/2}\sqrt{\frac{1}{9N\hat{C}_{pk}^2}+\frac{1}{2df}}\right],\hat{C}_{pk}\left[1+\Phi^{-1}_{1-\alpha/2}\sqrt{\frac{1}{9N\hat{C}_{pk}^2}+\frac{1}{2df}}\right]\right)$$

where

 $\hat{C}_{pk}$  is the estimated value for Cpk

 $\Phi^{-1}{}_{1-\alpha/2}$  is the (1 -  $\alpha/2)^{th}$  quantile of a standard normal distribution

df is the degrees of freedom

*N* is the number of observations

*m* is the number of subgroups

For Overall Sigma capability, the degrees of freedom is equal to N - 1.

For Within Sigma capability, the degrees of freedom depends on the subgrouping and the within sigma estimation method.

- For Within Sigma capability with unbalanced subgroups, the degrees of freedom calculation is the same regardless of the within sigma estimation method. The degrees of freedom is equal to N - m.
- For Within Sigma capability with balanced subgroups of size n = N/m, the degrees of freedom calculation depends on the within sigma estimation method.
  - When Within Sigma is estimated by the average of the unbiased standard deviations, the degrees of freedom is equal to  $f^*(N-m)$ . The scale factor f, which varies between 0.875 and 1, is defined as follows:

$$f = \frac{1}{2(n-1)\left(\frac{(n-1)}{2}\left(\frac{\Gamma(\frac{n-1}{2})}{\Gamma(\frac{n}{2})}\right)^2 - 1\right)}$$

where  $\Gamma(n)$  is the gamma function evaluated at n.

For more information, see Bissell (1990).

 When Within Sigma is estimated by the average of ranges, the degrees of freedom is calculated as  $df = 1/A - (3/16) * A + (3/64) * A^2 + 0.25$ . A is defined as follows:

$$A = \frac{2d_3(n)^2}{m \cdot d_2(n)^2}$$

 $d_2(n)$  is the expected value of the range of n independent normally distributed variables with unit standard deviation

 $d_3(n)$  is the standard deviation of the range of n independent normally distributed variables with unit standard deviation

For more information, see David (1951).

- When Within Sigma is estimated by the unbiased pooled standard deviations, the degrees of freedom is equal to N - m.
- For Within Sigma capability with no subgroups, the degrees of freedom calculation depends on the within sigma estimation method.
  - When Within Sigma is estimated by the average moving ranges, the degrees of freedom is calculated as 0.62 \* (N - 1).
  - When Within Sigma is estimated by the median moving ranges, the degrees of freedom is calculated as 0.32 \* (N - 1).

For more information, see Wheeler (2004, p. 82).

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**Note:** The confidence interval for Cpm is computed only when the target value is centered between the lower and upper specification limits.

The  $100(1 - \alpha)\%$  confidence interval for Cpm is calculated as follows:

$$\left(\hat{Cpm}\sqrt{\frac{\chi^2_{\alpha/2,\gamma}}{\gamma}},\hat{Cpm}\sqrt{\frac{\chi^2_{1-\alpha/2,\gamma}}{\gamma}}\right)$$

where

Cpm is the estimated value for Cpm

 $\chi^2_{\alpha/2,\gamma}$  is the  $(\alpha/2)^{th}$  quantile of a chi-square distribution with  $\gamma$  degrees of freedom

$$\gamma = \frac{N\left(1 + \left(\frac{\overline{x} - T}{s}\right)^2\right)^2}{1 + 2\left(\frac{\overline{x} - T}{s}\right)^2}$$

*N* is the number of observations

 $\bar{x}$  is the mean of the observations

*T* is the target value

s is the sigma estimate

For Overall Sigma capability, s is the Overall Sigma estimate. For Within Sigma capability, s is replaced by the Within Sigma estimate.

**Tip:** For more information on confidence intervals for Cp, Cpk, and Cpm, see Pearn and Kotz (2006).

#### Cpl and Cpu

Lower and upper confidence limits for Cpl and Cpu are computed using the method of Chou et al. (1990).

The  $100(1 - \alpha)\%$  confidence limits for Cpl (denoted by  $CPL_L$  and  $CPL_U$ ) satisfy the following equations:

$$\Pr[t_{n-1}(\delta_L) \ge 3\hat{C}_{pl}\sqrt{n}] = \alpha/2$$
 where  $\delta_L = 3CPL_L\sqrt{n}$ 

$$\Pr[t_{n-1}(\delta_U) \le 3\hat{C}_{pl}\sqrt{n}] = \alpha/2$$
 where  $\delta_U = 3CPL_U\sqrt{n}$ 

where

 $t_{n-1}(\delta)$  has a non-central t-distribution with n - 1 degrees of freedom and noncentrality parameter  $\delta$ 

 $\hat{C}_{pl}$  is the estimated value for Cpl

The  $100(1 - \alpha)\%$  confidence limits for Cpu (denoted by  $CPU_L$  and  $CPU_U$ ) satisfy the following equations:

$$\Pr[t_{n-1}(\delta_L) \ge 3\hat{C}_{pu}\sqrt{n}] = \alpha/2$$
 where  $\delta_L = 3CPU_L\sqrt{n}$ 

$$\Pr[t_{n-1}(\delta_U) \le 3\hat{C}_{pu}\sqrt{n}] = \alpha/2$$
 where  $\delta_U = 3CPU_U\sqrt{n}$ 

where

 $t_{n-1}(\delta)$  has a non-central t-distribution with n - 1 degrees of freedom and noncentrality parameter  $\delta$ 

 $\hat{C}_{pu}$  is the estimated value for Cpu

# Capability Indices for Nonnormal Distributions: Percentile and Z-Score Methods

This section describes how capability indices are calculated for nonnormal distributions. Two methods are described: the Percentile (also known as ISO/Quantile) method and the Z-Score (also known as Bothe/Z-scores) method. When you select a distribution for a nonnormal process variable, you can fit a parametric distribution or a nonparametric distribution. You can use either the Percentile or the Z-Score methods to calculate capability indices for the process variable of interest. However, unless you have a very large amount of data, a nonparametric fit might not accurately reflect behavior in the tails of the distribution.

**Note:** For both the Percentile and the Z-Score methods, if the data are normally distributed, the capability formulas reduce to the formulas for normality-based capability indices.

The descriptions of the two methods use the following notation:

LSL = Lower specification limit

*USL* = Upper specification limit

T = Target value

#### Percentile (ISO/Quantile) Method

The percentile method replaces the mean in the standard capability formulas with the median of the fitted distribution and the  $6\sigma$  range of values with the corresponding percentile range. The method is described in AIAG (2005).

Denote the  $\alpha$ \*100<sup>th</sup> percentile of the fitted distribution by  $P_{\alpha}$ . Then Percentile method capability indices are defined as follows:

$$P_{pk} = \min\left(\frac{P_{0.5} - LSL}{P_{0.5} - P_{0.00135}}, \frac{USL - P_{0.5}}{P_{0.99865} - P_{0.5}}\right)$$

$$P_{pl} = \frac{P_{0.5} - LSL}{P_{0.5} - P_{0.00135}}$$

$$P_{pu} = \frac{USL - P_{0.5}}{P_{0.99865} - P_{0.5}}$$

$$P_p = \frac{USL - LSL}{P_{0.99865} - P_{0.00135}}$$

$$C_{pm} = \frac{\min(\frac{T - LSL}{P_{0.5} - P_{0.00135}}, \frac{USL - T}{P_{0.99865} - P_{0.5}})}{\sqrt{1 + (\frac{\mu - T}{\sigma})^2}}$$

#### **Z-Score (Bothe/Z-Scores) Method**

The Z-Score method transforms the specification limits to values that have the same probabilities on a standard normal scale. It computes capability measures that correspond to a normal distribution with the same risk levels as the fitted nonnormal distribution.

Let *F* denote the fitted distribution for a process variable with lower and upper specification limits given by LSL and USL. Equivalent standard normal specification limits are defined as follows:

$$\begin{bmatrix} LSL_F = \Phi^{-1}(F(LSL)) \\ USL_F = \Phi^{-1}(F(USL)) \end{bmatrix}$$

Then the Z-Score method capability indices are defined as follows:

$$\begin{split} &P_{pk} = \min(-LSL_F/3, USL_F/3) \\ &P_{pl} = -LSL_F/3 \\ &P_{pu} = USL_F/3 \\ &P_{pu} = (USL_F-LSL_F)/6 \end{split}$$

**Note:** Because Cpm is a target-based measure, it cannot be calculated using the Z-Scores method.

**Note:** For very capable data, F(LSL) or F(USL) can be so close to zero or one, respectively, that  $LSL_F$  or  $USL_F$  cannot be computed. In these cases, JMP automatically switches from the Z-Score method to the Percentile method by default. This gives more meaningful capability indices. To turn off this default setting, select File > Preferences > Platforms > Process Capability.

#### **Parameterizations for Distributions**

This section gives the density functions *f* for the distributions used in the Process Capability platform. It also gives expected values and variances for all but the Johnson and SHASH distributions.

#### Normal

$$f(x|\mu,\sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left[-\frac{1}{2\sigma^2}(x-\mu)^2\right], \quad -\infty < x < \infty, \quad -\infty < \mu < \infty, \quad \sigma > 0$$

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$$E(X) = \mu$$
$$Var(X) = \sigma^2$$

Beta

$$f(x|\alpha,\beta) = \frac{1}{B(\alpha,\beta)} x^{\alpha-1} (1-x)^{\beta-1} , \quad 0 \le x \le 1 , \quad \alpha > 0 , \quad \beta > 0$$

$$E(X) = \frac{\alpha}{\alpha+\beta}$$

$$Var(X) = \frac{\alpha\beta}{(\alpha+\beta)^2(\alpha+\beta+1)}$$

where  $B(\cdot)$  is the Beta function.

#### **Exponential**

$$f(x|\sigma) = \frac{1}{\sigma} \exp(-x/\sigma) , x > 0 , \sigma > 0$$

$$E(X) = \sigma$$

$$Var(X) = \sigma^{2}$$

#### Gamma

$$f(x|\alpha,\sigma) = \frac{1}{\Gamma(\alpha)\sigma^{\alpha}} x^{\alpha-1} \exp(-x/\sigma) , x>0 , \alpha>0 , \sigma>0$$
 
$$E(X) = \alpha\sigma$$
 
$$Var(X) = \alpha\sigma^2$$

where  $\Gamma(\cdot)$  is the gamma function.

#### **Johnson**

Johnson Su

$$f(x|\gamma, \delta, \sigma, \theta) = \frac{\delta}{\sigma} \left[ 1 + \left( \frac{x - \theta}{\sigma} \right)^2 \right]^{-1/2} \phi \left[ \gamma + \delta \sinh^{-1} \left( \frac{x - \theta}{\sigma} \right) \right], \quad -\infty < x, \theta, \gamma < \infty \quad , \quad \theta > 0 \quad , \delta > 0$$

Johnson Sb

$$f(x|\gamma, \delta, \sigma, \theta) = \phi \left[ \gamma + \delta \ln \left( \frac{x - \theta}{\sigma - (x - \theta)} \right) \right] \left( \frac{\delta \sigma}{(x - \theta)(\sigma - (x - \theta))} \right) , \quad \theta < x < \theta + \sigma \quad , \quad \sigma > 0$$

Johnson SI

$$f(x|\gamma, \delta, \sigma, \theta) = \frac{\delta}{|x-\theta|} \phi \left[ \gamma + \delta \ln\left(\frac{x-\theta}{\sigma}\right) \right], \quad x > 0 \text{ if } \sigma = 1, \quad x < 0 \text{ if } \sigma = -1$$

where  $\phi(\cdot)$  is the standard normal probability density function.

#### Lognormal

$$f(x|\mu,\sigma) = \frac{1}{\sigma\sqrt{2\pi}} \frac{\exp\left[\frac{-(\log(x) - \mu)^2}{2\sigma^2}\right]}{x} , \quad x > 0 , \quad -\infty < \mu < \infty , \quad \sigma > 0$$

$$E(X) = \exp(\mu + \sigma^2/2)$$

$$Var(X) = \exp(2(\mu + \sigma^2)) - \exp(2\mu + \sigma^2)$$

#### Mixture of Normals

The Mixture of 2 Normals and Mixture of 3 Normals options for Distribution share the following parameterization:

$$f(x|\mu_i, \sigma_i, \pi_i) = \sum_{i=1}^k \frac{\pi_i}{\sigma_i} \phi\left(\frac{x - \mu_i}{\sigma_i}\right)$$

$$E(X) = \sum_{i=1}^{k} \pi_i \mu_i$$

$$Var(X) = \sum_{i=1}^{k} \pi_{i}(\mu_{i}^{2} + \sigma_{i}^{2}) - \left(\sum_{i=1}^{k} \pi_{i}\mu_{i}\right)^{2}$$

where  $\mu_i$ ,  $\sigma_i$ , and  $\pi_i$  are the respective mean, standard deviation, and proportion for the  $i^{th}$  group, and  $\phi(\cdot)$  is the standard normal probability density function. For the Mixture of 2 Normals, k is equal to 2. For the Mixture of 3 Normals distribution, k is equal to 3. A separate mean, standard deviation, and proportion of the whole is estimated for each group in the mixture.

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#### **SHASH**

$$f(x|\gamma, \delta, \sigma, \theta) = \frac{\delta \cosh(w)}{\sqrt{\sigma^2 + (x - \theta)^2}} \phi[\sinh(w)], -\infty < \gamma, x, \theta < \infty, 0 < \delta, 0 < \sigma$$

where

 $\phi(\cdot)$  is the standard normal pdf

$$w = \gamma + \delta \sinh^{-1} \left( \frac{x - \theta}{\sigma} \right)$$

**Note:** When  $\gamma = 0$  and  $\delta = 1$ , the SHASH distribution is equivalent to the normal distribution with location  $\theta$  and scale  $\sigma$ .

#### Weibull

$$f(x|\alpha, \beta) = \frac{\beta}{\alpha\beta}x^{\beta-1}\exp\left[-\left(\frac{x}{\alpha}\right)^{\beta}\right], \quad \alpha > 0, \quad \beta > 0$$

$$E(X) = \alpha \Gamma \left( 1 + \frac{1}{\beta} \right)$$

$$Var(X) = \alpha^{2} \left\{ \Gamma\left(1 + \frac{2}{\beta}\right) - \Gamma^{2}\left(1 + \frac{1}{\beta}\right) \right\}$$

where  $\Gamma(\cdot)$  is the gamma function.

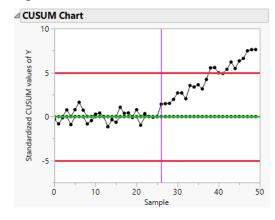
# **CUSUM Control Charts**

#### **Create Tabular CUSUM Control Charts with Decision Limits**

Cumulative Sum (CUSUM) control charts enable you to detect small shifts in a process. They are useful in detecting shifts that occur over time, such as a gradual drift, and that are not necessarily accompanied by a sudden shift. The CUSUM Control Chart platform creates a CUSUM chart with decision limits, similar to a Shewhart chart. This chart is also called a *tabular CUSUM chart*. To create a V-mask cumulative sum control chart, see "V-Mask CUSUM Control Charts".

The CUSUM Control Chart platform also provides information about average run length (ARL). The *average run length* is the average number of samples or observations that can be expected to occur before an out-of-control signal occurs. You can use the average run length to assess the performance of a CUSUM chart, given specific parameters and assuming constant variance.

Figure 8.1 CUSUM Control Chart



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# Overview of the CUSUM Control Chart Platform

A tabular CUSUM chart consists of two one-sided decision limits charts superimposed on one chart. The chart contains decision limits that signal when the process is out of control and places a shift line on the chart where the shift is suspected to have occurred. To use the CUSUM Control Chart platform, you must determine the smallest change in the mean that you consider important. You can view the CUSUM control chart in standard deviation units or in data units. For more information about tabular CUSUM charts, see Woodall and Adams (1998) and Montgomery (2013).

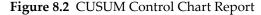
Another form of a cumulative sum control chart is the V-mask chart. To create a V-mask CUSUM chart, see "V-Mask CUSUM Control Charts".

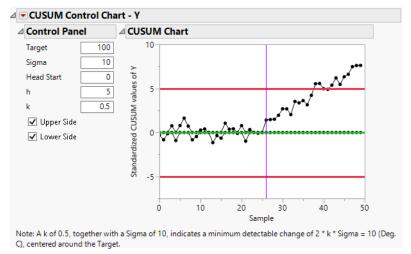
**Note:** The summary results in the CUSUM Control Chart platform do not always match the summary results in the V-mask CUSUM platform. Specifically, the summary results for a two-sided V-mask CUSUM chart do not match those from a CUSUM Control Chart with both Upper Side and Lower Side options selected. However, the one-sided summary reports from the CUSUM Control Chart platform and the V-mask CUSUM platform do match.

# **Example of CUSUM Control Chart**

You want to detect small shifts in the temperature of an engine. The data table contains temperature measurements from the engine thermostat.

- Select Help > Sample Data Library and open Quality Control/Engine Temperature Sensor.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > CUSUM Control Chart.
- Select Y and click Y.
- 4. Click **OK**.
- 5. In the Target box, type 100.
- 6. In the Sigma box, type 10.





The vertical line on the CUSUM Chart indicates that a shift in the temperature measurements started around sample 26.

**Note:** You can compare this result to the Individual Moving Range control chart by running the IMR Chart table script in Engine Temperature Sensor.jmp. The IMR chart does not trigger any of the Nelson tests.

#### **Example of a One-Sided CUSUM Control Chart**

Continuing the previous example, suppose that you care only about increasing temperature changes. To change the CUSUM control chart in Figure 8.2 to a one-sided chart, deselect the Lower Side check box. When you do that, the points for the negative cumulative sums are removed from the chart. You are left with a CUSUM control chart that contains only the positive cumulative sum points.

C), centered around the Target.

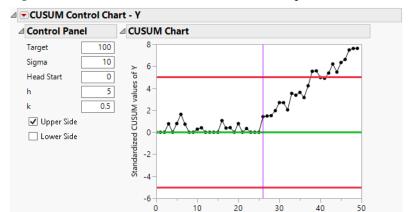


Figure 8.3 One-Sided CUSUM Control Chart Report

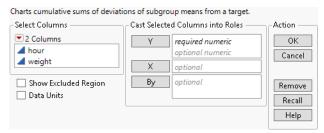
# **Launch the CUSUM Control Chart Platform**

Note: A k of 0.5, together with a Sigma of 10, indicates a minimum detectable change of 2 \* k \* Sigma = 10 (Deg.

Launch the CUSUM Control Chart platform by selecting **Analyze > Quality and Process > Control Chart > CUSUM Control Chart**.

Sample

Figure 8.4 The CUSUM Control Chart Launch Window



For more information about the options in the Select Columns red triangle menu, see *Using JMP*.

The CUSUM Control Chart platform launch window contains the following options:

**Y** Identifies the variables that you want to chart.

**Note:** The rows of the data table must be sorted in the order in which the observations were collected.

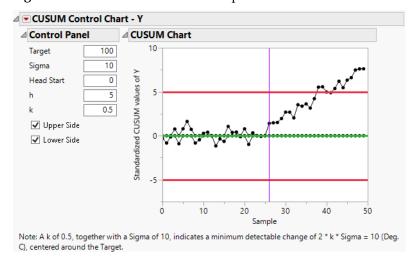
- **X** Identifies a subgroup variable. The horizontal axis of the CUSUM chart is labeled by the subgroup variable. If a value of this column is present more than once, the average response at each X value is plotted on the CUSUM chart.
- **By** Produces a separate report for each level of the By variable. If more than one By variable is assigned, a separate report is produced for each possible combination of the levels of the By variables.
- **Show Excluded Region** (Applicable only when an X variable is specified.) Specifies that subgroups that are entirely excluded are shown on the horizontal axis in the CUSUM control chart.
- **Data Units** Specifies that data units be used in the report rather than standard deviation units. By default, the chart and parameters are shown in standard deviation units. However, if you select the Data Units option in the launch window, the chart and parameters are shown in the units of the data column that is being analyzed.

When you use standard deviation units, values for the h and k parameters do not depend on the process standard deviation. This can be an advantage.

# The CUSUM Control Chart Platform Report

By default, the CUSUM Control Chart platform produces a report that contains a parameter control panel and a CUSUM chart.

Figure 8.5 CUSUM Control Chart Report



**CUSUM Control Charts** 

#### Control Panel for CUSUM Control Chart

The Control Panel report contains the current values for the chart parameters. The current values are in boxes that enable you to update the parameter values. There are also boxes for Upper Side and Lower Side. If you have specified the Data Units option in the launch window, this setting is denoted in the Control Panel below the check boxes.

The following options appear in the Control Panel report:

**Target** The known value of the mean. This is the value of the center line in the chart. By default, this parameter is set to the Target value in the Spec Limits column property for the Y column. If the Y column does not have a Target value in the Spec Limits column property, this parameter is set to the overall average of the Y column.

**Note:** To use the overall average of the Y column as the value of the center line even if the Y column has a Target value in the Spec Limits column property, select the Use Process Mean for Center Line platform preference. This preference is located in File > Preferences > Platforms > CUSUM Control Chart.

- **Sigma** The known value of the standard deviation. By default, this parameter is set to the average moving range of the Y column. If there is an X variable, the Sigma parameter is set to the average moving range of the summary data.
- **Head Start** The value of the cumulative sums before the first sample. Starting the cumulative sums at a nonzero value increases the sensitivity of the CUSUM chart near the beginning of the samples. This parameter is also known as the fast initial response (FIR) value. By default, this parameter is set to 0.
- **h or H** The value of the parameter that defines the limits. If the Data Units option was not selected in the launch window, this is the h parameter. If the Data Units option was selected in the launch window, this is the H parameter. Note that H is equal to h times Sigma. By default, h is equal to 5 and H is equal to 5 times Sigma.
- **k or K** The value of the parameter that defines the smallest change in the mean that is valuable to detect. If the Data Units option was not selected in the launch window, this is the k parameter. If the Data Units option was selected in the launch window, this is the K parameter. Note that K is equal to k times Sigma. By default, k is equal to 0.5 and K is equal to one half of Sigma.
- **Upper Side** Shows or hides the positive values for the cumulative sum on the chart. These values are the  $C^+$  values.
- **Lower Side** Shows or hides the negative values for the cumulative sum on the chart. These values are the  $C^-$  values.

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**Using Data Units** The presence of this text indicates that the Data Units option was selected in the launch window and that the values in the CUSUM chart are centered but not standardized.

#### **CUSUM Chart**

The CUSUM Chart report contains the cumulative sum control chart with decision limits that are determined by the current values of the chart parameters. The samples (or subgroups if you specified an X variable) are denoted on the horizontal axis. The vertical axis denotes centered values of the positive and negative values for the cumulative sum. If the Data Units option was not selected in the launch window, the vertical axis denotes cumulative sums for standardized response values. If the Data Units option was selected in the launch window, the vertical axis denotes cumulative sums for unstandardized response values.

# **CUSUM Control Chart Platform Options**

The CUSUM Control Chart red triangle menu contains the following options:

**Show Limits** Shows or hides the upper and lower decision limits in the CUSUM Chart.

**Show Center Line** Shows or hides the center line in the CUSUM Chart.

**Show Shift Lines** (Available only when there is a shift detected in the data.) Shows or hides the vertical lines in the CUSUM Chart that designate shifts. Shift lines are drawn at the start of a shift.

- A positive shift occurs when the value of  $C^+$  exceeds the upper limit on the chart. The start of the shift is defined as the first point after the most recent zero value for  $C^+$ .
- A negative shift occurs when the value of C falls below the lower limit on the chart.
   The start of the shift is defined as the first point after the most recent zero value for C.

**Show ARL** Shows or hides the Average Run Length (ARL) report. See "Average Run Length (ARL) Report".

**ARL Profiler** Shows or hides a profiler of average run length versus the parameters h and k. If you have specified the Data Units option in the launch window, the profiler plots average run length versus the parameters H and K.

The average run length (ARL) for a specified shift is the average number of runs expected before an out-of-control signal occurs. For example, the ARL at 0 represents the average

number of runs expected before a false-alarm signal occurs when the process is in control. When the process is in control, the shift size is 0.

The ARL Profiler enables you to explore how various settings of the parameters affect the performance of the corresponding CUSUM chart. As the parameters in the Control Panel report are updated, the ARL Profiler is updated as well. An ideal CUSUM chart has a high ARL(0) value and a low ARL( $\Delta$ ) value, where  $\Delta$  is the size shift that is of interest.

The ARL Profiler depends on the settings of the Upper Side and Lower Side options in the Control Panel report:

- If both the Upper Side and Lower Side options are selected, the profiler represents the average run length for crossing either the upper or lower decision limits on the CUSUM chart.
- If only the Upper Side option is selected, the profiler represents the average run length for the upper decision limit on the CUSUM chart.
- If only the Lower Side option is selected, the profiler represents the average run length for the lower decision limit on the CUSUM chart.

For more information about the options in the red triangle menu next to ARL Profiler, see Profilers.

**Control Panel** Shows or hides a report of the current values of the parameters. This report enables you to change the parameter values as well as the sidedness of the CUSUM chart.

**Parameters Report** Shows or hides a report of the current values of the parameters.

**Test Beyond Limits** Shows or hides a red circle around any point that is above the upper limit or below the lower limit in the CUSUM chart.

**Save Summaries** Creates a new data table that contains statistics for each subgroup in the CUSUM chart. The following statistics are saved to the new data table: the subgroup number and size, the subgroup sample mean, an indicator of shift starts, a value that indicates each interval between shift starts, the upper and lower cumulative sums and corresponding consecutive run counts, and the LCL and UCL values.

**Tune Chart** Shows or hides a control that enables you to set an acceptable range for the Y variable. Adjust the minimum and maximum values of the acceptable range and click **Done**. At this point, the CUSUM chart updates based on a new value of the k parameter.

 If you specified the Data Units option in the launch window, the imputed k parameter is the average of the minimum and maximum values.

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 If the Data Units option is not specified, the imputed K parameter is the average of the minimum and maximum values divided by the Sigma parameter.

Setting the acceptable range for the Y variable enables you to set the practical significance of the CUSUM chart. This is particularly helpful when the testing interval is more frequent, which can result in a much shorter practical average run length.

**Reset to Defaults** Resets all parameters back to their default values.

**Alarm Script** Enables you to write and run a script that indicates when the data fail special causes tests. Results can be written to a file, written to the log or sent in an email. There is an option to include an explanation of why the test failed.

As an Alarm Script is invoked, the following variables are available, both in the issued script and in subsequent JSL scripts:

qc\_col is the name of the column

qc\_test is the test that failed

qc\_sample is the sample number

**Tip:** After an alarm script is specified, the alarm script is invoked when the Test Beyond Limits option is turned on.

See the Scripting Guide for more information about writing custom Alarm Scripts.

See *Using JMP* for more information about the following options:

**Redo** Contains options that enable you to repeat or relaunch the analysis. In platforms that support the feature, the Automatic Recalc option immediately reflects the changes that you make to the data table in the corresponding report window.

**Save Script** Contains options that enable you to save a script that reproduces the report to several destinations.

**Save By-Group Script** Contains options that enable you to save a script that reproduces the platform report for all levels of a By variable to several destinations. Available only when a By variable is specified in the launch window.

# Average Run Length (ARL) Report

The Average Run Length (ARL) report contains a table and a graph of ARL values. The average run length (ARL) for a specified shift is the average number of runs expected before an out-of-control signal occurs. For example, the ARL at 0 represents the average number of runs expected before seeing a false-alarm signal when the process is in control. When the process is in control, the shift size is 0.

**CUSUM Control Charts** 

The table and graph in the ARL report enable you to explore how various settings of the parameters affect the performance of the corresponding CUSUM chart. As the h and k parameters in the Control Panel report are updated, the ARL report is updated as well. An ideal CUSUM chart has a high ARL(0) value and a low ARL( $\Delta$ ) value, where  $\Delta$  is the size shift that is of interest.

The Average Run Length (ARL) report depends on the settings of the Upper Side and Lower Side options in the Control Panel report. If only one option is selected, the ARL report uses calculations for the corresponding one-sided CUSUM chart. If both options are selected, the ARL report uses calculations for the two-sided CUSUM chart. Note that the two-sided ARL values are related to the positive and negative one-sided ARL values by the following equation:

$$\frac{1}{ARL} = \frac{1}{Positive ARL} + \frac{1}{Negative ARL}$$

#### **ARL Table**

The ARL Table shows the average run length for shifts ( $\Delta$ ) between zero and three at 0.25 increments. If the Data Units option is specified, the shift is represented by 2\*K/Sigma<sup>2</sup>. If the Data Units option is not specified, the shift is represented by 2\*k/Sigma.

## ARL Graph

The ARL Graph shows the average run length for shifts ( $\Delta$ ) between 0 and 3. This graph contains the same data points as the ARL Table to the left of the ARL Graph.

# Additional Examples of CUSUM Control Charts

- "Example of the Data Units Option in a CUSUM Control Chart"
- "Example of CUSUM Chart with Subgroups"

# **Example of the Data Units Option in a CUSUM Control Chart**

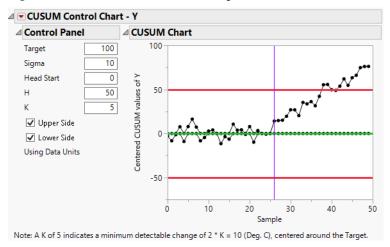
This example uses the Data Units option and reproduces the analysis in "Example of CUSUM Control Chart". You want to detect small shifts in the temperature of an engine. The data table contains temperature measurements from the engine thermostat.

- Select Help > Sample Data Library and open Quality Control/Engine Temperature Sensor.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > CUSUM Control Chart.

- 3. Select Y and click Y.
- 4. Select the box next to Data Units.
- Click **OK**.
- 6. In the Target box, type 100.
- 7. In the Sigma box, type 10.

Note that the options below Head Start are H and K, instead of h and k. These parameters are now specified in units of the data column, rather than in standard deviation units.

Figure 8.6 CUSUM Control Chart Report



Like in the example using sigma units, the vertical line on the CUSUM Chart indicates that a shift in the temperature measurements started around sample 26.

# **Example of CUSUM Chart with Subgroups**

A machine fills 8-ounce cans of two-cycle engine oil additive. The filling process is believed to be in statistical control. The process is set so that the average weight of a filled can ( $\mu_0$ ) is 8.10 ounces. Previous analysis shows that the standard deviation of fill weights ( $\sigma_0$ ) is 0.05 ounces.

Subgroup samples of four cans are selected and weighed every hour for twelve hours. Each observation in the Oil1 Cusum.jmp data table contains one value of weight and its associated value of hour. The observations are sorted so that the values of hour are in increasing order. You want to be able to detect a  $2\sigma$  shift in the process.

- 1. Select Help > Sample Data Library and open Quality Control/Oil1 Cusum.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > CUSUM Control Chart.
- Select weight and click Y.

- Select hour and click X.
- Click OK.
- 6. In the Target box, type 8.1.

This is the target mean for the process.

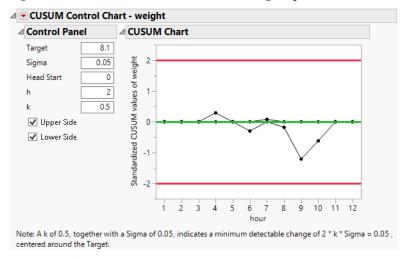
7. In the Sigma box, type 0.05.

This is the known standard deviation for the process.

8. In the h box, type 2.

This defines the decision limits to be 2 standard deviations in each direction.

Figure 8.7 CUSUM Control Chart with Subgroups



The CUSUM Chart does not show any points outside of the upper or lower decision limits. There is no evidence that a shift in the process has occurred.

**Note:** Montgomery (2013) states that "only if there is some significant economy of scale or some other valid reason for taking samples of size greater than one should subgroups of size greater than one be used with the CUSUM." The use of rational subgroups in the tabular CUSUM chart does not always improve the performance of the chart.

# Statistical Details for the CUSUM Control Chart Platform

- "Statistical Details for CUSUM Control Chart Construction"
- "Statistical Details for Shift Detection"
- "Statistical Details for Average Run Length"

#### Statistical Details for CUSUM Control Chart Construction

This section defines the statistics that are used in the construction of the CUSUM Chart. Some of these statistics are also saved in the data table that is created by the Save Summaries command.

#### One-Sided Upper and Lower Cumulative Sums

The definitions of  $C^+$  and  $C^-$  depend on the setting of the Data Units option.

**Note:** In the Save Summaries data table,  $C^+$  and  $C^-$  are labeled Upper Cumulative Sum and Lower Cumulative Sum, respectively.

#### **Cumulative Sums in Standardized Units**

If the Data Units option is not selected,  $C^+$  and  $C^-$  for each step are defined as follows:

$$C_{i}^{+} = \max(0, \frac{x_{i} - T}{\sigma} - k + C_{i-1}^{+})$$

$$C_{i} = \min\left(0, \frac{x_{i} - T}{\sigma} + k + C_{i-1}\right)$$

where:

 $x_i$  is the value of the response at the  $i^{th}$  step

*T* is the target of the process

 $\sigma$  is the standard deviation of the process

*k* is the reference value, in units of standard deviations

If a value is specified for Head Start, that value is used as the initial  $C^+$  value and the negative of that value is used as the initial  $C^-$  value. Otherwise, the initial values of  $C^+$  and  $C^-$  are zero.

**CUSUM Control Charts** 

#### **Cumulative Sums in Data Units**

If the Data Units option is selected,  $C^+$  and  $C^-$  for each step are defined as follows:

$$C_i^+ = \max(0, (x_i - T) - K + C_{i-1}^+)$$

$$C_i = \min(0, (x_i - T) + K + C_{i-1})$$

where:

 $x_i$  is the value of the response at the  $i^{th}$  step

*T* is the target of the process

 $\sigma$  is the standard deviation of the process

*K* is the reference value, in units of the data

If a value is specified for Head Start, that value is used as the initial  $C^+$  value and the negative of that value is used as the initial  $C^-$  value. Otherwise, the initial values of  $C^+$  and  $C^-$  are zero.

#### **Counters for Positive and Negative Runs**

 $N^+$  at each step is the number of steps since the most recent zero value for  $C^+$ .  $N^-$  at each step is the number of steps since the most recent zero value for  $C^-$ .

**Note:** In the Save Summaries data table,  $N^+$  and  $N^-$  are labeled Positive Runs and Negative Runs, respectively.

## Statistical Details for Shift Detection

A positive shift occurs when the value of  $C^+$  exceeds the upper limit on the chart. The start of the shift is defined as the first point after the most recent zero value for  $C^+$ .

A negative shift occurs when the value of  $C^-$  exceeds the lower limit on the chart. The start of the shift is defined as the first point after the most recent zero value for  $C^-$ .

# Statistical Details for Average Run Length

The one-sided average run length (ARL) values are calculated using the integral equation method (with 24 Gaussian points) described by Goel and Wu (1971). If the Head Start value is greater than 0, the values are calculated according to the method in Appendix A.1 of Lucas and Crosier (1982).

Note that the two-sided ARL values are related to the positive and negative one-sided ARL values by the following equation:

$$\frac{1}{ARL} = \frac{1}{Positive ARL} + \frac{1}{Negative ARL}$$

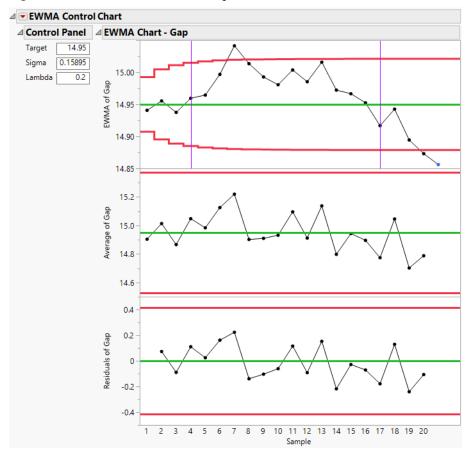
Lucas and Crosier (1982) describe the properties of a Head Start value for CUSUM charts in which the initial CUSUM  $S_0$  is set to a nonzero value. This is sometimes referred to as a fast initial response (FIR) feature. Average run length calculations given by them show that the FIR feature has little effect when the process is in control and that it leads to a faster response to an initial out-of-control condition than a standard CUSUM chart.

# **EWMA Control Charts**

## **Create Exponentially Weighted Control Charts**

Exponentially weighted moving average (EWMA) charts can be used to detect small shifts in a process. Each point on an EWMA chart is the weighted average of all the previous subgroup means, including the mean of the present subgroup sample. The weights decrease exponentially going backward in time.

Figure 9.1 EWMA Control Chart Report



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# Overview of the EWMA Control Chart Platform

Exponentially weighted moving average (EWMA) charts can be used to detect small shifts in a process. Each point on an EWMA chart is the weighted average of all the previous subgroup means, including the mean of the present subgroup sample. The weights decrease exponentially going backward in time. For more information about exponentially weighted moving average charts, see Box et al. (2009) and Montgomery (2013).

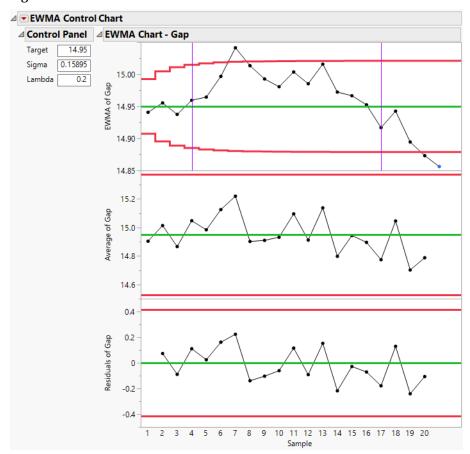
The EWMA Control Chart platform pairs an EWMA chart with an X chart and a residual chart. If you do not specify a Subgroup variable, the X chart is an individual measurements chart. If you specify a Subgroup variable and at least one subgroup size is greater than 1, the X chart is an XBar chart.

# **Example of the EWMA Control Chart Platform**

In the sample data table Clips1.jmp, the measure of interest is the gap between the ends of manufactured metal clips. To monitor the process for a change in the average gap, subgroup samples of five clips have been measured daily.

- 1. Select **Help > Sample Data Library** and open Quality Control/Clips1.jmp.
- Select Analyze > Quality and Process > Control Chart > EWMA Control Chart.
- 3. Select Gap and click Y.
- 4. Select Sample and click **Subgroup**.
- Click **OK**.

Figure 9.2 EWMA Control Chart

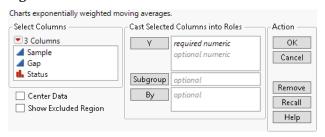


Purple vertical lines in the EWMA chart denote shifts. Shift starts are detected at samples 4 and 17.

# Launch the EWMA Control Chart Platform

Launch the EWMA Control Chart platform by selecting **Analyze > Quality and Process > Control Chart > EWMA Control Chart.** 

Figure 9.3 EWMA Control Chart Launch Window



For more information about the options in the Select Columns red triangle menu, see *Using JMP*.

The EWMA Control Chart platform launch window contains the following options:

**Y** Identifies the variables that you want to chart.

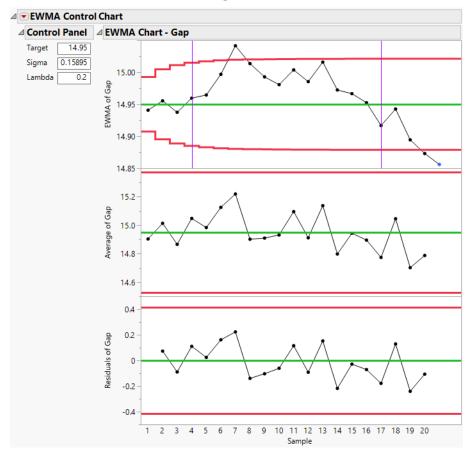
**Note:** If you do not specify a Subgroup variable, the rows of the data table must be sorted in the order in which the observations were collected.

- **Subgroup** Identifies a subgroup variable. The horizontal axis of the EWMA chart is labeled by the subgroup variable.
- **By** Produces a separate report for each level of the By variable. If more than one By variable is assigned, a separate report is produced for each possible combination of the levels of the By variables.
- **Center Data** Specifies that the data are centered by subtracting the target from each observation.
- **Show Excluded Region** (Applicable only when a Subgroup variable is specified.) Specifies that subgroups that are entirely excluded in the data table are shown in the EWMA control chart.

# The EWMA Control Chart Platform Report

By default, the EWMA Control Chart platform produces a report that contains a parameter control panel, an EWMA chart, an X chart, and a residuals chart.

Figure 9.4 EWMA Control Chart Report



## **Control Panel for EWMA Control Chart**

The Control Panel contains the current values for the chart parameters. The current values are in boxes that enable you to update the parameter values.

**EWMA Control Charts** 

The following options appear in the Control Panel:

**Target** The known value of the mean. This is the value of the center line in the chart. By default, this parameter is set to the Target value in the Spec Limits column property for the Y column. If the Y column does not have a Target value in the Spec Limits column property, this parameter is set to the overall average of the Y column.

The Target value cannot be edited in these situations:

- If you specified the Center Data option in the launch window.
- If the Y variable has a Spec Limits column property that contains a value for Target.
   However, you can select the Use Overall Mean for Target option in the red triangle menu to switch between the Target value in the Spec Limits column property and the overall mean of the Y variable.

**Sigma** The known value of the standard deviation. By default, this parameter is set to the average moving range of the Y column. If there is a Subgroup variable, the Sigma parameter is set to the average of the moving ranges of the subgroup means.

**Note:** The default Sigma value calculation does not include excluded rows.

**Lambda** The value of the smoothing constant for weighting prior samples. By default, this parameter is set to 0.2.

\*Using Centered Data The presence of this text indicates that the Centered Data option was selected in the launch window and that the values in the EWMA chart and X chart are centered around the Target value.

## **EWMA Chart Report**

The EWMA Chart report contains three charts: an EWMA chart, an X chart, and a residuals chart. For more information about the interpretation of these charts, see Box et al. (2009).

#### **EWMA Chart**

The EWMA chart is an exponentially weighted moving average (EWMA) chart with decision limits that are determined by the current values of the chart parameters:

- If you specified a Subgroup variable and at least one subgroup size is greater than 1, the horizontal axis denotes the subgroups.
- Otherwise, the horizontal axis denotes the samples.

In both cases, the vertical axis denotes the exponentially weighted moving average. If you specified the Center Data option in the launch window, the vertical axis denotes the exponentially weighted moving average with the target value subtracted from it. Each sample or subgroup has a single point on the chart. There is one additional point that is a forecast point, which is shown in blue.

**Note:** If the last sample (or subgroup) is both hidden and excluded, the line connecting the last sample (or subgroup) to the forecast point is not drawn.

#### X Chart

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The X chart is a Shewhart control chart of the observations:

- If you specified a Subgroup variable and at least one subgroup size is greater than 1, the X chart is an XBar chart of the mean values. The horizontal axis denotes the subgroups. The vertical axis denotes the subgroup means. If you selected the Center Data option in the launch window, the vertical axis denotes the subgroup means with the target value subtracted from them. Each subgroup has a single point on the chart.
- Otherwise, the X chart is an individual measurements chart of the values. The horizontal axis denotes the samples. The vertical axis denotes the measurements. If you selected the Center Data option in the launch window, the vertical axis denotes the measurements with the target value subtracted from them. Each sample has a single point on the chart.

For more information about the limits on the X chart, see "Statistical Details for Control Chart Builder".

#### Residuals Chart

The residuals chart enables you to visually check for autocorrelation:

- If you specified a Subgroup variable and at least one subgroup size is greater than 1, the residuals chart is a chart of the differences between each subgroup mean and the EWMA value for the previous subgroup. The  $i^{th}$  residual is calculated as  $r_i = X_i EWMA_{i-1}$  where  $X_i$  denotes the  $i^{th}$  subgroup mean and  $EWMA_{i-1}$  denotes the  $(i-1)^{th}$  EWMA value.
- Otherwise, the residuals chart is a chart of the differences between each sample value and the EWMA value for the previous sample. The  $i^{th}$  residual is calculated as  $r_i = X_i EWMA_{i-1}$  where  $X_i$  denotes the  $i^{th}$  sample value and  $EWMA_{i-1}$  denotes the  $(i-1)^{th}$  EWMA value.

The limits on the residuals chart are  $\pm 3*ResidSigma$ , where ResidSigma is the standard deviation of the residuals.

# The EWMA Control Chart Platform Options

The EWMA Control Chart red triangle menu contains the following options:

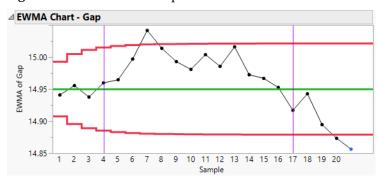
**Show Limits** Shows or hides the upper and lower decision limits in the EWMA chart, X chart, and residuals chart.

**Show Center Line** Shows or hides the center line in the EWMA chart, X chart, and residuals chart.

**Show Shift Lines** Shows or hides the vertical lines in the EWMA chart that designate shifts. Shift lines are drawn at the start of a shift. A shift start is defined as the first point after the EWMA value crosses the center line in a particular direction.

- A positive shift occurs when the EWMA value exceeds the upper limit on the chart. The start of the shift is defined as the first point after the most recent EWMA value below the Target line.
- A negative shift occurs when the EWMA value falls below the lower limit on the chart. The start of the shift is defined as the first point after the most recent EWMA value above the Target line.

Figure 9.5 Shift Lines Example



In this example, the point for sample 7 is above the upper limit. Looking back from sample 7, the most recent point below the Target line is sample 3. Therefore, sample 4 is the first point above the Target line since the most recent point below the Target line and is denoted as the start of the positive shift.

Similarly, the point for sample 20 is below the lower limit and the most recent point above the Target line is sample 16. Therefore, sample 17 is denoted as the start of the negative shift.

**Test Beyond Limits** Shows or hides a red circle around any point that is above the upper limit or below the lower limit in the EWMA and X charts.

**Show ARL** Shows or hides the Average Run Length (ARL) report. See "Average Run Length (ARL) Report for EWMA Control Charts".

**Control Panel** Shows or hides a report of the current values of the parameters. This report enables you to change the parameter values in the EWMA chart.

**Parameters Report** Shows or hides a report of the current values of the parameters.

**Constant Limits** Specifies that the EWMA chart limits are calculated using an asymptotic expression so that the limits on the EWMA chart are constant.

**Caution:** The Constant Limits option has no effect when the sample sizes are not equal across subgroups.

**Save Summaries** Creates a new data table that contains statistics for each subgroup in the EWMA chart. The following statistics are saved to the new data table: the subgroup number, the subgroup label, the subgroup size, the subgroup mean, an indicator of shift starts, a value that indicates each interval between shift starts, the exponentially weighted moving average of each subgroup, the number of positive and negative consecutive run counts, the LCL and UCL values, and test failure indicators. The forecast value is saved in the last row of the summary table.

**Reset to Defaults** Resets all parameters to their default values. If a Lambda value has been specified in the Lambda platform preference, the Lambda value is reset to the value that is specified in the platform preference.

**Note:** When the *Y* variable has a Spec Limits column property that contains a value for Target, the Reset to Defaults option sets the Target to the Target value in the Spec Limits column property.

**Restart EWMA After Empty Subgroup** Specifies how calculations for the moving average and limits are handled when there are empty subgroups. A subgroup can be empty if all the observations for the subgroup are missing values or are in excluded rows. If this option is selected, the calculations restart in the first nonmissing subgroup that follows an empty subgroup. The restart of the calculations resets the moving average to the overall mean. If this option is not selected, the EWMA calculations continue with the most recent nonmissing subgroup moving average.

**Use Overall Mean for Target** (Available only when the *Y* variable has a Spec Limits column property that contains a value for Target.) Sets the Target in the EWMA chart to the overall mean of the *Y* variable. If this option is not selected, the Target in the EWMA chart is set to the Target value in the Spec Limits column property.

**Overlay Charts** Specifies whether the individual location values are overlaid on the EWMA chart. When this option is selected, the Location chart is no longer shown. Instead, the

**EWMA Control Charts** 

points from the Location chart appear on the EWMA chart as unconnected gray Xs. The limits from the Location chart do not appear on the EWMA chart, unless the Show X Limits on Overlay Charts option is selected.

**Show X Limits on Overlay Charts** (Available only when the Overlay Charts option is selected.) Shows or hides the limits from the Location chart on the EWMA chart when the Overlay Charts option is selected. When the Location chart limits are shown on the EWMA chart, they appear as dashed lines.

**Note:** The Test Beyond Limits option is applied to the Location chart values in the Overlay Chart only when the Show X Limits on Overlay Charts option is selected.

**Lambda Slider** Shows or hides a slider control that enables you to change the value of the Lambda parameter interactively.

**Show X Chart** Shows or hides the Location chart below the EWMA chart.

**Note:** When the Overlay Charts option is selected, the Show X Chart option shows or hides the individual location values and limits that are overlaid on the EWMA chart.

**Show Residuals Chart** Shows or hides a chart of residuals.

**Alarm Script** Enables you to write and run a script that indicates when the data fail special causes tests. Results can be written to a file, written to the log or sent in an email. There is an option to include an explanation of why the test failed.

As an Alarm Script is invoked, the following variables are available, both in the issued script and in subsequent JSL scripts:

qc\_col is the name of the column

qc\_test is the test that failed

qc\_sample is the sample number

**Tip:** After an alarm script is specified, the alarm script is invoked when the Test Beyond Limits option is turned on.

See the *Scripting Guide* for more information about writing custom Alarm Scripts.

See *Using JMP* for more information about the following options:

**Redo** Contains options that enable you to repeat or relaunch the analysis. In platforms that support the feature, the Automatic Recalc option immediately reflects the changes that you make to the data table in the corresponding report window.

**Save Script** Contains options that enable you to save a script that reproduces the report to several destinations.

**Save By-Group Script** Contains options that enable you to save a script that reproduces the platform report for all levels of a By variable to several destinations. Available only when a By variable is specified in the launch window.

# Average Run Length (ARL) Report for EWMA Control Charts

The Average Run Length (ARL) report contains a table and a graph of ARL values. The average run length (ARL) for a specified shift is the average number of runs expected before an out-of-control signal occurs. For example, the ARL at 0 represents the average number of runs expected before seeing a false-alarm signal when the process is in control. When the process is in control, the shift size is 0.

The table and graph in the ARL report enable you to explore how various settings of the Lambda parameter affect the performance of the corresponding EWMA chart. The table and graph also enable you to compare the performance of the EWMA chart with a Shewhart chart, such as the X chart in the EWMA Chart report. The Shewhart ARL column is equivalent to the EWMA ARL column when Lambda is set to 1.

The value of EWMA ARL at 0 depends on the setting of the Constant Limits option:

- If the Constant Limits option is selected, the process is assumed to have been in control long enough that the effect of the starting value is negligible. In this case, also referred to as a *steady state* of the EWMA chart, the value of EWMA ARL(0) is calculated using the method described in Crowder (1987).
- If the Constant Limits option is not selected, the value of EWMA ARL(0) is calculated using the method described in Knoth (2004). This situation is also referred to as a *zero state* of the EWMA chart.

## **ARL Report**

The ARL Report shows the average run length for standardized shifts ( $\Delta$ ) between 0 and 3 at 0.25 increments. The shift is represented by  $\operatorname{sqrt}(n)$ \*RawShift/Sigma, where n is the constant sample size in each subgroup. For the multiplier used in calculating control limits, K = 3 is assumed. This table contains ARL values for the EWMA chart as well as a Shewhart chart.

## ARL Graph

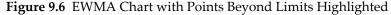
The ARL Graph shows the average run length for standardized shifts ( $\Delta$ ) between 0 and 3. This graph contains the same data points as the ARL Table to the left of the ARL Graph. The solid line corresponds to the EWMA ARL values, and the dashed line corresponds to the Shewhart ARL values.

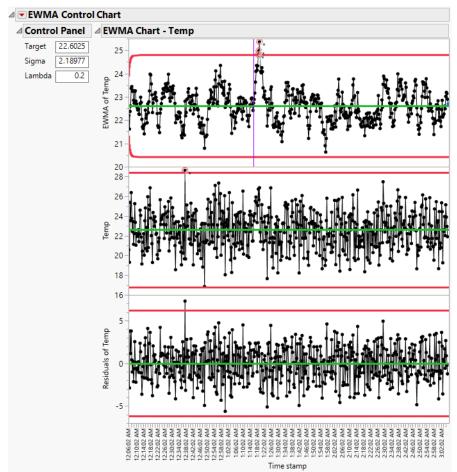
**EWMA Control Charts** 

# Additional Example of the EWMA Control Chart Platform

In this example, you create a chart that overlays the subgroup points and limits on the EWMA control chart. This enables you to see the EWMA points in the context of the subgroup points. The Quench.jmp sample data table contains simulated observations of temperature at the time of magnet quench. Magnet quench occurs when part of the superconducting coil enters a resistive state and increases in temperature. When this happens, containment of the fusion reactor is at risk. Immediately shutting down power to the magnet is required to prevent a breach.

- 1. Select **Help > Sample Data Library** and open Quality Control/Quench.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > EWMA Control Chart.
- 3. Select Temp and click Y.
- 4. Select Time stamp and click **Subgroup**.
- 5. Click **OK**.
- 6. Click the EWMA Control Chart red triangle and select **Test Beyond Limits**.





Note that three observations are outside the limits in the EWMA chart and one observation is outside the limits in the X chart. The observations outside of the limits are indicated by a red circle. The purple vertical line in the EWMA chart denotes a shift upward around 1:16 AM.

- 7. Click the EWMA Control Chart red triangle and select **Overlay Charts**. The X chart limits are not shown on the overlay chart by default, so the observation outside the X limits is not circled until you turn on the X limits for the overlay chart.
- 8. Click the EWMA Control Chart red triangle and select **Show X Limits on Overlay Charts**.

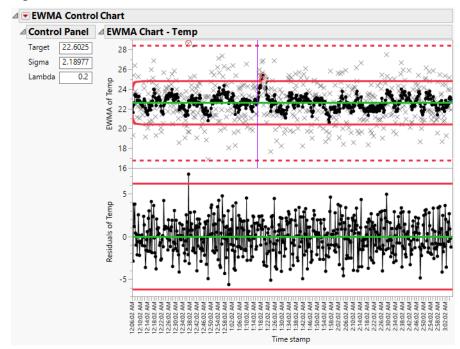
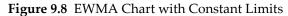


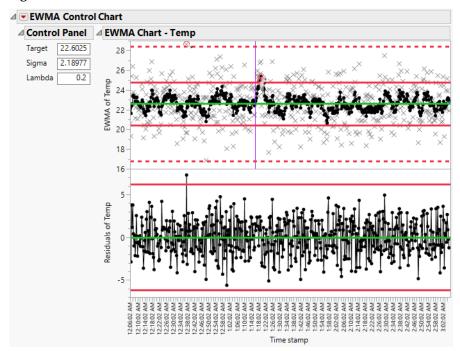
Figure 9.7 EWMA Chart with Overlaid X Chart

The solid lines and circles in the top chart represent the limits and points for the EWMA chart. The dashed lines and x markers represent the limits and points for the X chart. Note that the observations outside the EWMA limits and the X limits are still circled.

9. Click the EWMA Control Chart red triangle and select **Constant Limits**.



Statistical Details for the EWMA Control Chart Platform



Because the time span of the data is so long, the asymptotic limits differ from the original EWMA limits only for the first few subgroups. In this case, you might decide that you can use constant (asymptotic) limits instead of the EWMA limits.

# Statistical Details for the EWMA Control Chart **Platform**

This section defines the statistics that are used in the construction of the EWMA chart. Some of these statistics are also saved in the data table that is created by the Save Summaries command.

The  $i^{th}$  point on the EWMA chart is calculated as follows:

$$EWMA_i = \lambda X_i + (1 - \lambda)EWMA_{i-1}$$

where:

 $\lambda$  = Lambda parameter

 $X_i = i^{th}$  sample value (or subgroup mean)

$$EWMA_{i-1} = (i-1)^{th}$$
 EWMA value

When i = 1, define  $EWMA_0$  as the Target value.

**Note:** When the Restart EWMA after Empty Subgroup option is selected, the  $EWMA_{i-1}$  value following an empty subgroup is the Target value. When the Restart EWMA after Empty Subgroups option is not selected, the  $EWMA_{i-1}$  value following an empty subgroup is the EWMA value for the most recent non-empty subgroup.

The computation of the control limits on the EWMA chart is determined by the setting of the Constant Limits option.

#### **EWMA Limits**

When the Constant Limits option is not selected and the subgroup sizes are not equal, the EWMA control limits are computed as follows:

LCL = 
$$T - K\sigma\lambda \sqrt{\sum_{j=1}^{i} \frac{(1-\lambda)^{2(i-j)}}{n_j}}$$

UCL = 
$$T + K\sigma\lambda \sqrt{\sum_{j=1}^{i} \frac{(1-\lambda)^{2(i-j)}}{n_j}}$$

where:

T = Target value

K = the sigma multiplier and is set to 3 by default

 $\sigma$  = Sigma value

i = the number of the sample (or subgroup)

 $n_i$  = the size of subgroup i

When the Constant Limits option is not selected and the subgroup sizes are equal, the formulas for the EWMA control limits simplify as follows:

LCL = 
$$T - K\sigma \sqrt{\frac{\lambda}{n(2-\lambda)}[1-(1-\lambda)^{2i}]}$$

UCL = 
$$T + K\sigma \sqrt{\frac{\lambda}{n(2-\lambda)}[1-(1-\lambda)^{2i}]}$$

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where:

T = Target value

K = the sigma multiplier and is set to 3 by default

 $\sigma$  = Sigma value

i =the number of the sample (or subgroup)

n = the size of each subgroup (or 1 if no subgroup is specified)

#### **Constant Limits**

When the Constant Limits option is selected, the EWMA control limits are computed as follows:

LCL = 
$$T - K\sigma \sqrt{\frac{\lambda}{n(2-\lambda)}}$$

UCL = 
$$T + K\sigma \sqrt{\frac{\lambda}{n(2-\lambda)}}$$

where:

T = Target value

K = the sigma multiplier and is set to 3 by default

σ = Sigma value

n = the subgroup size (or 1 if no subgroup is specified)

For more information about constructing exponentially weighted moving average charts, see Montgomery (2013).

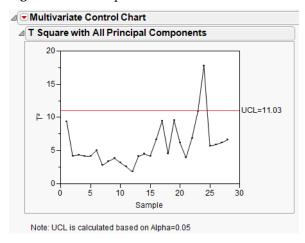
# **Multivariate Control Charts**

## **Monitor Multiple Process Characteristics Simultaneously**

Multivariate control charts are used to monitor two or more interrelated process variables. Where univariate control charts are used to monitor a single independent process characteristic, multivariate control charts are necessary when process variables are correlated. The Multivariate Control Chart platform enables you to build Hotelling  $T^2$  charts. You can use the platform to determine whether a process is stable as well as to monitor a process as new data are collected.

For monitoring and diagnosing complex processes, see "Model Driven Multivariate Control Charts".

Figure 10.1 Example of a Multivariate Control Chart



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# **Overview of Multivariate Control Charts**

Multivariate control charts are used to monitor two or more interrelated process variables. Where univariate control charts are used to monitor a single independent process characteristic, multivariate control charts are necessary when process variables are correlated. A Hotelling  $T^2$  chart, or just  $T^2$  chart for short, is one type of multivariate control chart. A  $T^2$  chart can detect shifts in the mean or the relationship between several interrelated variables. The observations can either be individual observations of the process variables or they can be grouped into rational subgroups.

You can construct a multivariate control chart using current or historical data. The control chart is said to be a Phase I chart if it is constructed using current data; the control chart is said to be a Phase II chart if it is constructed using target statistics from a historical data set. In Phase I, you check that the process is stable and establish a historical data set from which to calculate target statistics for the process. In Phase II, the multivariate control chart uses the target statistics from Phase I in order to monitor new process observations.

To construct a Phase II multivariate control chart, first identify a period of time during which the process is stable and capable.

- Develop a Phase I control chart to verify that the process is stable over this period.
   The data used in Phase I provides a historical data set.
- 2. Save the target statistics for this historical data set.
- 3. Monitor the on-going process using a Phase II control chart based on the target statistics that were saved in step 2.

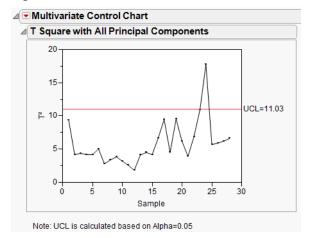
# **Example of a Multivariate Control Chart**

This example illustrates constructing a control chart for data that are not sub-grouped. The data are measurements on a steam turbine engine. For an example that uses sub-grouped data, "Example of Monitoring a Process Using Sub-Grouped Data".

#### **Step 1: Determine Whether the Process Is Stable**

- 1. Select **Help > Sample Data Library** and open Quality Control/Steam Turbine Historical.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > Multivariate Control Chart.
- 3. Select all of the columns and click **Y**, **Columns**.
- 4. Click **OK**.

Figure 10.2 Initial Multivariate Control Chart



The process seems to be in reasonable statistical control, because there is only one out-of-control point. Therefore, it is appropriate to create targets based on this data.

#### **Step 2: Save Target Statistics**

Click the red triangle next to Multivariate Control Chart and select Save Target Statistics.
 This creates a new data table containing target statistics for the process.

Figure 10.3 Target Statistics for Steam Turbine Data

	Ref_Stats	Fuel	Steam Flow	Steam Temp	MW	Cool Temp	Pressure
1	_SampleSize	28	28	28	28	28	28
2	_NumSample	1	1	1	1	1	1
3	_Mean	237595.78571	179015.78571	846.39285714	20.647142857	53.871428571	29.139285714
4	_Std	7247.6859825	4374.3063819	2.9481857034	0.5341650261	0.2088010623	0.0497347461
5	_Corr_Fuel	1	0.8714382899	-0.549875041	0.8558570808	-0.270049819	-0.469928462
6	_Corr_Steam Flow	0.8714382899	1	-0.629023927	0.9852529223	-0.223127002	-0.533056185
7	_Corr_Steam Temp	-0.549875041	-0.629023927	1	-0.595214609	0.2475387217	0.2192147319
8	_Corr_MW	0.8558570808	0.9852529223	-0.595214609	1	-0.207305813	-0.50447312
9	_Corr_Cool Temp	-0.270049819	-0.223127002	0.2475387217	-0.207305813	1	0.3617461646
10	_Corr_Pressure	-0.469928462	-0.533056185	0.2192147319	-0.50447312	0.3617461646	1

2. Save the new data table as Steam Turbine Targets.jmp.

Now that target statistics have been established, create the multivariate control chart that monitors the process.

#### **Step 3: Monitor the Process**

1. Select **Help > Sample Data Library** and open Quality Control/Steam Turbine Current.jmp.

This sample data table contains recent observations from the process.

- 2. Select Analyze > Quality and Process > Control Chart > Multivariate Control Chart.
- 3. Select all of the columns and click **Y, Columns**.
- 4. Click Get Targets.
- 5. Open the Steam Turbine Targets.jmp table that you saved.
- 6. Click **OK**.

The default alpha level is set to 0.05. Change it to 0.001.

- Click the red triangle next to Multivariate Control Chart and select Set Alpha Level > Other.
- 8. Type 0.001 and click **OK**.

Figure 10.4 Steam Turbine Control Chart

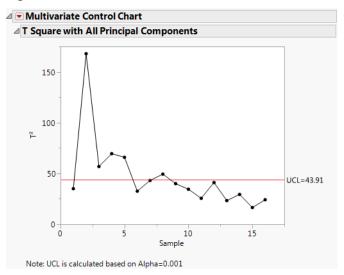
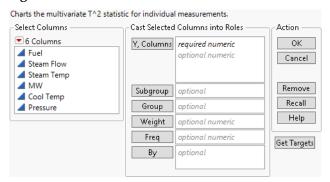


Figure 10.4 shows out-of-control conditions occurring at observations 2, 3, 4, 5, and 8. This result implies that these observations do not conform to the historical data from Steam Turbine Historical.jmp, and that the process should be further investigated. To find an assignable cause, you might want to examine individual univariate control charts or perform another univariate procedure.

# Launch the Multivariate Control Chart Platform

Launch the Multivariate Control Chart platform by selecting **Analyze > Quality And Process > Control Chart > Multivariate Control Chart.** 

Figure 10.5 The Multivariate Control Chart Launch Window



For more information about the options in the Select Columns red triangle menu, see *Using IMP*.

The Multivariate Control Chart platform launch window contains the following options:

**Y, Columns** Specify the columns to be analyzed.

**Subgroup** Enter a column with sub-grouped data. Hierarchically, this group is nested within **Group**.

**Group** Enter a column that specifies group membership at the highest hierarchical level.

**Weight** Identifies the data table column whose variables assign weight (such as importance or influence) to the data.

**Freq** Identifies the data table column whose values assign a frequency to each row. Can be useful when your data table contains summarized data.

**By** Identifies a column that creates a report consisting of separate analyses for each level of the variable.

**Get Targets** Click to select a JMP table that contains historical targets for the process.

# The Multivariate Control Chart

Use the multivariate control chart to quickly identify shifts in your process and to monitor your process for special cause indications.

Follow the instructions in "Example of a Multivariate Control Chart" to produce the results shown in Figure 10.6.

■ Multivariate Control Chart T Square with All Principal Components 150 100 50 -UCL=43.91 Note: UCL is calculated based on Alpha=0.001 Principal Components of Target Data: on Covariances Eigenvalue Percent 20 40 60 80 Cum Percent ChiSquare 68113144 95.046 95.046 1163.46 20.000 3550369 4.954 100.000 977.875 14.000 5.2538 0.000 100.000 210.549 9.000 <.0001\* 100.000 0.0081 0.000 100,000 9.844 2.000 0.0015 0.000 100 000 0.000 0.000 Eigenvectors 0.00011 -0.00026 0.00000 0.00005 0.00001 -0.00001 Fuel Steam Flow -0.00000 -0.00000 0.43623 -0.06279 -0.07346 Steam Temp MW 0.00000 0.00000 0.00321 0.13618 11.06244 -2.42921 Cool Temp -0.00000 0.00000 0.00549 4.99852 -0.37488 -1.79856 -0.00000 -0.00000 -0.00141 0.35934 1.00953 25.96065 Pressure Note: Eigenvectors were divided by square root of eigenvalues. Principal Components of Current Data: on Covariances Eigenvalue Percent 20 40 60 80 Cum Percent ChiSquare DF Prob>ChiSq 44528275 95.921 95.921 1133.58 20.000 1893508 4 079 100 000 933,552 14,000 < 0001\* 100.000 3.0286 0.000 172.174 9.000 <.0001\* 0.0722 100.000 48.036 5.000 0.000 100.000 2.000 0.0008 0.000 100.000 0.000 Fuel 0.00014 -0.00028 -0.00008 -0.00011 -0.00006 -0.00007 Steam Flow 0.00006 0.00067 0.00006 -0.00012 0.00004 0.00055 Steam Temp 0.00000 -0.00000 0.57433 -0.03529 0.19949 0.00000 0.00000 0.00307 3.68646 0.92442 -0.43413 Cool Temp -0.00000 -0.00000 -0.01720 -0.50095 6.76037 1.22547 -0.00000 -0.00000 0.00517 0.06319 -0.22439 34.88730 Pressure

Figure 10.6 Multivariate Control Chart

**Tip:** For information about additional options, see "Multivariate Control Chart Platform Options".

The multivariate control chart plots Hotelling's T<sup>2</sup> statistic. The calculation for the control limit differs based on whether targets have been specified. To understand how the T<sup>2</sup> statistic and the UCL (Upper Control Limit) are calculated, see "Statistical Details for Multivariate Control Charts". For more information about control limits, see Tracy et al. (1992).

In this example, the Principal Components reports for both data sets indicate that the first eigenvalue, corresponding to the first principal component, explains about 95% of the total variation in the variables. The values in both Eigenvectors tables indicate that the first principal component is driven primarily by the variables Fuel and Steam Flow. You can use this information to construct a potentially more sensitive control chart based only on this first component. For more information about the Principal Components reports, see "Principal Components".

# **Multivariate Control Chart Platform Options**

The Multivariate Control Chart red triangle menu contains the following options:

- **T Square Chart** Shows the  $T^2$  chart. Hotelling's  $T^2$  chart is a multivariate extension of the XBar chart that takes correlation into account.
- **T Square Partitioned** Constructs multivariate control charts based on the principal components of Y. Specify the number of major principal components for  $T^2$ . See "T Square Partitioned".
- **Set Alpha Level** Set the  $\alpha$  level used to calculate the control limit. The default is  $\alpha$ =0.05.
- **Show Covariance** Shows the Covariance report. Covariance is a measure of the linear relationship between two variables. When a subgroup variable is specified, the Pooled Covariance report is shown.
- **Show Correlation** Shows the Correlation report. When a subgroup variable is specified, the Pooled Correlation report is shown.
- **Show Inverse Covariance** Shows the Inverse Covariance report. If the inverse covariance is singular, a generalized inverse of the covariance matrix is reported. When a subgroup variable is specified, the Pooled Inverse Covariance report is shown.
- **Show Inverse Correlation** Shows the Inverse Correlation report. If the inverse correlation is singular, a generalized inverse of the correlation matrix is reported. When a subgroup variable is specified, the Pooled Inverse Correlation report is shown.
- **Show Means** Shows the Group Means report, which contains the means for each group.
- **Save T Square** Creates a new column in the data table containing  $T^2$  values.

- **Save T Square Formula** Creates a new column in the data table. Stores a formula in the column that calculates the  $T^2$  values.
- **Save Target Statistics** Creates a new data table containing target statistics for the process. Target statistics include: sample size, the number of samples, mean, standard deviation, and any correlations.
- **Change Point Detection** (Not available for sub-grouped data.) Shows a Change Point Detection plot of test statistics by row number and indicates the row number where the change point appears. See "Change Point Detection".
- **Principal Components** Shows reports showing eigenvalues and their corresponding eigenvectors. Principal components help you understand which of the many variables you might be monitoring are primarily responsible for the variation in your process. See "Principal Components".
- **Save Principal Components** Creates new columns in the data table that contain the scaled principal components.

# **T Square Partitioned**

If you are monitoring a large number of correlated process characteristics, you can use the T Square Partitioned option to construct a control chart based on principal components. If a small number of principal components explains a large portion of the variation in your measurements, then a multivariate control chart based on these big components might be more sensitive than a chart based on your original, higher-dimensional data.

The T Square Partitioned option is also useful when your covariance matrix is ill-conditioned. When this is the case, components with small eigenvalues, explaining very little variation, can have a large, and misleading, impact on T<sup>2</sup>. It is useful to separate out these less important components when studying process behavior.

Once you select the T Square Partitioned option, you need to decide how many major principal components to use.

The option creates two multivariate control charts: T Square with Big Principal Components and T Square with Small Principal Components. Suppose that you enter r as the number of major components when you first select the option. The chart with Big Principal Components is based on the r principal components corresponding to the r largest eigenvalues. These are the r components that explain the largest amount of variation, as shown in the Percent and Cum Percent columns in the Principal Components: on Covariances reports. The chart with Small Principal Components is based on the remaining principal components.

For a given subgroup, its  $T^2$  value in the Big Principal Components chart and its  $T^2$  value in the Small Principal Components chart sum to its overall  $T^2$  statistic presented in the  $T^2$  with All Principal Components report. For more information about how the partitioned  $T^2$  values are calculated, see Kourti and MacGregor (1996).

**Tip:** Consider using the Model Driven Multivariate Control Chart platform for decomposition of the T<sup>2</sup> statistic. See "Model Driven Multivariate Control Charts".

# **Change Point Detection**

When the data set consists of multivariate individual observations, a control chart can be developed to detect a shift in the mean vector, the covariance matrix, or both. This method partitions the data and calculates likelihood ratio test statistics for a shift. The statistic that is plotted on the control chart is an observation's likelihood ratio test statistic divided by the product of the following:

- Its approximate expected value assuming no shift.
- An approximate value for an upper control limit.

Division by the approximate upper control limit allows the points to be plotted against an effective upper control limit of 1. A Change Point Detection plot readily shows the change point for a shift occurring at the maximized value of the control chart statistic. The Change Point Detection implementation in JMP is based on Sullivan and Woodall (2000) and is described in "Statistical Details for Change Point Detection".

**Note:** The Change Point Detection method is designed to show a single shift in the data. Detect multiple shifts by recursive application of this method.

Note the following about the Change Point Detection plot:

- Values above 1.0 indicate a possible shift in the data.
- Control chart statistics for the Change Point Detection plot are obtained by dividing the likelihood ratio statistic of interest (either a mean vector or a covariance matrix) by a normalizing factor.
- The change point of the data occurs for the observation having the maximum test statistic value for the Change Point Detection plot.

Note the following about the scatterplot matrix:

- This plot shows the shift in the sample mean vector.
- In the "Example of Change Point Detection", data are divided into two groups. The first 24 observations are classified as the first group. The remaining observations are classified as the second group.

**Multivariate Control Charts** 

## **Principal Components**

The Principal Components report contain the following information:

**Eigenvalue** Eigenvalues for the covariance matrix.

**Percent** Percent variation explained by the corresponding eigenvector. Also shows an accompanying bar chart.

**Cum Percent** Cumulative percent variation explained by eigenvectors corresponding to the eigenvalues.

**ChiSquare** Provides a test of whether the correlation remaining in the data is of a random nature. This is a Bartlett test of sphericity. When this test rejects the null hypothesis, this implies that there is structure remaining in the data that is associated with this eigenvalue.

**DF** Degrees of freedom associated with the Chi-square test.

**Prob > ChiSq** *p*-value for the test.

**Eigenvectors** Table of eigenvectors corresponding to the eigenvalues. Note that each eigenvector is divided by the square root of its corresponding eigenvalue.

For more information about principal components, see *Multivariate Methods*.

# **Additional Examples of Multivariate Control Charts**

- "Example of Monitoring a Process Using Sub-Grouped Data"
- "Example of T Square Partitioned"
- "Example of Change Point Detection"

## Example of Monitoring a Process Using Sub-Grouped Data

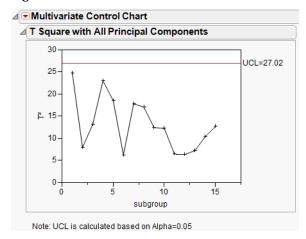
The workflow for monitoring a multivariate process with sub-grouped data is similar to the one for individual data. See "Example of a Multivariate Control Chart". You create an initial control chart to save target statistics and then use these targets to monitor the process.

### Step 1: Determine Whether the Process Is Stable

- Select Help > Sample Data Library and open Quality Control/Aluminum Pins Historical.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > Multivariate Control Chart.
- 3. Select all of the Diameter and Length columns and click **Y, Columns**.

- 290
- 4. Select subgroup and click **Subgroup**.
- 5. Click **OK**.

Figure 10.7 Multivariate Control Chart for Sub-Grouped Data, Step 1



The process appears to be in statistical control, making it appropriate to create targets using this data.

### **Step 2: Save Target Statistics**

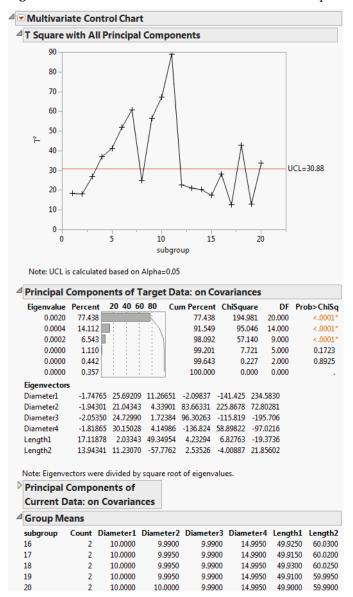
- 1. Click the red triangle next to Multivariate Control Chart and select **Save Target Statistics**. This creates a new data table containing target statistics for the process.
- Save the new data table as Aluminum Pins Targets.jmp.
   Now that target statistics have been established, create the multivariate control chart for process monitoring.

### **Step 3: Monitor the Process**

- Select Help > Sample Data Library and open Quality Control/Aluminum Pins Current.jmp.
   This sample data table contains recent observations from the process.
- 2. Select Analyze > Quality and Process > Control Chart > Multivariate Control Chart.
- 3. Select all of the Diameter and Length columns and click **Y, Columns**.
- 4. Select subgroup and click **Subgroup**.
- 5. Click **Get Targets**.
- 6. Open the Aluminum Pins Targets.jmp table that you saved.
- 7. Click **OK**.

8. Click the red triangle next to Multivariate Control Chart and select **Show Means**. The Show Means option gives the means for each subgroup. You can then observe which groups are most dissimilar from each other.

Figure 10.8 Multivariate Control Chart for Sub-Grouped Data, Step 3



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Figure 10.8 shows indications of instability at subgroups 4-7, 9-11, 18, and 20. This result implies that these observations do not conform to the historical data from Aluminum Pins Historical.jmp, and that the process should be further investigated. To determine why the process was out of control at these points, you might want to examine individual univariate control charts or perform another univariate procedure.

An alternative method to monitoring this process is based on the big principal components. In this example, for the historical data, the first three principal components account for about 98% of the variation. Based on this, you might construct a chart for the first three principal components. Then you would monitor current data using those three components. The control limits for the chart used in monitoring the process should be based on the corresponding chart for the historical data.

## **Example of T Square Partitioned**

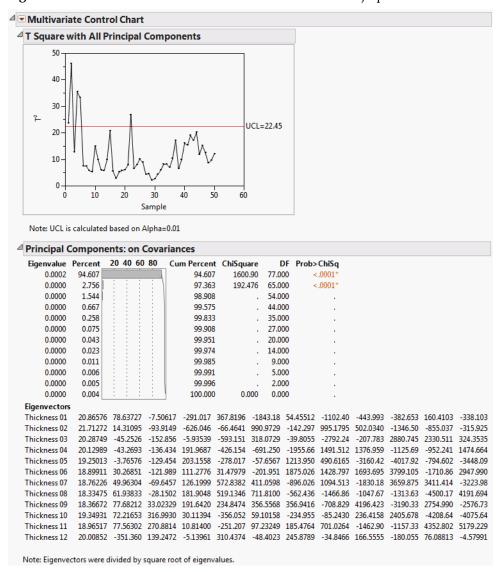
Use T Square Partitioned to separate out the more important components from the less important components when studying process behavior. In this example, the coating on each of 50 bars was measured at 12 uniformly spaced locations across the bar. You want to examine the variation in the measurements and determine whether the causes of variation need to be investigated further.

- 1. Select **Help > Sample Data Library** and open Quality Control/Thickness.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > Multivariate Control Chart.
- 3. Select all of the Thickness columns and click **Y**, **Columns**.
- 4. Click **OK**.

The current alpha level is set to 0.05, which corresponds to a 5% false alarm rate. You want to set the false alarm rate to 1%.

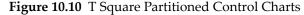
5. To change the alpha level, click the red triangle next to Multivariate Control Chart, select **Set Alpha Level**, and choose **0.01**.

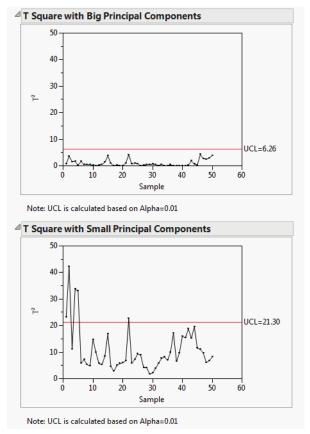
Figure 10.9 Initial Multivariate Control Chart for Thickness.jmp



The overall control chart in Figure 10.9 suggests that special causes affected bars 1, 2, 4, 5, and 22. Looking at the Principal Components report, you can see that almost 95% of the variation in the 12 thickness measurements is explained by the first principal component. You want to study the variation associated with this principal component further.

- 6. Click the red triangle Multivariate Control Chart and select **T Square Partitioned**.
- 7. Accept the default value of 1 principal component by clicking **OK**.





In contrast to the Principal Components report, the T Square with Big Principal Components chart, which reflects variation for only the first component, shows no evidence of special causes. The T Square with Small Principal Components chart shows that the special cause indications reside in the remaining smaller components. These smaller components do not explain much variation, and likely represent random noise. Therefore, you might conclude that the variation in the thickness measurements is not a major cause for concern.

# **Example of Change Point Detection**

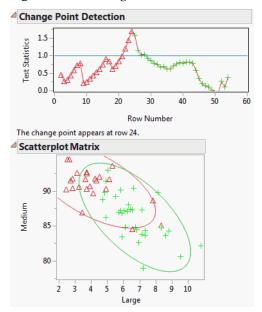
Use change point detection to find the point at which a shift occurs in your data.

- 1. Select **Help > Sample Data Library** and open Quality Control/Gravel.jmp.
- 2. Select Analyze > Quality and Process > Control Chart > Multivariate Control Chart.
- 3. Select Large and Medium and click **Y**, **Columns**.
- 4. Click **OK**.

Statistical Details for Multivariate Control Charts

5. Click the red triangle next to Multivariate Control Chart and select **Change Point Detection**.





**Tip:** You might need to drag the axes to see the density ellipses for the two groups, depending on your data.

In the Change Point Detection plot, values above 1.0 indicate a possible shift in the data. At least one shift is apparent; the change point occurs at observation 24 and the shift occurs immediately after observation 24. The 95% prediction regions for the two groups have approximately the same size, shape, and orientation, visually indicating that the sample covariance matrices are similar.

# Statistical Details for Multivariate Control Charts

- "Statistical Details for Individual Observations"
- "Statistical Details for Observations in Rational Subgroups"
- "Statistical Details for Change Point Detection"

### Statistical Details for Individual Observations

Consider measurements that are not sub-grouped, that is, where the natural subgroup size is n = 1. Denote the number of observations by m and the number of variables measured by p. A  $T^2$  statistic is calculated and plotted for each observation. The calculation of the  $T^2$  statistic and upper control limit (UCL) depends on the source of the target statistics. In a Phase I chart, the limits are based on the same data that is being plotted on the control chart. In a Phase II chart, the limits are based on target statistics that were calculated from a historical data set. For more information about  $T^2$  statistic and control limit calculations for Hotelling  $T^2$  control charts, see Montgomery (2013).

#### **Calculations for Phase I Control Charts**

In Phase I control charts, the  $T^2$  statistic for the  $i^{th}$  observation is defined as follows:

$$T_i^2 = (Y_i - \overline{Y})'S^{-1}(Y_i - \overline{Y})$$

where:

 $Y_i$  is the column vector of p measurements for the i<sup>th</sup> observation

 $\overline{Y}$  is the column vector of sample means of the *p* variables

 $S^{-1}$  is the inverse of the sample covariance matrix

The  $T_i^2$  value for each of the i observations are the points plotted on the multivariate control chart.

When computing Phase I control limits, the UCL is based on the beta distribution. Specifically, the upper control limit (UCL) is defined as follows:

$$UCL = \frac{(m-1)^2}{m} \beta \left[ 1 - \alpha; \frac{p}{2}; \frac{m-p-1}{2} \right]$$

where:

p = number of variablesm = number of observations

$${}^{\beta}_{\left[1-\alpha;\frac{p}{2};\frac{m-p-1}{2}\right]} = (1-\alpha)^{th} \text{ quantile of a Beta } \left(\frac{p}{2},\frac{m-p-1}{2}\right) \text{ distribution}$$

#### Calculations for Phase II Control Charts

In Phase II control charts, define the historical data set as X. Then the  $T^2$  statistic for the  $i^{th}$  observation is defined as follows:

$$T_i^2 = (Y_i - \overline{X})' S_X^{-1} (Y_i - \overline{X})$$

where:

 $Y_i$  is the column vector of p measurements for the i<sup>th</sup> observation

 $\overline{X}$  is the column vector of sample means of the p variables, calculated from the historical data set

 $S_X^{-1}$  is the inverse of the sample covariance matrix, calculated from the historical data set

The  $T_i^2$  value for each of the *i* observations are the points plotted on the multivariate control chart.

When computing Phase II control limits, new observations are independent of the historical data set. In this case, the upper control limit (UCL) is a function of the *F* distribution and partially depends on the number of observations in the historical data set from which the targets are calculated. The UCL is defined as follows:

$$UCL = \begin{cases} \frac{p(m+1)(m-1)}{m(m-p)} F_{[1-\alpha, p, m-p]} & \text{if } m \le 100\\ \frac{p(m-1)}{m-p} F_{[1-\alpha, p, m-p]} & \text{if } m > 100 \end{cases}$$

where:

p = number of variables

m = number of observations in the historical data set

$$F_{[1-\alpha, p, m-p]} = (1-\alpha)^{th}$$
 quantile of an  $F(p, m-p)$  distribution

# Statistical Details for Observations in Rational Subgroups

Consider the case where p variables are monitored and m subgroups of size n > 1 are obtained. A  $T^2$  statistic is calculated and plotted for each subgroup. The calculation of the  $T^2$  statistic and upper control limit (UCL) depends on the source of the target statistics. In a Phase I chart, the limits are based on the same data that is being plotted on the control chart. In a Phase II chart, the limits are based on target statistics that were calculated from a historical data set. For more information about  $T^2$  statistic and control limit calculations for Hotelling  $T^2$  control charts, see Montgomery (2013).

#### Calculations for Phase I Control Charts

For Phase I control charts, the  $T^2$  statistic for the  $j^{th}$  subgroup is defined as follows:

$$T_i^2 = (\overline{Y}_i - \overline{Y})' S_p^{-1} (\overline{Y}_i - \overline{Y})$$

where:

 $\overline{Y}_j$  is the mean of the n column vectors of p measurements for the  $j^{\text{th}}$  subgroup

$$\overline{Y} = \frac{1}{m} \sum_{j=1}^{m} \overline{Y}_{j}$$
 is the mean of the subgroup means

 $S_i$  is the sample covariance matrix for the *n* observations in the  $j^{th}$  subgroup

$$S_p = \frac{1}{m} \sum_{j=1}^{m} S_j$$
 is the pooled covariance matrix, calculated as the mean of the

within-subgroup covariance matrices

The Phase I upper control limit (UCL) is defined as follows:

$$UCL = \frac{p(m-1)(n-1)}{mn - m - p + 1} F_{[1-\alpha, p, mn - m - p + 1]}$$

where:

p = number of variablesn = sample size for each subgroupm = number of subgroups

$$F_{[1-\alpha, p, mn-m-p+1]} = (1-\alpha)^{th}$$
 quantile of an  $F(p, mn-m-p+1)$  distribution

#### Calculations for Phase II Control Charts

In Phase II control charts, define the historical data set from which the target statistics are calculated as X. Then the  $T^2$  statistic for the  $j^{th}$  subgroup is defined as follows:

$$T_j^2 = (\overline{Y}_j - \overline{X})' S_p^{-1} (\overline{Y}_j - \overline{X})$$

where:

 $\overline{Y}_j$  is the mean of the n column vectors of p measurements for the  $j^{\text{th}}$  subgroup

 $\overline{X}_k$  is the mean of the n column vectors of p measurements for the k<sup>th</sup> subgroup from the historical data set

$$\overline{X} = \frac{1}{m} \sum_{k=1}^{m} \overline{X}_{k}$$
 is the overall mean of the observations

 $S_k$  is the sample covariance matrix for the n observations in the  $k^{th}$  subgroup from the historical data set

$$S_p = \frac{1}{m} \sum_{k=1}^{m} S_k$$
 is the pooled covariance matrix, calculated as the mean of the

within-subgroup covariance matrices

The Phase II upper control limit (UCL) is defined as follows:

$$UCL = \frac{p(m+1)(n-1)}{mn - m - p + 1} F_{[1-\alpha, p, mn - m - p + 1]}$$

where:

p = number of variables

n = subgroup sample size

m = number of subgroups in the historical data set

$$F_{[1-\alpha, p, mn-m-p+1]} = (1-\alpha)^{th}$$
 quantile of an  $F(p, mn-m-p+1)$  distribution

#### **Additivity of Test Statistics for Observations in Rational Subgroups**

When a sample of mn independent normal observations is grouped into m rational subgroups each of size n, define  $T^2_M$  as the distance between the mean  $\overline{Y}_j$  of the jth subgroup and the target value. ( $T^2_M$  is equivalent to  $T^2$  in the previous sections for observations in rational subgroups.) You can also calculate  $T^2$  statistics related to the internal variability in each subgroup and the overall variability around the target value. The components of the  $T^2$  statistic are additive, much like sums of squares. Specifically, the following relationship is true for each of the m subgroups:

$$T_{A_j}^2 = T_{M_j}^2 + T_{D_j}^2$$

In all of the following definitions,  $S_p$  is defined as it is in the previous sections, depending on whether the control chart is a Phase I or a Phase II control chart. Also, define  $\mu$  as  $\overline{Y}$  for Phase I control charts and as  $\overline{X}$  for Phase II control charts.

The distance from the target value for the  $j^{th}$  subgroup is defined as follows:

$$T_{M_j}^2 = n(\overline{Y}_j - \mu)' S_P^{-1}(\overline{Y}_j - \mu)$$

The internal variability for the  $j^{th}$  subgroup is defined as follows:

$$T_{D_j}^2 = \sum_{i=1}^{n} (Y_{ji} - \overline{Y}_j)' S_p^{-1} (Y_{ji} - \overline{Y}_j)$$

where  $Y_{ji}$  is the  $i^{th}$  column vector of p measurements for the  $j^{th}$  subgroup.

The overall variability for the  $j^{th}$  subgroup is defined as follows:

$$T_{A_j}^2 = \sum_{i=1}^{n} (Y_{ji} - \mu)' S_p^{-1} (Y_{ji} - \mu)$$

where  $Y_{ji}$  is the  $i^{th}$  column vector of p measurements for the  $j^{th}$  subgroup.

**Note:** When you select the **Save T Square** or **Save T Square Formula** options from the Multivariate Control Chart red triangle menu, the three values saved in each row correspond to one value of *i* in the three definitions above.

# **Statistical Details for Change Point Detection**

This discussion follows the development in Sullivan and Woodall (2000).

#### **Assumptions**

Denote a multivariate distribution of dimension p with mean vector  $\mu_i$  and covariance matrix  $\Sigma_i$  by  $N_p(\mu_i,\Sigma_i)$ . Suppose that the  $x_i$  are m (where m > p) independent observations from such a distribution:

$$x_i \sim N_p(\mu_i, \Sigma_i), \quad i = 1, ..., m$$

If the process is stable, the means  $\mu_i$  and the covariance matrices  $\Sigma_i$  equal a common value so that the  $x_i$  have a  $N_n(\mu, \Sigma)$  distribution.

Suppose that a single change occurs in either the mean vector or the covariance matrix, or both, between the  $m_1$  and  $m_1$ +1 observations. Then the following conditions hold:

- Observations 1 through  $m_1$  have the same mean vector and the same covariance matrix  $(\mu_{ar}\Sigma_a)$ .
- Observations  $m_1 + 1$  to m have the same mean vector and covariance matrix  $(\mu_{lp}, \Sigma_p)$ .
- One of the following occurs:
  - If the change affects the mean,  $\mu_a \neq \mu_b$ .
  - If the change affects the covariance matrix,  $\Sigma_a \neq \Sigma_b$ .
  - If the change affects both the mean and the covariance matrix,  $\mu_a \neq \mu_b$  and  $\Sigma_a \neq \Sigma_b$ .

#### Overview

A likelihood ratio test approach is used to identify changes in one or both of the mean vector and covariance matrix. The likelihood ratio test statistic is used to compute a control chart statistic that has an approximate upper control limit of 1. The control chart statistic is plotted for all possible  $m_1$  values. If any observation's control chart statistic exceeds the upper control limit of 1, this is an indication that a shift occurred. Assuming that exactly one shift occurs, that shift is considered to begin immediately after the observation with the maximum control chart statistic value.

#### **Likelihood Ratio Test Statistic**

The maximum value of twice the log-likelihood function for the first  $m_1$  observations is defined as follows:

$$l_1 = -m_1 k_1 \log[2\pi] - m_1 \log[|S_1|_{k_1}] - m_1 k_1$$

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The equation for  $l_1$  uses the following notation:

- $S_1$  is the maximum likelihood estimate of the covariance matrix for the first  $m_1$  observations.
- $k_1 = \text{Min}[p, m_1-1]$  is the rank of the  $p \times p$  matrix  $S_1$ .
- The notation  $|S_1|_{k_1}$  denotes the generalized determinant of the matrix  $S_1$ , which is defined as the product of its  $k_1$  positive eigenvalues  $\lambda_{j}$ :

$$\left|S_1\right|_{k_1} = \prod_{j=1}^{k_1} \lambda_j$$

The generalized determinant is equal to the ordinary determinant when  $S_1$  has full rank.

Denote the maximum of twice the log-likelihood function for the subsequent  $m_2 = m - m_1$  observations by  $l_2$ , and the maximum of twice the log-likelihood function for all m observations by  $l_0$ . Both  $l_2$  and  $l_0$  are given by expressions similar to that given for  $l_1$ .

The likelihood ratio test statistic compares the sum  $l_1 + l_2$  to  $l_0$ . The sum  $l_1 + l_2$  is twice the log-likelihood that assumes a possible shift at  $m_1$ . The value  $l_0$  is twice the log-likelihood that assumes no shift. If  $l_0$  is substantially smaller than  $l_1 + l_2$ , the process is assumed to be unstable.

The likelihood ratio test statistic for a test of whether a change begins at observation  $m_1 + 1$  is defined as follows:

$$\begin{split} & \text{Irt}[m_1] & = (l_1 + l_2 - l_0) \\ & = (m_1(p - k_1) + m_2(p - k_2))(1 + \log(2\pi)) \\ & + m \log[|S|] - m_1 \log\Big[\big|S_1\big|_{k_1}\Big] - m_2 \log\Big[\big|S_2\big|_{k_2}\Big] \end{split}$$

The distribution of the likelihood ratio test statistic is asymptotically chi-square distributed with p(p + 3)/2 degrees of freedom. Large log-likelihood ratio values indicate that the process is unstable.

#### The Control Chart Statistic

Simulations indicate that the expected value of  $lrt[m_1]$  varies based on the observation's location in the series, and, in particular, depends on p and m. See Sullivan and Woodall (2000).

Approximating formulas for the expected value of  $lrt[m_1]$  are derived by simulation. To reduce the dependence of the expected value on p,  $lrt[m_1]$  is divided by its asymptotic expected value, p(p + 3)/2.

**Multivariate Control Charts** 

The formulas for the approximated expected value of  $lrt[m_1]$  divided by p(p+3)/2 are defined as follows:

$$\operatorname{ev}[m,p,m_1] = \left( \begin{array}{c} a_p + m_1 b_{p'} & \text{if } m_1$$

where

$$a_p = -\frac{0.08684(p - 14.69)(p - 2.036)}{(p - 2)}$$

and

$$b_p = \frac{0.1228(p-1.839)}{(p-2)}$$

For p = 2, the value of ev[ $m_1p_2, m_1$ ] when  $m_1$  or  $m_2 = 2$  is 1.3505.

**Note:** The formulas above are not accurate for p > 12 or m < (2p + 4). In such cases, simulation should be used to obtain approximate expected values.

An approximate upper control limit that yields a false out-of-control signal with probability approximately 0.05, assuming that the process is stable, is calculated as follows:

$$UCL[m,p] \cong (3.338 - 2.115\log[p] + 0.8819(\log[p])^{2} - 0.1382(\log[p])^{3})$$

$$+ (0.6389 - 0.3518\log[p] + 0.01784(\log[p])^{3})\log[m].$$

Note that this formula depends on *m* and *p*.

The control chart statistic is defined to be twice the log of the likelihood ratio test statistic divided by p(p + 3), divided by its approximate expected value, and also divided by the approximate value of the control limit. Because of the division by the approximate value of the UCL, the control chart statistic can be plotted against an upper control limit of 1. The approximate control chart statistic is calculated as follows:

$$\hat{y}[m_1] = \frac{2 \text{lrt}[m_1]}{p(p+3)(\text{ev}[m,p,m_1] \text{UCL}[m,p])}$$

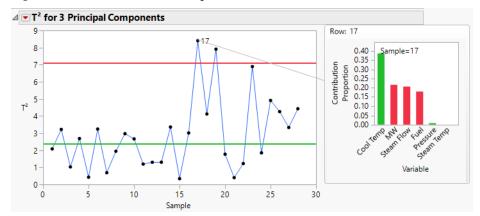
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# **Model Driven Multivariate Control Charts**

**Monitor and Diagnosis a Complex Process** 

Model-driven multivariate control charts are used to monitor parameters for multiple processes in a single control chart. The Model Driven Multivariate Control Chart (MDMVCC) platform enables you to build a control chart based on principal components or partial least squares models. For a set of continuous variables, the MDMVCC platform uses principal components to build the control chart. For saved principal components or partial least squares score functions, the MDMVCC platform builds a control chart based on the provided models. Use the MDMVCC platform to interactively explore and understand the underlying components that lead to out-of-control signals.

Figure 11.1 Model-driven Multiple Control Chart



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# Overview of Model Driven Multivariate Control Charts

The Model Driven Multivariate Control Chart (MDMVCC) platform has two primary functions: monitoring and diagnosing.

- Use multivariate control charts to monitor a multivariate process.
- You can interactively drill down to investigate the contributions of individual variables to the overall signal to diagnosis the process.

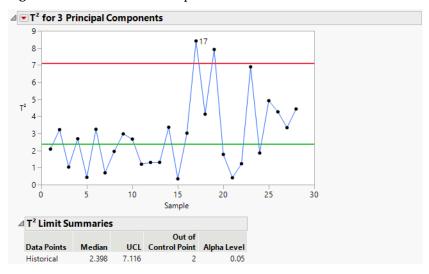
For more information about multivariate control charts, see Kourti and MacGregor (1996).

# **Example of Model Driven Multivariate Control Charts**

This example uses the Steam Turbine Historical.jmp sample data table that contains process variables from a steam turbine system. You want to build a control chart for the six monitored variables.

- 1. Select Help > Sample Data Library and open Quality Control/Steam Turbine Historical.jmp.
- 2. Select Analyze > Quality and Process > Model Driven Multivariate Control Chart.
- 3. Select all six columns, click **Process**, and click **OK**.

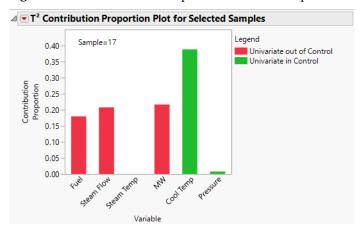
**Figure 11.2** Steam Turbine Report



Note that the process shifts after sample 16.

- 4. Select the sample 17 data point. Right-click and select **Rows > Row Label**.
- 5. Hover over the sample 17 data point to view the  $T^2$  contribution proportion plot for that point. Click on the plot to open the plot in the report window.

Figure 11.3 Contribution Proportion Plot for Sample 17



Note that Cool Temp contributes 40% of the  $T^2$  value. The Cool Temp bar is green indicating that sample 17 is within the univariate control limits for Cool Temp. Steam Flow and MW each contribute about 20% of the  $T^2$  value. They are both red, which indicates that sample 17 is outside of the univariate control limits for each variable. Steam Temp has a zero contribution to the  $T^2$  value. In this example, you found variables where the multivariate out-of-control sample could be traced to an out-of-control univariate variable. However, that is not always the case. In multivariate process control you may observe an out-of-control point on the  $T^2$  chart but find that the sample is in-control at the univariate level for all variables.

6. Hover over the Steam Flow bar in the contribution proportion plot to see a univariate control chart for Steam Flow. Click on the chart to open in a new report window.

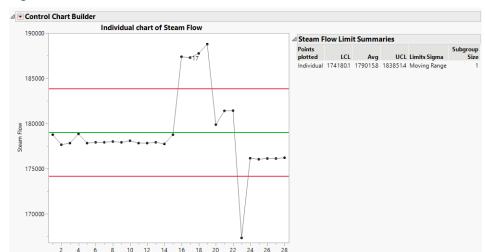
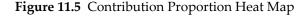
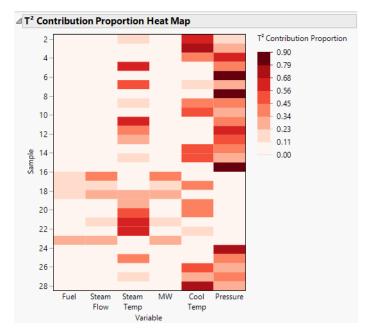


Figure 11.4 Individual Chart for Steam Flow

The individual chart indicates that the steam flow might have experienced an upset around sample 17. When control limits are specified in the Controls Limits column property, the individual chart respects those limits.

7. In the PCA Model Driven Multivariate Control Chart report window, Click the  $T^2$  for 3 Principal Components red triangle and select **Contribution Proportion Heat Map**.



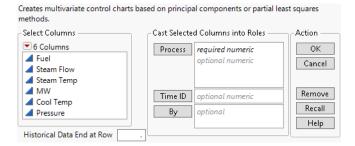


The contribution proportion heat map shows that there is a shift in the contribution proportions for rows 16, 17, and 18 and again at row 23 as compared to other rows. Generally, Steam Temp, Cool Temp, and Pressure contribute the most to the  $T^2$  value for each row.

# Launch the Model Driven Multivariate Control Chart Platform

Launch the Model Driven Multivariate Control Chart (MDMVCC) platform by selecting Analyze > Quality and Process > Model Driven Multivariate Control Chart.

Figure 11.6 The Model Driven Multivariate Control Chart Launch Window



For more information about the options in the Select Columns red triangle menu, see *Using JMP*.

The Model Driven Multivariate Control Chart platform launch window contains the following options:

**Process** Assigns the process columns. See "Data Format".

- **Time ID** Assigns a column that is used to identify samples. If no Time ID is assigned, the row number identifies the observations. If the Time ID column is a time, the time identifies each sample. Otherwise, the numeric value of the Time ID identifies each sample.
- **By** Produces a separate report for each level of the By variable. If more than one By variable is assigned, a separate report is produced for each possible combination of the By variables.
- **Historical Data End at Row** Specifies a row number to indicate where historical data end. This enables you to calculate chart limits based on historical data. Both historical and current data are plotted on the charts. Historical data are also known as Phase I data, and current data are also known as Phase II data.

#### **Data Format**

The MDMVCC platform accepts data in the following three allowable data formats:

- **Raw Data** Use continuous process data to build a control chart that is based on the principal components of the data. The default dimension of the control chart is based on the number of principal components that account for 85% of the process variation. This number is based on the cumulative percent of the principal component eigenvalues.
- **Principal Components** Use principal component columns that were previously saved from a principal component analysis (PCA). The default dimension of the control chart is the number of components specified as process variables.
- **Partial Least Squares Score Data** Use score columns that were previously saved from a partial least squares (PLS) analysis to build a control chart that is based on the score columns. The default dimension of the control chart is the number of scores specified as process variables.

#### Notes:

- PCA or PLS models built with a frequency or weight column are not supported.
- PCA or PLS models built with historical data must use the same number of historical data rows as specified in the MDMVCC launch window.
- PCA models built from within the Multivariate platform are not supported.

# The Model Driven Multivariate Control Chart Report

The initial Model Driven Multivariate Control Chart Report shows a  $T^2$  control chart. The hover labels on the chart are themselves charts. Click the hover label charts to open larger versions of the charts. Depending on the chart, they open in a separate report window or in the Diagnosis the Process section of the MDMVCC report. You can use the graphlets to interactively drill down into the data.

Row: 17 8 0.40 Sample=17 0.35 Contribution 0.30 0.25 6 0.20 0.15 4 Variable 0 10 15 20 25 30 Sample

Figure 11.7 MDMVCC Report with a Hover Graphlet

# Model Driven Multivariate Control Chart Platform Options

**Show History Summary Statistics** Shows or hides summary statistics for rows designated as historical data or all rows if historical data rows are not specified. Summary statistics include univariate means and standard deviations for process variables. For PCA-based charts, the eigenvalues and eigenvectors are displayed. For charts based on PLS scores, the standard deviation of scores and the score loadings are displayed.

#### **Monitor the Process**

**Show Monitoring Plots** Shows or hides the selected process monitoring plots.

**Set Component** Enables you to set the number of components for the  $T^2$ , DModX, or SPE plots. The number of components can range from one up to the number of valid eigenvectors for PCA driven analysis or from one up to the number of PLS model factors for PLS driven analysis.

**Set**  $\alpha$  **Level** Enables you to adjust the alpha level that is used for all control chart limits.

Model Driven Multivariate Control Chart Platform Options

- $T^2$  Plot Shows or hides a  $T^2$  plot. The  $T^2$  statistic is a summary of multivariate variation that measures how far away an observation is from the center of a PCA or PLS model.
- **Normalized DModX Plot** Shows or hides a plot of the normalized DModX values. DModX measures the distance of each observation to the PCA or PLS model. A high DModX value indicates an observation that deviates from the underlying correlation structure of the data.
- **Squared Prediction Error Plot** Shows or hides the squared prediction error (SPE) plot. SPE measures the sum of squared of the residuals from the PCA or PLS model. A high SPE value indicates an observation that deviates from the underlying correlation structure of the data.
- **Score Plot** Shows or hides a score plot of principal components or partial least squares factors. See "Score Plot".
- **Diagnose the Process** (Available when at least one diagnostic plot is active.) Shows or hides diagnostic plots.
- See *Using JMP* for more information about the following options:
- **Redo** Contains options that enable you to repeat or relaunch the analysis. In platforms that support the feature, the Automatic Recalc option immediately reflects the changes that you make to the data table in the corresponding report window.
- **Save Script** Contains options that enable you to save a script that reproduces the report to several destinations.
- **Save By-Group Script** Contains options that enable you to save a script that reproduces the platform report for all levels of a By variable to several destinations. Available only when a By variable is specified in the launch window.

## **Plot Options**

The following options apply to the  $T^2$ , Normalized DModX, Squared Prediction Error, and Score Plots. The plots, when selected, appear in the Diagnosis the Process section of the report window.

- **Show Limit Summaries** (Not available for the Score Plot.) Shows or hides control chart limits and summary data in a report table below the chart.
- **Contribution Heat Map** Shows or hides a heat map that is colored by the variable contributions of each observation.
- **Contribution Proportion Heat Map** Shows or hides a heat map that is colored by the variable contributions expressed as proportions of the overall value of each observation.

- **Contribution Plot for Selected Samples** (Available only when one or more points are selected.) Shows or hides a bar chart of the individual component contributions to the overall value for each selected sample.
- **Contribution Proportion Plot for Selected Samples** (Available only when one or more points are selected.) Shows or hides a bar chart of the individual component contributions expressed as proportions of contribution of the overall value for each selected sample.
- **Mean Contribution Proportion Plot for Selected Samples** (Available only when two or more points are selected.) Shows or hides a bar chart of the average of the individual component contributions to the overall value for each selected sample.

**Note:** Bars are green if the value or mean value is within 3 sigma of the mean. Bars are red if the value or mean value is beyond 3 sigma of the mean. When control limits are specified in the Controls Limits column property, the bar coloring respects those limits.

The following options are available for contribution plots:

- **Sort Bars** Enables you to sort the bars from largest to smallest contribution or from largest to smallest average contribution for multiple plots.
- **Label Bars** Enables you to label the bars by the value, the column name, or to remove labels (No Label).
- **Control Charts for Selected Items** Shows a control chart for the selected columns. When control limits are specified in the Controls Limits column property, the individual chart respects those limits.
- **Scatterplot Matrix** (Available when two or more bars are selected.) Shows a scatterplot matrix for the selected variables.
- **Remove Plot** Removes the plot from the report window.
- **Normalized Score Plot for Selected Samples** (Available only for a Score Plot when one or more points are selected.) Shows or hides a bar chart of normalized scores for each sample selected.
- **Score Ellipse Coverage** (Available only for Score Plots with two components.) Adds an ellipse with the specified coverage to the score plot. The ellipse is based on historical data. When both Phase I and Phase II data are present, there is an ellipse for each phase and the Phase II ellipse is dashed.
- **Connect Points** (Available only for Score Plots.) Connects data points in the score plot.
- **Show Loadings** (Available only for Score Plots.) Shows the PCA loadings on the score plot using biplot arrows.
- **Save Columns** For each plot there are three options to save values to the data table:

Quality and Process Methods

**Save Values** Saves values ( $T^2$ , Normalized DModX, SPE, or scores) to a new data table column.

**Save Contributions** Saves contributions to new data table columns.

**Save Contribution Proportions** Saves contribution proportions to new data table columns.

#### Score Plot

The Score Plot displays a plot of principal components or partial least squares factors. Use the controls below the plot to change the components shown in the Score Plot.

Use the buttons to the right of the plot to assign and compare the relative contributions between two groups of points. Relative contributions show how two or more samples differ from each other. Relative contributions show what changes in the underlying process variables contribute to differences in groups of samples. One use is to investigate the differences between an in-control sample and an out-of-control sample.

Group A is the reference group and Group B the comparator group. Each group can consist of one or more points. To assign the reference group, select one or more points and then click Group A. To assign the comparator group, select one or more points and then click Group B. To display the Relative Score Contribution Plot, click Compare.

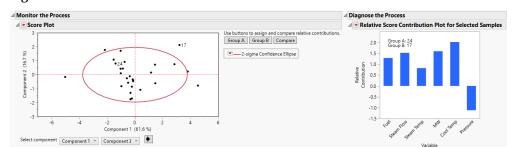


Figure 11.8 Score Plot with Relative Contribution Plot for Row 17 Relative to Row 24

# Additional Examples of the Model Driven Multivariate Control Chart Platform

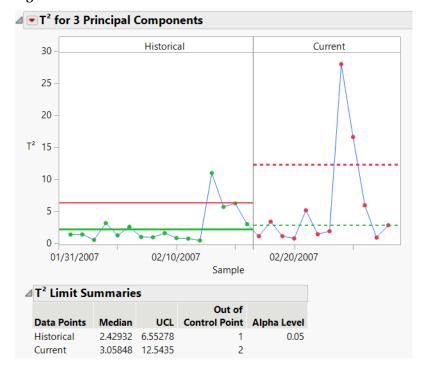
- "Example of an MDMVCC with Historical Data"
- "Example of an MDMVCC with a PLS Model"

# **Example of an MDMVCC with Historical Data**

This example demonstrates the use of historical data to set the monitoring limits for current data.

- 1. Select **Help > Sample Data Library** and open Quality Control/Flight Delays.jmp.
- 2. Select Analyze > Quality and Process > Model Driven Multivariate Control Chart.
- 3. Select the AA through WN and click **Process**.
- 4. Select Flight Date and click **Time ID**.
- 5. Enter 16 for Historical Data End at Row.
- 6. Click **OK**.

**Figure 11.9** *T*<sup>2</sup> Chart for Historical and Current Data



Note that there are two sets of limits. One set applies to the historical data. A second set of limits applies to the current data. For more information about how the historical data is used to calculate the two sets of limits, see "Limits".

**Tip:** Turn on Automatic Recalc to enable the chart to automatically update as you add additional observations to the data table. The Automatic Recalc option is under redo when you click the PCA Model Driven Multivariate Control Chart red triangle.

# **Example of an MDMVCC with a PLS Model**

This example demonstrates the use of a PLS model for monitoring a multivariate process. Consider a process with 14 inputs and 5 quality variables. You have a PLS model that explains the process and you want to use this model to monitor the process for deviations.

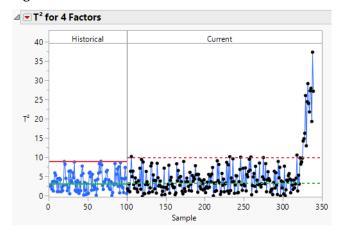
1. Select **Help > Sample Data Library** and open Polyethylene Process.jmp.

This data table contains 14 process variables and 5 quality or output variables. The first 100 rows are historical data used to build a PLS model to describe the process. These rows are colored blue. The remaining 239 rows are data collected since the model was built.

The partial least squares model finds 4 score functions that describe the process. These functions are saved to the data table in columns X Score 1 Formula to X Score 4 Formula. To build the PLS model, use the table script *Set current data as excluded* to exclude the 239 rows of data collected after the historical data. Then use the *Fit Partial Least Squares* table script to build the PLS model to relate the quality variable to the process variables.

- 2. Select Analyze > Quality and Process > Model Driven Multivariate Control Chart.
- Select the X Score 1 Formula through X Score 4 Formula and click Process.
- Set the Historical Data End at Row to 100.
- 5. Click **OK**.

Figure 11.10  $T^2$  Chart

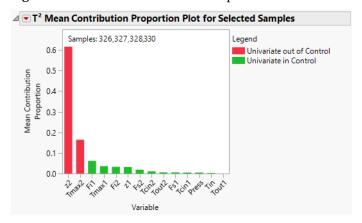


The blue data points represent the historical data. The black data points are data points collected after the control chart was established. The process experienced an upset that begins around sample number 326.

6. Hover over the sample data points that are above the upper control limit to view contribution plots.

- 7. Select the first cluster of data points above the upper control limit. Click the  $T^2$  for 4 Factors red triangle and select **Mean Contribution Proportion Plot for Selected Samples**.
- 8. Click the red triangle next to T2 Mean Contribution Proportion Plot for Selected Samples and select **Sort Bars**.

Figure 11.11 Mean Contribution Proportion Plot



Notice that the contributions plot is in terms of the PLS model input variables. It appears that z2 and Tmax2 are causing the process upset. Tmax2 and z2 are related. Tmax2 is a reactor temperature and z2 is the location of the Tmax2 temperature.

**Note:** The descriptions of the factors are recorded in the Notes column property.

# Statistical Details for the Model Driven Multivariate Control Chart Platform

# **Monitoring Statistics**

 $T^2$ 

The  $T_i^2$  value for each of the i observations is plotted on the  $T^2$  control chart. For historical and current data, the  $T^2$  values for a PCA or PLS model with k components are defined as:

$$T_i^2 = t_i^T S_k^{-1} t_i$$

where:

 $t_i$  = the vector of k scores for the i<sup>th</sup> observation

 $S_k$  = the diagonal sample covariance matrix of the k scores for historical observations

For PCA models,  $S_k$  is the diagonal eigenvalue matrix.

The mean of each of the k historical score vectors is 0 when the data is centered during the data preprocessing step. This step occurs in PCA on correlations or covariances and in PLS with centering. For preprocessing options where  $\mathbf{X}$  is not centered, the data is assumed to have been centered by the user, so the mean of each of the k score vectors is 0. For more information about Hotelling's  $T^2$ , see Montgomery (2013).

#### SPE

For both PCA and PLS models, the preprocessed **X** matrix can be decomposed as:

$$X = T_k P_k^T + E$$

where  $T_k = (t_1,...,t_k)$  is the k dimensional score matrix and  $P_k = (p_1,...,p_k)$  is a matrix with the first k eigenvectors for PCA models or the loading matrix for PLS models. The squared prediction error of this PCA or PLS model is used for the SPE control chart.

The  $SPE_i$  value for each of the i observations is plotted on the SPE control chart. The squared prediction error is defined as:

$$SPE_i = e_i^T e_i = \sum_{j=1}^p e_{ij}^2$$

where

 $e_i$  = the residual vector for observation i

p = number of variables

#### DModX

The  $DModX_i$  value for each of the i observations is plotted on the DModX control chart. The normalized distance to model (DModX) is defined as:

Statistical Details for the Model Driven Multivariate Control Chart Platform

$$DModX_{i} = \frac{SPE_{i}/(df_{1})}{\left(\sum_{i=1}^{n} SPE_{i}\right)/(df_{2})} = \frac{\sum_{j=1}^{p} e_{ij}^{2}/(df_{1})}{\sum_{i=1}^{n} \sum_{j=1}^{p} e_{ij}^{2}/(df_{2})} = \frac{\sum_{j=1}^{p} e_{ij}^{2}}{d}$$

where

 $e_{ij}$  = the residual for observation i and variable j

 $df_1 = p-k$ 

 $df_2 = (n-k-1)(p-k)$  if the data is centered and (n-k)(p-k) if the data is not centered

n = number of historical data observations

k = number of PCA/PLS components

p = number of variables

**Note:**  $DModX_i$  is equal to  $SPE_i$  scaled by 1/d.

#### Limits

All data are treated as historical data when the number of historical rows is not specified in the launch window. See "Launch the Model Driven Multivariate Control Chart Platform".

 $T^2$ 

The upper control limit (UCL) for historical data is based on the Beta distribution and defined as:

$$UCL = \frac{(n-1)^2}{n} \beta \left[ 1 - \alpha; \frac{k}{2}; \frac{n-k-1}{2} \right]$$

where:

n = number of historical data observations

k = number of PCA or PLS components

$$\beta \left[ 1 - \alpha; \frac{k}{2}; \frac{n-k-1}{2} \right] = (1-\alpha)^{\text{th}} \text{ quantile of a Beta} \left[ \frac{k}{2}; \frac{n-k-1}{2} \right] \text{ distribution.}$$

The UCL for current data is based on the *F* distribution and defined as:

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$$UCL = \frac{k(n+1)(n-1)}{n(n-k)}F[1-\alpha;k;(n-k)]$$

where:

n = number of historical data observations

k = number of PCA or PLS components

 $F(1-\alpha; k; n-k) = (1-\alpha)^{th}$  quantile of an F(k; n-k) distribution.

#### **DModX**

For PCA and PLS models, the UCL is based on the *F* distribution. The DModX UCL for PCA models is defined as:

$$UCL = F[1 - \alpha; df_1; df_2]$$

where:

$$df_1 = p-k$$

 $df_2 = (n-k-1)(p-k)$  if the data is centered and (n-k)(p-k) if the data is not centered

n = number of historical data observations

k = number of PCA components

p = number of variables

 $F(1-\alpha; n-p-1; p-k) = (1-\alpha)^{\text{th}}$  quantile of a F(n-p-1; p-k) distribution.

The DModX UCL for PLS models is defined as:

$$UCL = F[1 - \alpha; h; nh]$$

where:

$$h = (2\hat{\mu}_{SPE}^2)/(\hat{\sigma}_{SPE}^2)$$

 $\mu_{SPE}$  = historical sample mean of SPE

 $\hat{\sigma}_{SPE}^2$  = historical sample variance of SPE

n = number of historical data observations

 $F(1-\alpha; h; nh) = (1-\alpha)^{th}$  quantile of an F(h; nh) distribution.

#### **SPE**

The SPE UCL for PCA models is defined as:

$$UCL = \theta_1 \left[ 1 - \frac{\theta_2 h_0 (1 - h_0)}{\theta_1^2} + \frac{z_{1 - \alpha} (2\theta_2 h_0^2)^{1/2}}{\theta_1} \right]^{1/h_0}$$

where:

$$h_0 = 1 - 2\theta_1 \theta_3 / (3\theta_2^2)$$

$$\theta_1 = \sum_{a=1}^k \lambda_a$$

$$\theta_2 = \sum_{a=1}^k \lambda_a^2$$

$$\theta_3 = \sum_{a=1}^k \lambda_a^3$$

 $\lambda_a$  = the  $a^{th}$  eigenvalue

k = number of PCA components

 $z_{1-\alpha} = (1-\alpha)^{th}$  quantile of the standard normal distribution

For more information about SPE control limits for PCA models, see Jackson and Mudholkar (1979).

For PLS models, the UCL is based on the chi-square distribution and defined as:

$$UCL = g\chi^2_{[1-\alpha;h]}$$

where

$$g=(\hat{\sigma}_{SPE}^2)/(2\hat{\mu}_{SPE})$$

$$h = (2\hat{\mu}_{SPE}^2)/(\hat{\sigma}_{SPE}^2)$$

 $\mu_{SPE}$  = historical sample mean of SPE

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$$\hat{\sigma}_{SPE}^2$$
 = historical sample variance of SPE

$$\chi^2(1-\alpha; h) = (1-\alpha)^{th}$$
 quantile of an  $\chi^2(h)$  distribution

The g and h parameters are estimated by the method of moments. For more information about SPE control limits for PLS models, see Nomikos (1995).

### **Contributions**

 $T^2$ 

The  $T^2$  contributions for a PCA or PLS model with p variables and k components are calculated as:

$$\begin{split} T_{i}^{2} &= t_{i}^{T} S_{k}^{-1} t_{i} \\ &= \sum_{a=1}^{k} \frac{t_{ia}^{2}}{s_{a}} \\ &= \sum_{a=1}^{k} \frac{t_{ia}}{s_{a}} \sum_{j=1}^{p} r_{ja} x_{ij} \\ &= \sum_{j=1}^{p} \left( \sum_{a=1}^{k} \frac{t_{ia}}{s_{a}} r_{ja} x_{ij} \right) \end{split}$$

where:

 $t_i$  = the vector of k scores for the i<sup>th</sup> observation

 $S_k$  = the diagonal sample covariance matrix of the k scores for historical observations. For PCA models,  $S_k$  is the diagonal eigenvalue matrix.

 $s_a$  = the  $a^{th}$  diagonal element of  $\mathbf{S}_k$ 

 $r_{ja}$  = the  $j^{th}$  element of the  $a^{th}$  eigenvector for PCA models and the  $a^{th}$  column of the  $\mathbf{R}_k$  loading matrix for PLS models.  $\mathbf{R}_k$  is the matrix used to relate the score matrix,  $\mathbf{T}_k$  to the  $\mathbf{X}$  matrix, such that  $\mathbf{T}_k$ = $\mathbf{X}\mathbf{R}_k$ .

 $x_{ii}$  = the value of the  $j^{th}$  variable for the  $i^{th}$  observation.

**Note:** The *p* terms in the last sum are the variable contributions.

The contribution of each variable is the sum of its contribution to each score, weighted by the normalized score value. A variable is considered to have a large contribution to  $T_i^2$  if there is a large normalized score value, and the variable contribution is large.

$$\sum_{j=1}^{p} Cont(T_i^2)_j = T_i^2$$

the contribution proportion of variable *j* is defined as:

$$ContProp(T_i^2)_j = \frac{Cont(T_i^2)_j}{p}$$

$$\sum_{j=1}^{p} Cont(T_i^2)_j$$

**Note:** When computing  $T^2$  contribution proportions, JMP zeros out negative contributions. Negative contributions are possible due to the interaction of variables during the projection of **X** in PCA and PLS models. The negative contributions are zeroed in order to identify the variable contributions that represent a large proportion of the total positive contributions.

For more information about PCA contributions and negative contributions, see Kourti and MacGregor (1996). For more information about PLS contributions, see Li et al. (2009).

#### **DModX**

For PCA and PLS models, the contribution of variable i to  $DModX_i$  is defined as:

$$Cont(DModX_i)_j = \frac{e_{ij}}{\sqrt{d}}$$

Note that since

$$DModX_{i} = \sum_{j=1}^{p} \frac{e_{ij}^{2}}{d}$$

the contribution proportion of variable j is defined as:

$$ContProp(DModX_i)_j = \frac{e_{ij}^2/d}{DModX_i}$$

#### SPE

For PCA and PLS models, the contribution of variable j to  $SPE_i$  is defined as:

$$Cont(SPE_i)_j = e_{ij}$$

Note that since

$$SPE_i = \sum_{j=1}^{p} e_{ij}^2$$

the contribution proportion of variable *j* is defined as:

$$ContProp(SPE_i)_j = \frac{e_{ij}^2}{SPE_i}$$

#### **Score Contributions**

The score contribution computation is the same as  $T^2$  contributions but are computed only for the dimensions selected in the score plot.

## Score Plot Group Comparisons

For the score plot group comparisons, the relative score contribution for variable *j* is the difference between the average contribution in group B and the average contribution in group A:

$$\sum_{i \in B} \frac{Cont(T_i^*)_j}{n_b} - \sum_{i \in A} \frac{Cont(T_i^*)_j}{n_a}$$

where

 $T_i^*$  = the  $i^{th}$  row of the score matrix with columns corresponding to the dimensions shown in the score plot.

A =the set of observations in group A

B = the set of observations in group B

 $n_a$  = the number of observations in group A

 $n_b$  = the number of observations in group B.

## **Score Plot Loadings**

The loadings shown on the score plot are based on PCA eigenvectors or PLS X score loadings (**R** matrix). These loadings are scaled by the maximum absolute value of scores. The scaling is performed in order to graph the loadings on the score plot. The loadings illustrate each variable's approximate influence on each score.

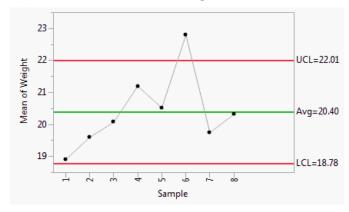
# **Legacy Control Charts**

### **Create Variable and Attribute Control Charts**

A control chart is a graphical and analytic tool for monitoring process variation. The natural variation in a process can be quantified using a set of control limits. Control limits help distinguish common-cause variation from special-cause variation. Typically, action is taken to identify and eliminate special-cause variation. It is also important to quantify the common-cause variation in a process, as this determines the capability of a process.

The legacy control chart platforms in JMP provide a variety of control charts, as well as runs charts, V-Mask CUSUM charts, and weighted moving average charts. To support process improvement initiatives, most of the control chart options display separate control charts for different phases of a project on the same chart.

Figure 12.1 Control Chart Example



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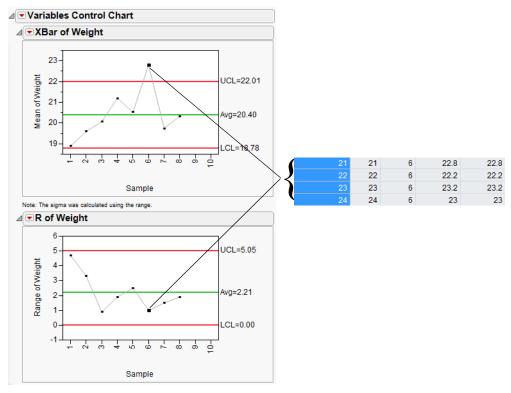
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# **Example of a Legacy Control Chart**

This example uses the Coating.jmp sample data table in the Quality Control sample data folder (taken from the *ASTM Manual on Presentation of Data and Control Chart Analysis*). The quality characteristic of interest is the Weight column. A subgroup sample of four is chosen.

- 1. Select **Help > Sample Data Library** and open Quality Control/Coating.jmp.
- Select Analyze > Quality And Process > Legacy Control Charts > XBar.
   Note the selected chart types of XBar and R.
- 3. Select Weight and click **Process**.
- 4. Select Sample and click Sample Label.
- 5. Click **OK**.

Figure 12.2 Variables Charts for Coating Data



An XBar chart and an R chart for the process are shown in Figure 12.2. Sample six indicates that the process is not in statistical control. To check the sample values, click the sample six summary point on either control chart. The corresponding rows highlight in the data table.

**Note:** If an S chart is chosen with the XBar chart, then the limits for the XBar chart are based on the standard deviation. Otherwise, the limits for the XBar chart are based on the range.

# **Legacy Control Chart Types**

Legacy control charts are broadly classified into two categories:

- "Control Charts for Variables" IR, XBar, Runs Chart, Levey-Jennings, Presummarize, CUSUM, UWMA, and EWMA.
- "Control Charts for Attributes" P, NP, C, and U.

### **Control Charts for Variables**

Control charts for variables are classified according to the subgroup summary statistic plotted on the chart:

- The **IR** selection provides additional chart types:
  - Individual Measurement charts display individual measurements. These charts are appropriate when only one measurement is available for each subgroup sample.
  - Moving Range charts display moving ranges of two or more successive measurements.
     See "Moving Range (Average) Charts".
- **XBar** charts display subgroup means (averages). This selection provides additional chart types:
  - **R** charts display subgroup ranges (maximum minimum).
  - **S** charts display subgroup standard deviations.

For quality characteristics measured on a continuous scale, a typical analysis shows both the process mean and its variability with a mean chart aligned above its corresponding R or S chart.

- Runs Chart displays data as a connected series of points. Runs charts can also plot the
  group means when the Sample Label role is used, either on the window or through a
  script.
- **Levey-Jennings** charts show a process mean with control limits based on a long-term sigma. The control limits are placed at 3s distance from the center line. The standard deviation, s, for the Levey-Jennings chart is calculated the same way standard deviation is in the Distribution platform.
- Presummarize charts display subgroup means and standard deviations. See "Presummarize Charts".

- CUSUM charts show cumulative sums of subgroup or individual measurements from a target value. See "V-Mask CUSUM Control Charts".
- UWMA charts show a uniformly weighted moving average of a specified number of measurements. See "Uniformly Weighted Moving Average Charts".
- EWMA charts show an exponentially weighted moving average of all measurements with a specified weight. See "Exponentially Weighted Moving Average Charts".

### Moving Range (Average) Charts

In a Moving Average chart, the quantities that are averaged can be individual observations instead of subgroup means. However, a Moving Average chart for individual measurements is not the same as a control chart for individual measurements or moving ranges with individual measurements plotted.

Moving Range (Average) charts display moving ranges of two or more successive measurements. Moving ranges are computed for the number of consecutive measurements that you enter in the **Range Span** box. The default range span is 2. Because moving ranges are correlated, these charts should be interpreted with care.

A Median Moving Range chart is also available. If you choose a Median Moving Range chart and an Individual Measurement chart, the limits on the Individual Measurement chart use the Median Moving Range as the sigma, rather than the Average Moving Range.

#### **Presummarize Charts**

If your data consist of repeated measurements of the same process unit, you can combine these into one measurement for the unit. Pre-summarizing is not recommended unless the data have repeated measurements on each process or measurement unit.

Presummarize summarizes the process column into sample means or standard deviations, based either on the sample size or sample label chosen. Then it charts the summarized data based on the options chosen in the launch window. You can also append a capability analysis by checking the appropriate box in the launch window.

The **Presummarize** launch window has the following options for chart types:

- Individual on Group Means
- Individual on Group Std Devs
- Moving Range on Group Means
- Moving Range on Group Std Devs
- Median Moving Range on Group Means
- Median Moving Range on Group Std Devs

There is also an option for setting the range span that is used for the moving range chart types.

#### V-Mask CUSUM Control Charts

V-Mask Cumulative Sum (CUSUM) control charts show cumulative sums of subgroup or individual measurements from a target value. V-Mask CUSUM charts can help you decide whether a process is in a state of statistical control by detecting small, sustained shifts in the process mean. In comparison, standard Shewhart control charts can detect sudden and large changes in measurement, such as a two or three sigma shift, but they are less effective at spotting smaller changes, such as a one sigma shift.

The **CUSUM** menu selection has options for V-mask cumulative sum charts. In addition to KSigma, you also specify:

- The vertical distance *h* between the origin for the V-mask and the upper or lower arm of the V-mask for a two-sided chart. For a one-sided chart, H is the decision interval. Choose H as a multiple of the standard error.
- The reference value *k*, where *k* is greater than zero.

Another form of a cumulative sum control chart is the tabular CUSUM chart. To create a tabular CUSUM chart, see "CUSUM Control Charts". The tabular CUSUM chart is recommended over the V-mask chart for a variety of reasons, including the following:

- The V-mask must be moved with each observation, not simply placed on the last observation.
- The cumulative sums in the V-mask procedure can end up a long way from the center of the graph, even for an on-target process.

Caution: Montgomery (2013) strongly "advises against using the V-mask procedure."

### **Uniformly Weighted Moving Average Charts**

Each point on a Uniformly Weighted Moving Average (UWMA) chart is the average of the w most recent subgroup means, including the present subgroup mean. When you obtain a new subgroup sample, the next moving average is computed by dropping the oldest of the previous w subgroup means and including the newest subgroup mean. The constant, w, is called the span of the moving average.

In addition to KSigma and Alpha, in the UWMA launch window you also specify:

• The Moving Average Span, or w, which indicates how many subgroups to include to form the moving average. The larger the Moving Average Span (w), the smoother the UWMA line, and the less it reflects the magnitude of shifts. This means that larger values of w guard against smaller shifts. See "Control Limits for UWMA Charts".

### **Exponentially Weighted Moving Average Charts**

Each point on an Exponentially Weighted Moving Average (EWMA) chart is the weighted average of all the previous subgroup means, including the mean of the present subgroup sample. The weights decrease exponentially going backward in time.

**Note:** An Exponentially Weighted Moving Average (EWMA) chart can also be called a Geometric Moving Average (GMA) chart.

In addition to KSigma and Alpha, in the EWMA launch window you also specify:

 A Weight parameter, which is the weight (0 < weight ≤ 1) assigned to the present subgroup sample mean. Small values of Weight are used to guard against small shifts. See "Control Limits for EWMA Charts".

**Tip:** See "EWMA Control Charts" for the newer EWMA Control Charts platform.

### **Control Charts for Attributes**

In the previous types of charts, measurement data was the process variable. This type of data is often continuous, and the charts are based on theory for continuous data. Another type of data is count data, where the variable of interest is a discrete count of the number of defects or blemishes per subgroup. For discrete count data, attribute charts are applicable, as they are based on binomial and Poisson models. Because the counts are measured per subgroup, it is important when comparing charts to determine whether you have a similar number of items in the subgroups between the charts. Attribute charts, like variables charts, are classified according to the subgroup sample statistic plotted on the chart.

### **Determining Which Attribute Chart to Use**

Each item is judged as either conforming or non-conforming:

**p-chart** Shows the *proportion* of defective items.

**np-chart** Shows the *number* of defective items.

The number of defects is counted for each item:

**c-chart** Shows the *number* of defects.

**u-chart** Shows the *proportion* of defects.

For attribute charts, specify the column containing the defect count or defective proportion as the Process variable. The data are interpreted as counts, unless the column contains non-integer values between 0 and 1.

- P charts display the proportion of nonconforming (defective) items in subgroup samples, which can vary in size. Since each subgroup for a P chart consists of N<sub>i</sub> items, and an item is judged as either conforming or nonconforming, the maximum number of nonconforming items in a subgroup is N<sub>i</sub>.
- NP charts display the number of nonconforming (defective) items in subgroup samples.
   Because each subgroup for an NP chart consists of N<sub>i</sub> items, and an item is judged as either conforming or nonconforming, the maximum number of nonconforming items in subgroup i is N<sub>i</sub>.

**Note:** To use the Sigma column property for P or NP charts, the value needs to be equal to the proportion. JMP calculates the sigma as a function of the proportion and the sample sizes.

• C charts display the number of nonconformities (defects) in a subgroup sample that usually, but does not necessarily, consists of one inspection unit.

**Caution:** For a C chart, if you do not specify a Sample Size or Constant Size, then the Sample Label is used as the sample size.

• U charts display the proportion of nonconformities (defects) in each subgroup sample that can have a varying number of inspection units.

**Caution:** For a U chart, if you do not specify a Unit Size or Constant Size, then the Sample Label is used as the unit size.

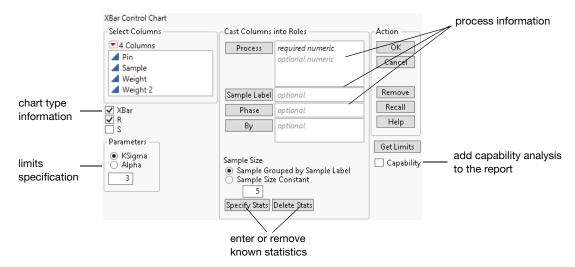
# **Launch a Legacy Control Chart Platform**

When you launch a legacy control chart platform by selecting **Analyze > Quality And Process > Legacy Control Charts**, a launch window similar to Figure 12.3 appears. The specific controls vary depending on which type of chart you select. Initially, the window shows the following types of information:

- "Process Information" for measurement variable selection
- Chart type information (for more information, see "Legacy Control Chart Types")
- "Limits Specifications"
- "Specified Statistics"

Launch a Legacy Control Chart Platform

Figure 12.3 XBar Control Chart Launch Window



For more information about the options in the Select Columns red triangle menu, see *Using IMP*.

### **Process Information**

The launch window displays a list of columns in the current data table. Here, you specify the variables to be analyzed and the subgroup sample size.

#### **Process**

The **Process** role selects variables for charting:

- For variables charts, specify measurements as the process.
- For attribute charts, specify the defect count or defective proportion as the process. The data are interpreted as counts, unless it contains non-integer values between 0 and 1.

**Note:** The rows of the data table must be sorted in the order in which the observations were collected. Even if there is a **Sample Label** variable specified, you still must sort the observations accordingly.

### Sample Label

The **Sample Label** role enables you to specify a variable whose values label the horizontal axis and can also identify unequal subgroup sizes. If you do not specify a sample label variable, the samples are identified by their subgroup sample number.

- If the sample subgroups are the same size, select the **Sample Size Constant** option and enter the size in the text box. If you entered a Sample Label variable, its values are used to label the horizontal axis. The sample size is used in the calculation of the limits regardless of whether the samples have missing values.
- If the sample subgroups have an unequal number of rows or have missing values and you
  have a column identifying each sample, select the Sample Grouped by Sample Label
  option and enter the sample identifying column as the sample label.

For attribute charts (P, NP, C, and U charts), this variable is the subgroup sample size. Additional options appear on the launch window, including **Sample Size**, **Constant Size**, or **Unit Size**, depending on your selection. In variables charts, it identifies the sample. When the chart type is **IR**, a **Range Span** text box appears. The *range span* specifies the number of consecutive measurements from which the moving ranges are computed.

#### Notes:

- The rows of the data table must be sorted in the order in which the observations were collected. Even if there is a **Sample Label** variable specified, you still must sort the observations accordingly.
- The non-integer part of the value for **Constant Size** is truncated. If you have a constant non-integer subgroup sample size, you must specify a column of constant values.

Launch a Legacy Control Chart Platform

The illustration in Figure 12.4 shows an XBar chart for a process with unequal subgroup sample sizes, using the Coating.jmp sample data from the Quality Control sample data folder.

XBar Control Chart Select Columns Cast Columns into Roles Action 4 Columns Process ■ Weight 2 ОК Pin optional numeric Cancel Sample Weight Weight 2 Remove Sample Label | 🚄 Sample Recall ✓ XBar ✓ R □ S Phase Help optional Ву **Parameters** Get Limits KSiqma Sample Size Capability Alpha 🗨 Sample Grouped by Sample Label 3 **▼**XBar of Weight 2 Specify UCL Mean of Weight Avq=20.36 20 19 5 Sample

Note: The sigma was calculated using the range

Figure 12.4 Variables Charts with Unequal Subgroup Sample Sizes

#### **Phase**

The **Phase** role enables you to specify a column identifying different phases, or sections. A *phase* is a group of consecutive observations in the data table. For example, phases might correspond to time periods during which a new process is brought into production and then put through successive changes. Phases generate, for each level of the specified Phase variable, a new sigma, set of limits, zones, and resulting tests.

On the window for XBar, R, S, IR, P, NP, C, U, Presummarize, and Levey-Jennings charts, a **Phase** variable button appears. If a phase variable is specified, the phase variable is examined, row by row, to identify to which phase each row belongs. Saving to a limits file reveals the sigma and specific limits calculated for each phase.

#### By

The **By** role identifies a variable to produce a separate analysis for each value that appears in the column.

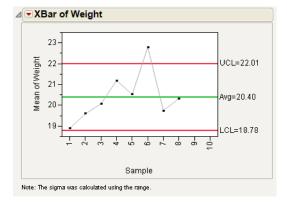
## **Limits Specifications**

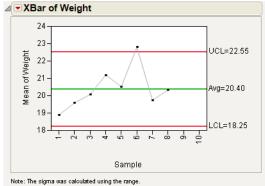
You can specify computations for control limits by entering a value for k (**K Sigma**), or by entering a probability for  $\alpha$  (**Alpha**), or by retrieving a limits value from the process columns' properties or a previously created Limits Table. Limits Tables and the **Get Limits** button are discussed in the section "Saving and Retrieving Limits". There must be a specification of either **K Sigma** or **Alpha**. The window default for **K Sigma** is 3.

### **KSigma**

The **KSigma** parameter option enables specification of control limits in terms of a multiple of the sample standard error. **KSigma** specifies control limits at k sample standard errors above and below the expected value, which shows as the center line. To specify k, the number of sigmas, click the radio button for **KSigma** and enter a positive k value into the text box. The usual choice for k is 3, which is three standard deviations. The examples shown in Figure 12.5 compare the XBar chart for the Coating.jmp data with control lines drawn with **KSigma** = 3 and **KSigma** = 4.

Figure 12.5 K Sigma =3 (left) and K Sigma=4 (right) Control Limits





### Alpha

The **Alpha** parameter option specifies control limits (also called *probability limits*) in terms of the probability  $\alpha$  that a single subgroup statistic exceeds its control limits, assuming that the process is in control. To specify alpha, click the **Alpha** radio button and enter the desired probability. Reasonable choices for  $\alpha$  are 0.01 or 0.001. For XBar charts under the assumption of normality and known in-control parameters, the **Alpha** value equivalent to a **KSigma** of 3 is 0.0027.

## **Specified Statistics**

After specifying a process variable, if you click the **Specify Stats** (when available) button on a Control Chart launch window, a tab with editable fields is appended to the bottom of the window. This lets you enter historical statistics (that is, statistics obtained from historical data) for the process variable. The Control Chart platform uses those entries to construct control charts. The example here shows 1 as the standard deviation of the process variable and 20 as the mean measurement.

Figure 12.6 Example of Specify Stats



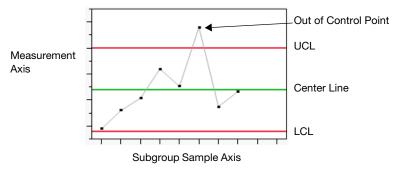
**Note:** When the mean is user-specified, it is labeled in the plot as  $\mu$ 0.

If you check the **Capability** option on a Control Chart launch window (Figure 12.3), a window appears as the platform is launched asking for specification limits. The standard deviation for the control chart selected is sent to the window and appears as a Specified Sigma value, which is the default option. After entering the specification limits and clicking OK, capability output appears in the same window next to the control chart. For information about how the capability indices are computed, see "Capability Indices for Normal Distributions".

# **Legacy Control Chart Reports**

The analysis produces a chart that can be used to determine whether a process is in a state of statistical control. The report varies depending on the type of chart that you select. Figure 12.7 displays the parts of a simple control chart. Control charts update dynamically as data is added or changed in the data table.

Figure 12.7 Example of a Control Chart



**Note:** Any rows that are excluded in the data table are also hidden in Runs charts, P charts, U charts, and C charts.

Control charts have the following characteristics:

- Each point plotted on the chart represents an individual process measurement or summary statistic. In Figure 12.7, the points represent the average for a sample of measurements.
  - Subgroups should be chosen *rationally*, that is, they should be chosen to maximize the probability of seeing a true process change *between* subgroups. Often, this requires knowledge of the process to determine the most effective grouping strategy. See Wheeler (2004); Woodall and Adams (1998).
- The vertical axis of a control chart is scaled in the same units as the summary statistic.
- The horizontal axis of a control chart identifies the subgroup samples and is time ordered. Observing the process over time is important in assessing if the process is changing.
- The green line is the center line, or the average of the data. The center line indicates the average (expected) value of the summary statistic when the process is in statistical control. Measurements should appear equally on both sides of the center line. If not, this is possible evidence that the process average is changing.
- The two red lines are the upper and lower control limits, labeled UCL and LCL. These limits give the range of variation to be expected in the summary statistic when the process is in statistical control. If the process is exhibiting only routine variation, then all the points

should fall randomly in that range. In Figure 12.7, one measurement is above the upper control limit. This is evidence that the measurement could have been influenced by a special cause, or is possibly a defect.

• A point outside the control limits (or the V-mask of a CUSUM chart) signals the presence of a special cause of variation.

Options within each platform create control charts that can be updated dynamically as samples are received and recorded or added to the data table.

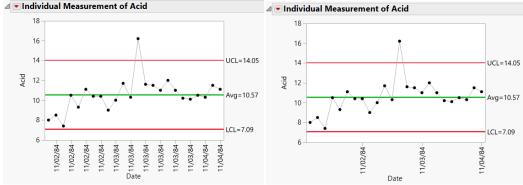
When a control chart signals abnormal variation, action should be taken to return the process to a state of statistical control if the process degraded. If the abnormal variation indicates an improvement in the process, the causes of the variation should be studied and implemented.

When you double-click the horizontal or vertical axis, the appropriate Axis Specification window appears for you to specify the format, axis values, number of ticks, gridline, reference lines, and other options to display on the axis.

For example, the Pickles.jmp data lists measurements taken each day for three days. In Figure 12.8, by default, the horizontal axis is labeled at every other tick. Sometimes this gives redundant labels, as shown to the left in Figure 12.8. If you specify a label at an increment of eight, the horizontal axis is labeled once for each day, as shown in the chart on the right.

Figure 12.8 Example of Labeled x Axis Tick Marks

Individual Measurement of Acid



**Tip:** For information about warnings and rules, see "Tests" and "Westgard Rules".

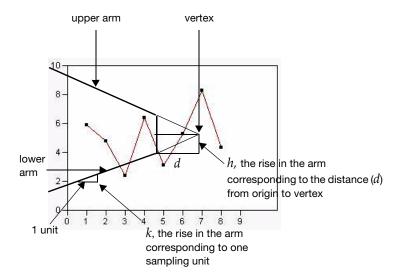
# V-Mask CUSUM Chart Reports

## Interpret a Two-Sided V-Mask CUSUM Chart

Note: See also "V-Mask CUSUM Chart Example".

To interpret a two-sided CUSUM chart, compare the points with limits that compose a V-mask. A V-mask is a shape in the form of a V on its side that is superimposed on the graph of the cumulative sums. The V-mask is formed by plotting V-shaped limits. The origin of a V-mask is the most recently plotted point, and the arms extended backward on the horizontal axis, as in Figure 12.9. As data are collected, the cumulative sum sequence is updated and the origin is relocated at the newest point.

Figure 12.9 V-Mask for a Two-Sided CUSUM Chart



Shifts in the process mean are visually easy to detect on a CUSUM chart because they produce a change in the slope of the plotted points. The point where the slope changes is the point where the shift occurs. A condition is *out-of-control* if one or more of the points previously plotted crosses the upper or lower arm of the V-mask. Points crossing the lower arm signal an increasing process mean, and points crossing the upper arm signal a downward shift.

There are important differences between CUSUM charts and Shewhart charts:

- A Shewhart control chart plots points based on information from a single subgroup sample. In CUSUM charts, each point is based on information from all samples taken up to and including the current subgroup.
- On a Shewhart control chart, horizontal control limits define whether a point signals an out-of-control condition. On a CUSUM chart, the limits can be either in the form of a V-mask or a horizontal decision interval.
- The control limits on a Shewhart control chart are commonly specified as  $3\sigma$  limits. On a CUSUM chart, the limits are determined from average run length.

A CUSUM chart is more efficient for detecting small shifts in the process mean. Lucas (1976) states that a V-mask detects a  $1\sigma$  shift about four times as fast as a Shewhart control chart.

## Interpret a One-Sided CUSUM Chart

Use a one-sided CUSUM chart to identify data approaching or exceeding the side of interest.

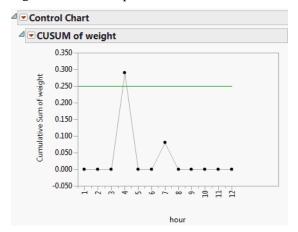


Figure 12.10 Example of a One-Sided CUSUM Chart

The *decision interval* or horizontal line is set at the H value that you entered in the launch window. In this example, it is 0.25. Any values exceeding the decision interval of 0.25 indicate a shift or out-of-control condition. In this example, observation 4 appears to be where a shift occurred. Also note that no V-mask appears for one-sided CUSUM charts.

# **Legacy Control Chart Platform Options**

Legacy control charts have red triangle menus that affect various parts of the platform:

- The menu on the top-most title bar affects the whole platform window. Its items vary with the type of chart that you select. See "Window Options for Legacy Control Charts".
- There is a menu of items on the chart type title bar with options that affect each chart individually. See "Chart Options for Legacy Control Charts".

## **Window Options for Legacy Control Charts**

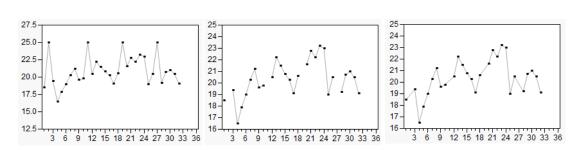
The red triangle menu on the window title bar lists options that affect the report window. If you request **XBar** and **R** at the same time, you can check each chart type to show or hide it. The specific options that are available depend on the type of control chart you request. Unavailable options show as grayed menu items.

**Show Limits Legend** Shows or hides the Avg, UCL, and LCL values to the right of the chart.

**Connect Through Missing** Connects points when some samples have missing values. In Figure 12.11, the left chart has no missing points. The middle chart has samples 2, 11, 19, and 27 missing with the points not connected. The right chart appears if you select the **Connect Through Missing** option, which is the default.

Figure 12.11 Example of Connected through Missing Option

No missing points Missing points are not connected Missing points are connected



**Use Median** For Runs Charts, when you select the **Show Center Line** option in the individual Runs Chart red triangle menu, a line is drawn through the center value of the column. The center line is determined by the **Use Median** setting of the main Runs Chart red triangle menu. When **Use Median** is selected, the median is used as the center line. Otherwise, the mean is used. When saving limits to a file, both the overall mean and median are saved.

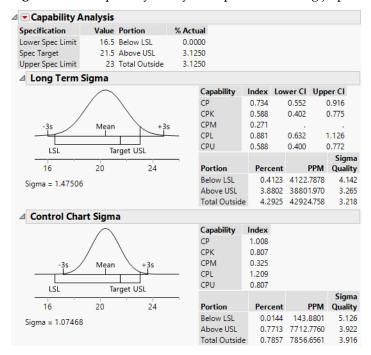
**Capability** (Not available when a Phase variable is specified.) Performs a Capability Analysis for your data. A pop-up window is first shown, where you can enter the Lower Spec Limit, Target, and Upper Spec Limit values for the process variable.

Figure 12.12 Capability Analysis Window



An example of a capability analysis report is shown in Figure 12.13 for Coating.jmp when the Lower Spec Limit is set as 16.5, the Target is set to 21.5, and the Upper Spec Limit is set to 23.

Figure 12.13 Capability Analysis Report for Coating.jmp



For additional information, see "Statistical Details for Capability Analysis".

**Save Sigma** Saves the computed value of sigma as a column property in the process variable column in the JMP data table.

**Save Limits** Saves the control limits in one of the following ways:

- **in Column** Saves control limits as a column property in the existing data table for the response variable. If the limits are constant, LCL, Avg, and UCL values for each chart type in the report are saved. This option is not available with phase charts. In addition, the option has no effect if the sample sizes are not constant for each chart.
- **in New Table** Saves the standard deviation and mean for each chart into a new data table. If the limits are constant, the LCL, Avg, and UCL for each chart are saved as well. If there are phases, a new set of values is saved for each phase. You can use this data table to use the limits later. In the Control Chart launch window, click **Get Limits** and then select the saved data table. See the section "Saving and Retrieving Limits".
- **Save Summaries** Creates a new data table that contains the sample label, sample sizes, the statistic being plotted, the center line, and the control limits. The specific statistics included in the table depend on the type of chart.
- **Alarm Script** Enables you to write and run a script that indicates when the data fail special causes tests. Results can be written to the log or spoken. See "Tests" of this guide. See the *Scripting Guide* for more information about writing custom Alarm Scripts.

See *Using JMP* for more information about the following options:

- **Redo** Contains options that enable you to repeat or relaunch the analysis. In platforms that support the feature, the Automatic Recalc option immediately reflects the changes that you make to the data table in the corresponding report window.
- **Save Script** Contains options that enable you to save a script that reproduces the report to several destinations.
- **Save By-Group Script** Contains options that enable you to save a script that reproduces the platform report for all levels of a By variable to several destinations. Available only when a By variable is specified in the launch window.

## **Chart Options for Legacy Control Charts**

The red triangle menu of chart options appears when you click the icon next to the chart name. Some options are also available under **Chart Options** when you right-click the chart. Not all of the options below are available for all control chart types.

**Box Plots** Superimposes box plots on the subgroup means plotted in a Mean chart. The box plot shows the subgroup maximum, minimum, 75th percentile, 25th percentile, and median. Markers for subgroup means show unless you deselect the **Show Points** option. The control limits displayed apply only to the subgroup mean. The **Box Plots** option is available only for  $\bar{X}$  charts. It is most appropriate for larger subgroup sample sizes (more than 10 samples in a subgroup).

**Needle** Connects plotted points to the center line with a vertical line segment.

Legacy Control Chart Platform Options

**Connect Points** Shows or hides the line that connects the data points.

**Show Points** Shows or hides the points representing summary statistics. Initially, the points show. You can use this option to suppress the markers denoting subgroup means when the **Box Plots** option is in effect.

**Connect Color** Displays the JMP color palette for you to choose the color of the line segments used to connect points.

**Center Line Color** Displays the JMP color palette for you to choose the color of the line segments used to draw the center line.

**Limits Color** Displays the JMP color palette for you to choose the color of the line segments used in the upper and lower limits lines.

**Line Width** Enables you to select the width of the control lines. Options are **Thin**, **Medium**, or **Thick**.

**Point Marker** Enables you to select the marker used on the chart.

**Show Center Line** Shows or hides the center line in the control chart.

**Show Control Limits** Shows or hides the chart control limits and their legends.

**Limits Precision** Sets the decimal limit for labels.

**Tests** Shows a submenu that enables you to choose which tests to mark on the chart when the test is positive. Tests apply only for charts whose limits are 3σ limits. Tests 1 to 4 apply to Mean, Individual, and attribute charts. Tests 5 to 8 apply to Mean charts, Presummarize, and Individual Measurement charts only. If tests do not apply to a chart, the Tests option is dimmed. When sample sizes are unequal, the Test options are grayed out. If the samples change while the chart is open and they become equally sized, and the zone or test option is selected, the zones or tests are applied immediately and appear on the chart. These special tests are also referred to as the *Western Electric Rules*. For more information about special causes tests, see "Tests".

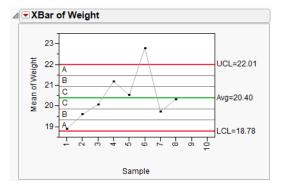
**Westgard Rules** Westgard rules are control rules that help you decide whether a process is in or out of control. The different tests are abbreviated with the decision rule for the particular test. See the text and chart in "Westgard Rules".

**Test Beyond Limits** Flags as a "\*" any point that is beyond the limits. This test works on all charts with limits, regardless of the sample size being constant, and regardless of the size of *k* or the width of the limits. For example, if you had unequal sample sizes, and wanted to flag any points beyond the limits of an R chart, you could use this command.

**Show Zones** Shows or hides the *zone lines*. The zones are labeled A, B, and C as shown here in the Mean plot for weight in the Coating.jmp sample data. Control Chart tests use the

zone lines as boundaries. The seven zone lines are set one sigma apart, centered on the center line.

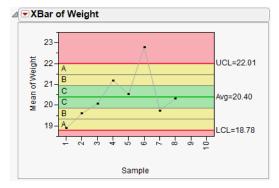
Figure 12.14 Show Zones



**Shade Zones** Shows or hides the default green, yellow, and red colors for the three zone areas and the area outside the zones. Green represents the area one sigma from the center line, yellow represents the area two and three sigmas from the center line, and red represents the area beyond three sigmas. Shades can be shown with or without the zone lines.

**Tip:** To change the colors used to shade the zones, right-click in the control chart and select Customize. In the Customize Graph window, you can specify colors for each of the three zones.

Figure 12.15 Shade Zones



**OC Curve** (Available when subgroup sizes are equal.) Opens a new window that contains the operating characteristic (OC) curve, using all the calculated values directly from the active control chart. See "Operating Characteristic Curves Utility".

## **Chart Options for V-Mask CUSUM Control Charts**

**Mask Color** (Available only when the Show V Mask option is selected.) Enables you to select a line color for the V-mask.

**Show Shift** Shows or hides the shift that you entered in the launch window.

**Show V Mask** Shows or hides the V-mask based on the statistics that you specified in the CUSUM Control Charts launch window.

**Show Parameters** Shows or hides a report that summarizes the CUSUM charting parameters.

**Show ARL** Shows or hides the average run length (ARL) information. The average run length is the expected number of samples taken before an out-of-control condition is signaled:

- ARL (Delta), sometimes denoted ARL1, is the average run length for detecting a shift in the size of the specified Delta.
- ARL(0), sometimes denoted ARL0, is the in-control average run length for the specified parameters (Montgomery 2013).

# Saving and Retrieving Limits

JMP can use previously established control limits for control charts:

- Upper and lower control limits, and a center line value.
- Parameters for computing limits such as a mean and standard deviation.

The control limits or limit parameter values must be either in a JMP data table, referred to as the *Limits Table*, or stored as a column property in the process column. When you specify the **Control Chart** command, you can retrieve the Limits Table with the **Get Limits** button on the Control Chart launch window.

Tip: To add specification limits to several columns at once, see "Manage Spec Limits Utility".

The easiest way to create a Limits Table is to save results computed by the Control Chart platform. The **Save Limits** command in the red triangle menu for each control chart automatically saves limits from the sample values. The type of data saved in the table varies according to the type of control chart in the analysis window. You can also use values from any source and create your own Limits Table.

All Limits Tables must have:

A column of special keywords that identify each row.

• A column for each of the variables whose values are the known standard parameters or limits. This column name must be the same as the corresponding process variable name in the data table to be analyzed by the Control Chart platform.

The following table describes the limit keywords and their associated control chart for both legacy control charts and charts created with Control Chart Builder.

**Table 12.1** Limits Table Keys with Appropriate Charts and Meanings

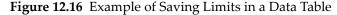
Keywords	For Charts	Meaning
_KSigma	All <i>except</i> Control Chart Builder and V-Mask CUSUM	multiples of the standard deviation of the statistics to calculate the control limits; set to missing if the limits are in terms of the alpha level
_Alpha	All <i>except</i> Control Chart Builder	Type I error probability used to calculate the control limits
_Range Span	IM, MR, MMR	number of consecutive measurements for which moving ranges are computed. Not applicable in the Control Chart Builder platform, where the range span is always equal to 2.
_Sample Size	All <i>except</i> Levey-Jennings and Presummarize	subgroup size
_Std Dev	XBar, R, S, IM, MR, G, T, V-Mask CUSUM, and Levey-Jennings	known process standard deviation
_U	C, U	known average number of nonconformities per unit
_P	NP, P	known value of average proportion nonconforming
_LCL, _UCL	XBar, IM, P, NP, C, U, G, T, and Levey-Jennings	lower and upper control limit for Mean Chart, Individual Measurement chart, or any attribute or rare event chart
_AvgR	R, MR	average range or average moving range

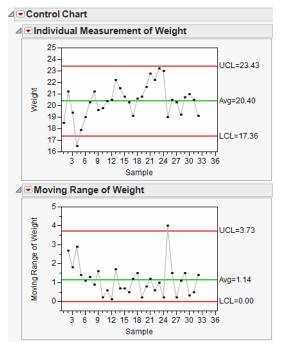
 Table 12.1 Limits Table Keys with Appropriate Charts and Meanings (Continued)

Keywords	For Charts	Meaning
_LCLR, _UCLR	R, MR	lower control limit for R or MR chart
		upper control limit for R or MR chart
_AvgS, _LCLS, _UCLS	S Chart	average standard deviation, upper and lower control limits for S chart
_AvgR_PreMeans _AvgR_PreStdDev _LCLR_PreMeans _LCLR_PreStdDev _UCLR_PreMeans _UCLR_PreStdDev _Avg_PreMeans _Avg_PreMeans _LCL_PreMeans _LCL_PreMeans _LCL_PreStdDev _UCL_PreMeans _UCL_PreMeans	IM, MR	Mean, upper, and lower control limits based on pre-summarized group means or standard deviations.
_Data Units _Two Sided _Headstart _Beta _Delta	V-Mask CUSUM	specifications for V-Mask CUSUM chart

You can save limits in a new data table or as properties of the response column. When you save control limits using the **in New Table** command, the limit keywords written to the table depend on the current chart types displayed.

Figure 12.16 shows examples of control limits saved to a data table using Coating.jmp. The rows with values \_Mean, \_LCL, and \_UCL are for the Individual Measurement chart. The values with the R suffix (\_AvgR, \_LCLR, and \_UCLR) are for the Moving Range chart. If you create these charts again using this Limits Table, the Control Chart platform identifies the appropriate limits from keywords in the \_LimitsKey column.





•		
F	_LimitsKey	Weight
1	_KSigma	3
2	_Alpha	0.0026997961
3	_Range Span	2
4	_Std Dev	1.0120139729
5	_Mean	20.396875
6	_LCL	17.360833081
7	_UCL	23.432916919
8	_AvgR	1.1419354839
9	_LCLR	0
10	_UCLR	3.7301687077

Note that values for \_KSigma, \_Alpha, and \_Range Span can be specified in the Control Chart Launch window. JMP always looks at the values from the window first. Values specified in the window take precedence over those in an active Limits Table.

Rows with unknown keywords and rows marked with the excluded row state are ignored. Except for \_Range Span, \_KSigma, \_Alpha, and \_Sample Size, any needed values not specified are estimated from the data.

# **Excluded, Hidden, and Deleted Samples**

The following table summarizes the effects of various conditions on samples and subgroups:

Table 12.2 Excluded, Hidden, and Deleted Samples

All rows of the sample are excluded before creating the chart.	Sample is not included in the calculation of the limits, but it appears on the graph.
Sample is excluded after creating the chart.	Sample is included in the calculation of the limits, and it appears in the graph. Nothing changes on the output by excluding a sample with the graph open.

Excluded, Hidden, and Deleted Samples

 Table 12.2 Excluded, Hidden, and Deleted Samples (Continued)

Sample is hidden before creating the chart.	Sample is included in the calculation of the limits, but does not appear on the graph.
Sample is hidden after creating the chart.	Sample is included in the calculation of the limits, but does not appear on the graph. The sample marker disappears from the graph, the sample label still appears on the axis, but limits remain the same.
All rows of the sample are both excluded and hidden before creating the chart.	Sample is not included in the calculation of the limits, and it does not appear on the graph.
All rows of the sample are both excluded and hidden after creating the chart.	Sample is included in the calculation of the limits, but does not appear on the graph. The sample marker disappears from the graph, the sample label still appears on the axis, but limits remain the same.
Data set is subsetted with Sample deleted before creating chart.	Sample is not included in the calculation of the limits, the axis does not include a value for the sample, and the sample marker does not appear on the graph.
Data set is subsetted with Sample deleted after creating chart.	Sample is not included in the calculation of the limits, and does not appear on the graph. The sample marker disappears from the graph, the sample label is removed from the axis, the graph shifts, and the limits change.

#### Some additional notes:

Hide and Exclude operate only on the row state of the first observation in the sample. For
example, if the second observation in the sample is hidden, but the first observation is not
hidden, the sample still appears on the chart.

**Note:** Excluded rows in Presummarize charts are excluded from calculations, regardless of which position they are within a sample.

- An exception to the exclude/hide rule: Both hidden and excluded rows are included in the
  count of points for Tests for Special Causes. An excluded row can be labeled with a special
  cause flag. A hidden point cannot be labeled. If the flag for a Tests for Special Causes is on
  a hidden point, it will not appear in the chart.
- Because of the specific rules in place (Table 12.2), the control charts do not support the Automatic Recalc script.

# Additional Examples of the Control Chart Platform

- "Presummarize Chart Example"
- "V-Mask CUSUM Chart Example"
- "One-Sided CUSUM Chart Example"
- "UWMA Chart Example"

## **Presummarize Chart Example**

This example uses the Coating.jmp data table.

- 1. Select **Help > Sample Data Library** and open Quality Control/Coating.jmp.
- 2. Select Analyze > Quality and Process > Legacy Control Charts > Presummarize.
- Select Weight and click Process.
- 4. Select Sample and click **Sample Label**.
- Select both Individual on Group Means and Moving Range on Group Means. The Sample Grouped by Sample Label button is automatically selected when you choose a Sample Label variable.

When using **Presummarize** charts, you can select either **On Group Means** options or **On Group Std Devs** options or both. Each option creates two charts (an Individual Measurement, also known as an X chart, and a Moving Range chart) if both IR chart types are selected.

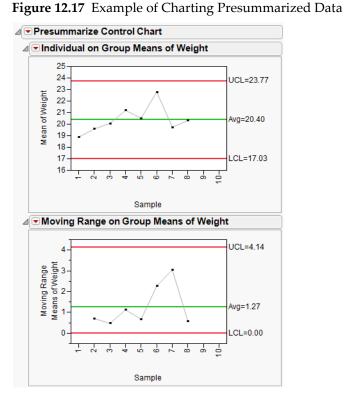
The **On Group Means** options compute each sample mean and then plot the means and create an Individual Measurement and a Moving Range chart on the means.

The **On Group Std Devs** options compute each sample standard deviation and plot the standard deviations as individual points. Individual Measurement and Moving Range charts for the standard deviations then appear.

6. Click **OK**.

**Legacy Control Charts** 

Figure 10.17 Evenuels of Chapting Drawnson animal Data



Although the points for XBar and S charts are the same as the Individual on Group Means and Individual on Group Std Devs charts, the limits are different because they are computed as Individual charts.

Another way to generate the presummarized charts, with the Coating.jmp data table:

- 1. Choose **Tables > Summary**.
- 2. Select Sample and click **Group**.
- 3. Select Weight, and then click **Statistics** > **Mean** and **Statistics** > **Std Dev**.
- 4. Click **OK**.
- 5. Select Analyze > Quality and Process > Legacy Control Charts > IR.
- 6. Select Mean(Weight) and Std Dev(Weight) and click Process.
- Click OK.

The resulting charts match the presummarized charts.

## V-Mask CUSUM Chart Example

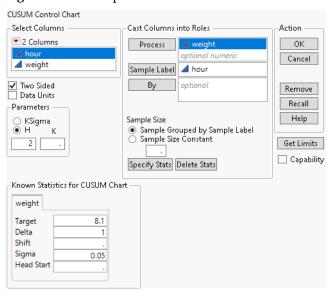
A machine fills 8-ounce cans of two-cycle engine oil additive. The filling process is believed to be in statistical control. The process is set so that the average weight of a filled can ( $\mu_0$ ) is 8.10 ounces. Previous analysis shows that the standard deviation of fill weights ( $\sigma_0$ ) is 0.05 ounces.

Subgroup samples of four cans are selected and weighed every hour for twelve hours. Each observation in the Oil1 Cusum.jmp data table contains one value of weight and its associated value of hour. The observations are sorted so that the values of hour are in increasing order.

- 1. Select **Help > Sample Data Library** and open Quality Control/Oil1 Cusum.jmp.
- 2. Select Analyze > Quality And Process > Legacy Control Charts > CUSUM.
- 3. Select weight and click **Process**.
- 4. Select hour and click **Sample Label**.
- 5. Select the **Two Sided** check box if it is not already checked.
- 6. In the Parameters area, click the **H** button and type 2.
- 7. Click **Specify Stats**.
- 8. Type 8.1 next to **Target**.
  - 8.1 is the average weight in ounces of a filled can. This is the target mean.
- 9. Type 1 next to **Delta**.
  - 1 is the absolute value of the smallest shift to be detected as a multiple of the process standard deviation or of the standard error.
- 10. Type 0.05 next to **Sigma**.
  - 0.05 is the known standard deviation of fill weights ( $\sigma_0$ ) in ounces.

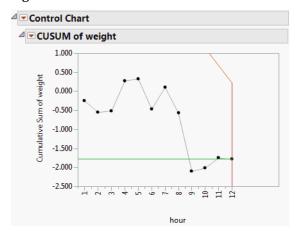
**Legacy Control Charts** 

Figure 12.18 Completed Launch Window



#### 11. Click **OK**.

Figure 12.19 Two-Sided CUSUM Chart for Oil1 Cusum.jmp Data



You can interpret the chart by comparing the points with the V-mask. The right edge of the V-mask is centered at the most recent point (the 12th hour). Because none of the points cross the arms of the V-mask, there is no evidence that a shift in the process has occurred. See "V-Mask CUSUM Chart Reports".

## **One-Sided CUSUM Chart Example**

Consider the data used in "V-Mask CUSUM Chart Example", where the machine fills 8-ounce cans of engine oil. In order to cut costs, the manufacturer is now concerned about significant over-filling (and not so concerned about under-filling). Use a one-sided CUSUM chart to identify any instances of over-filling. Anything that is 0.25 ounces beyond the mean of 8.1 is considered a problem.

- 1. Select **Help > Sample Data Library** and open Quality Control/Oil1 Cusum.jmp.
- 2. Select Analyze > Quality And Process > Legacy Control Charts > CUSUM.
- Deselect Two Sided.
- 4. Select weight and click **Process**.
- 5. Select hour and click **Sample Label**.
- 6. Click **H** and type 0.25.
- 7. Click **Specify Stats**.
- 8. Type 8.1 next to **Target**.
  - 8.1 is the average weight in ounces of a filled can. This is the target mean.
- 9. Type 1 next to **Delta**.

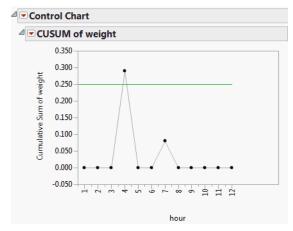
1 is the absolute value of the smallest shift to be detected as a multiple of the process standard deviation or of the standard error.

10. Type 0.05 next to **Sigma**.

0.05 is the known standard deviation of fill weights ( $\sigma_0$ ) in ounces.

11. Click **OK**.

Figure 12.20 One-Sided CUSUM Chart for Oil1 Cusum.jmp Data



**Legacy Control Charts** 

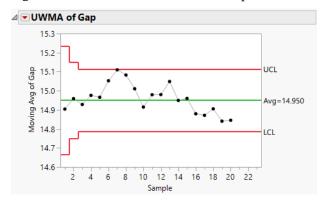
The decision interval is set at the H value that you entered (0.25). You can see that at the fourth hour, some significant over-filling occurred.

#### **UWMA Chart Example**

In the sample data table Clips1.jmp, the measure of interest is the gap between the ends of manufactured metal clips. To monitor the process for a change in the average gap, subgroup samples of five clips are selected daily. A UWMA chart with a moving average span of three is examined.

- Select **Help > Sample Data Library** and open Quality Control/Clips1.jmp.
- Select Analyze > Quality and Process > Legacy Control Charts > UWMA.
- Select Gap and click Process.
- Select Sample and click Sample Label.
- Change the **Moving Average Span** to 3.
- Click **OK**.

**Figure 12.21** UWMA Charts for the Clips1 data



The point for the first day is the mean of the five subgroup sample values for that day. The plotted point for the second day is the average of subgroup sample means for the first and second days. The points for the remaining days are the average of subsample means for each day and the two previous days.

The average clip gap appears to be decreasing, but no sample point falls outside the  $3\sigma$  limits.

### Statistical Details for the Control Chart Platform

- "Control Limits for Median Moving Range Charts"
- "Statistical Details for Capability Analysis"
- "Statistical Details for V-Mask CUSUM Control Charts"
- "Statistical Details for Weighted Moving Average Charts"

**Note:** For more information about other types of charts (such as XBar and R charts, P and NP charts, and more) see the "Statistical Details for Control Chart Builder".

#### **Control Limits for Median Moving Range Charts**

Control limits for Median Moving Range charts are computed as follows:

LCL<sub>MMR</sub> = max(0, MMR - 
$$kd_3(n)$$
  $\hat{\sigma}$  )

UCL<sub>MMR</sub> = MMR +  $kd_3(n)$   $\hat{\sigma}$ 

where:

MMR is the median of the nonmissing moving ranges.

$$\hat{\sigma} = MMR/0.954$$

 $d_3(n)$  is the standard deviation of the range of n independent normally distributed variables with unit standard deviation.

#### **Statistical Details for Capability Analysis**

This section contains details about the computation of the statistics in the Capability Analysis report.

#### **Variation Statistics**

All capability analyses use the same formulas. Options differ in how sigma ( $\sigma$ ) is computed:

**Long Term Sigma** Uses the overall sigma. This option is used for  $P_{pk}$  statistics, and computes sigma as follows:

$$\hat{\sigma} = \sqrt{\sum_{i=1}^{n} \frac{(x_i - \bar{x})^2}{n-1}}$$

**Note:** By default, the capability indices in the Long Term Sigma report use the Cp labeling that is used in the other sigma reports. To use Ppk labeling in the Long Term Sigma report, select the **File > Preferences > Platforms > Distribution > PpK Capability Labeling** preference.

**Control Chart Sigma** Uses a sigma that is determined by the control chart settings.

- If you specify a value for Sigma using the Specify Stats button in the control launch window, the specified value is used for computing capability indices.
- In an IR chart that uses the Moving Range (Average) option, the value for sigma is computed as follows:

$$\hat{\sigma} = \frac{\overline{R}}{d_2(n)}$$

where:

 $\overline{R}$  is the average of the moving ranges.

 $d_2(n)$  is the expected value of the range of n independent normally distributed variables with unit standard deviation, where n is the value of the Range Span option.

 In an IR chart that uses the Median Moving Range option, the value for sigma is computed as follows:

$$\hat{\sigma} = \frac{MMR}{d_A(n)}$$

where:

MMR is the median of the nonmissing moving ranges.

 $d_4(n)$  is the median of the range of n independent normally distributed variables with unit standard deviation, where n is the value of the Range Span option.

- In an XBar chart that uses the R option, the value for sigma is computed as follows:

$$\hat{\sigma} = \frac{\frac{R_1}{d_2(n_1)} + \dots + \frac{R_N}{d_2(n_N)}}{N}$$

Statistical Details for the Control Chart Platform

where:

 $R_i$  = range of  $i^{th}$  subgroup

 $n_i$  = sample size of  $i^{th}$  subgroup

 $d_2(n_i)$  = expected value of the range of  $n_i$  independent normally distributed variables with unit standard deviation

N = number of subgroups for which  $n_i \ge 2$ 

– In an XBar chart that uses the S option, the value for sigma is computed as follows:

$$\hat{\sigma} = \frac{\frac{s_1}{c_4(n_1)} + \dots + \frac{s_N}{c_4(n_N)}}{N}$$

where:

 $n_i$  = sample size of  $i^{th}$  subgroup

 $c_4(n_i)$  = expected value of the standard deviation of  $n_i$  independent normally distributed variables with unit standard deviation

N = number of subgroups for which  $n_i \ge 2$ 

 $s_i$  = sample standard deviation of the  $i^{th}$  subgroup

#### **Capability Indices for Normal Distributions**

This section provides details about the calculation of capability indices for normal data.

For a process characteristic with mean  $\mu$  and standard deviation  $\sigma$ , the population-based capability indices are defined as follows:

$$Cp = \frac{USL - LSL}{6\sigma}$$

Cpl = 
$$\frac{\mu - LSL}{3\sigma}$$

Cpu = 
$$\frac{USL - \mu}{3\sigma}$$

$$Cpk = min(Cpl, Cpu)$$

$$Cpm = \frac{\min(T - LSL, USL - T)}{3\sigma \sqrt{1 + \left(\frac{T - \mu}{\sigma}\right)^2}}$$

where:

LSL is the lower specification limit.

USL is the upper specification limit.

*T* is the target value.

For sample-based capability indices, the parameters are replaced by their estimates. The estimate for  $\sigma$  uses the method that you specified in the Capability Analysis window. See "Variation Statistics".

If either of the specification limits is missing, the capability indices containing the missing specification limit are reported as missing.

**Tip:** A capability index of 1.33 is often considered to be the minimum value that is acceptable. For a normal distribution, a capability index of 1.33 corresponds to an expected number of nonconforming units of about 6 per 100,000.

#### Confidence Intervals for Capability Indices

**Note:** Confidence intervals for capability indices appear only in the Long Term Sigma report.

The  $100(1 - \alpha)\%$  confidence interval for Cp is calculated as follows:

$$\left(\hat{\operatorname{CP}}\sqrt{\frac{\chi_{\alpha/2,\,n-1}^2}{n-1}},\hat{\operatorname{CP}}\sqrt{\frac{\chi_{1-\alpha/2,\,n-1}^2}{n-1}}\right)$$

where:

ĈP is the estimated value for Cp.

 $\chi^2_{\alpha/2, n-1}$  is the  $(\alpha/2)^{\text{th}}$  quantile of a chi-square distribution with n-1 degrees of freedom.

*n* is the number of observations.

The  $100(1 - \alpha)\%$  confidence interval for Cpk is calculated as follows:

$$\left(\hat{C}_{pk}\left[1-\Phi^{-1}_{1-\alpha/2}\sqrt{\frac{1}{9n\hat{C}_{pk}^2}+\frac{1}{2(n-1)}}\right],\hat{C}_{pk}\left[1+\Phi^{-1}_{1-\alpha/2}\sqrt{\frac{1}{9n\hat{C}_{pk}^2}+\frac{1}{2(n-1)}}\right]\right)$$

where:

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 $\hat{C}_{pk}$  is the estimated value for Cpk.

 $\Phi^{-1}_{1-\alpha/2}$  is the  $(1 - \alpha/2)^{th}$  quantile of a standard normal distribution.

*n* is the number of observations.

The  $100(1 - \alpha)\%$  confidence interval for CPM is calculated as follows:

$$\left(\hat{\text{CPM}}\sqrt{\frac{\chi^2_{\alpha/2,\gamma}}{\gamma}},\hat{\text{CPM}}\sqrt{\frac{\chi^2_{1-\alpha/2,\gamma}}{\gamma}}\right)$$

where:

CPM is the estimated value for CPM.

 $\chi^2_{\alpha/2,\,\gamma}$  is the  $(\alpha/2)^{th}$  quantile of a chi-square distribution with  $\gamma$  degrees of freedom.

$$\gamma = \frac{n\left(1 + \left(\frac{\bar{x} - T}{s}\right)^2\right)^2}{1 + 2\left(\frac{\bar{x} - T}{s}\right)^2}$$

*n* is the number of observations.

 $\bar{x}$  is the mean of the observations.

*T* is the target value.

*s* is the long-term sigma estimate.

**Note:** The confidence interval for CPM is computed only when the target value is centered between the lower and upper specification limits.

Lower and upper confidence limits for CPL and CPU are computed using the method of Chou et al. (1990).

**Legacy Control Charts** 

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The  $100(1 - \alpha)\%$  confidence limits for CPL (denoted by CPL<sub>L</sub> and CPL<sub>U</sub>) satisfy the following equations:

$$\Pr[t_{n-1}(\delta_L) \ge 3\hat{C}_{pl}\sqrt{n}] = \alpha/2$$
 where  $\delta_L = 3CPL_L\sqrt{n}$ 

$$\Pr[t_{n-1}(\delta_U) \le 3\hat{C}_{pl}\sqrt{n}] = \alpha/2$$
 where  $\delta_U = 3CPL_U\sqrt{n}$ 

where:

 $t_{n-1}(\delta)$  has a non-central t-distribution with n-1 degrees of freedom and noncentrality parameter  $\delta$ .

 $\hat{C}_{vl}$  is the estimated value for Cpl.

The  $100(1 - \alpha)\%$  confidence limits for CPU (denoted by CPU<sub>I</sub> and CPU<sub>I</sub>) satisfy the following equations:

$$\Pr[t_{n-1}(\delta_L) \ge 3\hat{C}_{pu}\sqrt{n}] = \alpha/2$$
 where  $\delta_L = 3CPU_L\sqrt{n}$ 

$$\Pr[t_{n-1}(\delta_{II}) \le 3\hat{C}_{pu}\sqrt{n}] = \alpha/2$$
 where  $\delta_{II} = 3CPU_{II}\sqrt{n}$ 

where:

 $t_{n-1}(\delta)$  has a non-central t-distribution with n-1 degrees of freedom and noncentrality parameter δ.

 $\hat{C}_{nu}$  is the estimated value for Cpu.

#### Capability Indices for Nonnormal Distributions

This section describes how capability indices are calculated for nonnormal distributions. These generalized capability indices are defined as follows:

$$Cp = \frac{USL - LSL}{P_{0.99865} - P_{0.00135}}$$

$$Cpk = min(C_{vl}, C_{vu})$$

Statistical Details for the Control Chart Platform

$$Cpm = \frac{\min(\frac{T - LSL}{P_{0.5} - P_{0.00135}}, \frac{USL - T}{P_{0.99865} - P_{0.5}})}{\sqrt{1 + (\frac{\mu - T}{\sigma})^2}}$$

$$Cpl = \frac{P_{0.5} - LSL}{P_{0.5} - P_{0.00135}}$$

$$Cpu = \frac{USL - P_{0.5}}{P_{0.99865} - P_{0.5}}$$

where:

LSL is the lower specification limit.

USL is the upper specification limit.

*T* is the target value.

 $P_{\alpha}$  is the  $\alpha$ \*100<sup>th</sup> percentile of the fitted distribution.

For the calculation of Cpm,  $\mu$  and  $\sigma$  are estimated using the expected value and square root of the variance of the fitted distribution. For more information about the relationship between the parameters in the Parameter Estimates report and the expected value and variance of the fitted distributions, see *Basic Analysis*.

#### **Sigma Quality Statistics**

The Sigma Quality statistics for each Portion (Below LSL, Above USL, and Total Outside) are calculated as follows:

Sigma Quality = 
$$\Phi^{-1}_{1-Pct/100} + 1.5$$

where:

Pct is the value in the Percent column of the report.

 $\Phi^{-1}_{1-Pct/100}$  is the  $(1 - Pct/100)^{th}$  quantile of a standard normal distribution.

**Note:** Even though the Percent Below LSL and Percent Above USL sum to the Percent Total Outside value, the Sigma Quality Below LSL and Sigma Quality Above USL values do not sum to the Sigma Quality Total Outside value. This is because calculating Sigma Quality involves finding normal distribution quantiles, and is therefore not additive.

#### Benchmark Z Statistics

Benchmark Z statistics are available only for capability analyses based on the normal distribution. The Benchmark Z statistics are calculated as follows:

Z Bench = 
$$\Phi^{-1}_{1-P(LSL)-P(USL)}$$

$$Z LSL = \frac{\mu - LSL}{\sigma} = 3 * Cpl$$

$$Z USL = \frac{USL - \mu}{\sigma} = 3 * Cpu$$

where:

LSL is the lower specification limit.

*USL* is the upper specification limit.

μ is the sample mean.

 $\sigma$  is the sample standard deviation.

 $\Phi^{-1}_{1-P(LSL)-P(USL)}$  is the  $(1-P(LSL)-P(USL))^{th}$  quantile of a standard normal distribution.

$$P(LSL) = \text{Prob}(X < LSL) = 1 - \Phi(Z LSL).$$

$$P(USL) = \text{Prob}(X > USL) = 1 - \Phi(Z \text{ USL}).$$

 $\Phi$  is the standard normal cumulative distribution function.

#### Statistical Details for V-Mask CUSUM Control Charts

The following notation is used in these formulas:

- $\bullet$   $\mu$  denotes the mean of the population, also referred to as the process mean or the process level.
- $\mu_0$  denotes the target mean (or goal) for the population. Sometimes, the symbol  $\overline{X}_0$  is used for  $\mu_0$ . See the American Society for Quality Statistics Division (2004). You can provide  $\mu_0$  as the Target in the Known Statistics for CUSUM Chart area on the launch window.
- $\sigma$  denotes the population standard deviation.  $\hat{\sigma}$  denotes an estimate of  $\sigma$ .
- $\sigma_0$  denotes a known standard deviation. You can provide  $\sigma_0$  as the Sigma in the Known Statistics for CUSUM Chart area on the launch window.
- *n* denotes the nominal sample size for the CUSUM chart.

- $\delta$  denotes the shift in  $\mu$  to be detected, expressed as a multiple of the standard deviation. You can provide  $\delta$  as the Delta in the Known Statistics for CUSUM Chart area on the launch window.
- $\Delta$  denotes the shift in  $\mu$  to be detected, expressed in data units. If the sample size n is constant across subgroups, then the following computation applies:

$$\Delta = \delta \sigma_{\overline{X}} = (\delta \sigma) / \sqrt{n}$$

You can provide  $\Delta$  as the Shift in the Known Statistics for CUSUM Chart area on the launch window.

**Note:** Some authors use the symbol D instead of  $\Delta$ .

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#### **Positive Shifts**

If the shift  $\delta$  to be detected is positive, the CUSUM for the  $t^{th}$  subgroup is computed as follows:

$$S_t = \max(0, S_{t-1} + (z_t - k))$$

t = 1, 2, ..., n, where  $S_0 = 0, z_t$  is defined as for two-sided charts, and the parameter k, termed the reference value, is positive. If the parameter k is not specified in the launch window, k is set to  $\delta/2$ . The CUSUM  $S_t$  is referred to as an upper cumulative sum.  $S_t$  can be computed as follows:

$$\max\left(0, S_{t-1} + \frac{\overline{X}_i - (\mu_0 + k\sigma_{\overline{X}_t})}{\sigma_{\overline{X}_t}}\right)$$

The sequence  $S_t$  cumulates deviations in the subgroup means greater than k standard errors from  $\mu_0$ . If  $S_t$  exceeds a positive value h (referred to as the *decision interval*), a shift or out-of-control condition is signaled.

#### **Negative Shifts**

If the shift to be detected is negative, the CUSUM for the  $t^{\text{th}}$  subgroup is computed as follows:

$$S_t = \max(0, S_{t-1} - (z_t + k))$$

**Legacy Control Charts** 

t = 1, 2, ..., n, where  $S_0 = 0$ ,  $z_t$  is defined as for two-sided charts, and the parameter k, termed the *reference value*, is positive. If the parameter k is not specified in the launch window, k is set to  $\delta/2$ . The CUSUM  $S_t$  is referred to as a *lower cumulative sum*.  $S_t$  can be computed as follows:

$$\max\left[0, S_{t-1} - \frac{\overline{X}_i - (\mu_0 - k\sigma_{\overline{X}_t})}{\sigma_{\overline{X}_t}}\right]$$

The sequence  $S_t$  cumulates the absolute value of deviations in the subgroup means less than k standard errors from  $\mu_0$ . If  $S_t$  exceeds a positive value h (referred to as the *decision interval*), a shift or out-of-control condition is signaled.

Note that  $S_t$  is always positive and h is always positive, regardless of whether  $\delta$  is positive or negative. For charts designed to detect a negative shift, some authors define a reflected version of  $S_t$  for which a shift is signaled when  $S_t$  is less than a negative limit.

Lucas and Crosier (1982) describe the properties of a fast initial response (FIR) feature for CUSUM charts in which the initial CUSUM  $S_0$  is set to a "head start" value. Average run length calculations given by them show that the FIR feature has little effect when the process is in control and that it leads to a faster response to an initial out-of-control condition than a standard CUSUM chart. You can provide a Head Start value in the Known Statistics for CUSUM Chart area on the launch window.

#### **Constant Sample Sizes**

When the subgroup sample sizes are constant (= n), it might be preferable to compute CUSUMs that are scaled in the same units as the data. CUSUMs are then computed as follows:

$$S_t = \max(0, S_{t-1} + (\overline{X}_t - (\mu_0 + k\sigma / \sqrt{n})))$$

where  $\delta > 0$ 

$$S_t = \max(0, S_{t-1} - (\overline{X}_t - (\mu_0 - k\sigma/\sqrt{n})))$$

where  $\delta < 0$ . In either case, the parameter k is rescaled to  $k' = k\sigma/\sqrt{n}$ . If the parameter k is not specified in the launch window, k' is set to  $\delta/2$ . A shift is signaled if  $S_t$  exceeds  $h' = h\sigma/\sqrt{n}$ . Some authors use the symbol H for h'.

#### **Two-Sided CUSUM Charts**

If the CUSUM chart is two-sided, the cumulative sum  $S_t$  plotted for the  $t^{th}$  subgroup is defined as follows:

$$S_t = S_{t-1} + z_t$$

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t = 1, 2, ..., n. Here  $S_0$ =0, and the term  $z_t$  is calculated as follows:

$$z_t = (\overline{X}_t - \mu_0)/(\sigma/\sqrt{n_t})$$

where  $\overline{X}_t$  is the  $t^{\text{th}}$  subgroup average, and  $n_t$  is the  $t^{\text{th}}$  subgroup sample size. If the subgroup samples consist of individual measurements  $x_t$ , the term  $z_t$  simplifies to the following computation:

$$z_t = (x_t - \mu_0)/\sigma$$

The first equation can be rewritten as follows:

$$S_t = \sum_{i=1}^t z_i = \sum_{i=1}^t (\overline{X}_i - \mu_0) / \sigma_{\overline{X}_i}$$

where the sequence  $S_t$  cumulates standardized deviations of the subgroup averages from the target mean  $\mu_0$ .

In many applications, the subgroup sample sizes  $n_i$  are constant  $(n_i = n)$ , and the equation for  $S_t$  can be simplified:

$$S_t = (1/\sigma_{\overline{X}}) \sum_{i=1}^t (\overline{X}_i - \mu_0) = (\sqrt{n}/\sigma) \sum_{i=1}^t (\overline{X}_i - \mu_0)$$

In some applications, it might be preferable to compute  $S_t$  as follows:

$$S_t = \sum_{i=1}^t (\overline{X}_i - \mu_0)$$

which is scaled in the same units as the data. In this case, the procedure rescales the V-mask parameters h and k to  $h' = h\sigma/\sqrt{n}$  and  $k' = k\sigma/\sqrt{n}$ , respectively. Some authors use the symbols F for k' and H for h'.

If the process is in control and the mean  $\mu$  is at or near the target  $\mu_0$ , the random walk model applies. Therefore, the points might wander away from zero, but they will not exhibit a large trend since positive and negative displacements from  $\mu_0$  tend to cancel each other. If  $\mu$  shifts in the positive direction, the points exhibit an upward trend, and if  $\mu$  shifts in the negative direction, the points exhibit a downward trend.

Statistical Details for the Control Chart Platform

#### **Control Limits for UWMA Charts**

Control limits for UWMA charts are computed for each subgroup *i* as follows:

$$LCL_{i} = \mu_{0} - k \frac{\hat{\sigma}}{min(i, w)} \sqrt{\frac{1}{n_{i}} + \frac{1}{n_{i-1}} + \dots + \frac{1}{n_{1+max(i-w, 0)}}}$$

Statistical Details for Weighted Moving Average Charts

$$UCL_{i} = \mu_{0} + k \frac{\hat{\sigma}}{min(i, w)} \sqrt{\frac{1}{n_{i}} + \frac{1}{n_{i-1}} + \dots + \frac{1}{n_{1+max(i-w, 0)}}}$$

where:

w is the span parameter (number of terms in moving average)

 $n_i$  is the sample size of the  $i^{th}$  subgroup

*k* is the number of standard deviations

 $\mu_0$  is the weighted average of the subgroup means

 $\hat{\sigma}$  is the estimated process standard deviation

#### Control Limits for EWMA Charts

Control limits for EWMA charts are computed as follows:

LCL = 
$$\mu_0 - k \hat{\sigma} r \sqrt{\sum_{j=0}^{i-1} \frac{(1-r)^{2j}}{n_{i-j}}}$$

UCL = 
$$\mu_0 + k \hat{\sigma} r \sqrt{\sum_{j=0}^{i-1} \frac{(1-r)^{2j}}{n_{i-j}}}$$

where:

*r* is the EWMA weight parameter  $(0 < r \le 1)$ 

 $x_{ij}$  is the  $j^{th}$  measurement in the  $i^{th}$  subgroup, with  $j = 1, 2, 3, ..., n_i$ 

 $n_i$  is the sample size of the  $i^{th}$  subgroup

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*k* is the number of standard deviations

 $\mu_0$  is the weighted average of the subgroup means

 $\hat{\sigma}$  is the estimated process standard deviation

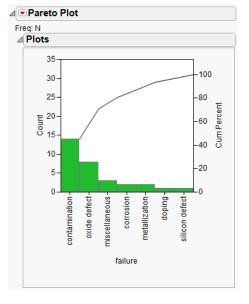
# Chapter 13

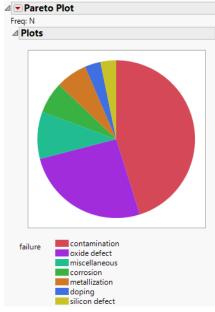
### **Pareto Plots**

#### **Focus Improvement Efforts on the Vital Few**

Improve the statistical quality of your process or operation using Pareto plots. A Pareto plot is a chart that shows severity (frequency) of problems in a quality-related process or operation. Pareto plots help you decide which problems to solve first by highlighting the frequency and severity of problems.

Figure 13.1 Pareto Plot Examples





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#### Overview of the Pareto Plot Platform

The Pareto Plot platform produces charts to display the relative frequency or severity of problems in a quality-related process or operation. The Pareto plot is displayed initially as a bar chart that shows the classification of problems arranged in decreasing order. The column whose values are the cause of a problem is assigned the *Y* role and is called the *process variable*.

You can also generate a comparative Pareto plot, which combines two or more Pareto plots for the same process variable. The single display shows plots for each value in a column assigned the *X* role, or combination of levels from two *X* variables. Columns assigned the *X* role are called *classification variables*.

The Pareto plot can chart a single Y (process) variable with no X classification variables, with a single X, or with two X variables. The Pareto function does not distinguish between numeric and character variables or between modeling types. You can switch between a bar chart and a pie chart. All values are treated as discrete, and bars or wedges represent either counts or percentages.

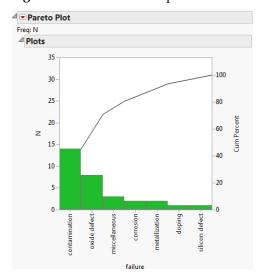
# **Example of the Pareto Plot Platform**

This example uses the Failure.jmp sample data table, which contains failure data and a frequency column. It lists causes of failure during the fabrication of integrated circuits and the number of times each type of defect occurred. From the analysis, you can determine which factors contribute most toward process failure.

- 1. Select **Help > Sample Data Library** and open Quality Control/Failure.jmp.
- Select Analyze > Quality and Process > Pareto Plot.
- Select failure and click Y, Cause.
   This column lists the causes of failure. It is the variable that you want to inspect.
- Select N and click Freq.
   This column list the number of times that each type of failure occurred.
- 5. Click OK.

Example of the Pareto Plot Platform

Figure 13.2 Pareto Plot Report Window



The left axis represents the count of failures, and the right axis represents the percent of failures in each category. The bars are in decreasing order with the most frequently occurring failure to the left. The curve indicates the cumulative failures from left to right.

- 6. Click the Pareto Plot red triangle and select **Label Cum Percent Points**.
  - Note that Contamination accounts for approximately 45% of the failures. The point above the Oxide Defect bar shows that Contamination and Oxide Defect together account for approximately 71% of the failures.
- 7. Click the Pareto Plot red triangle and deselect **Label Cum Percent Points** and **Show Cum Percent Curve**.
- 8. Click the label for the y-axis labeled **N** and rename it **Count**.
- 9. Double-click the y-axis to display the **Y Axis Settings** window.
  - In the **Maximum** field, type 15.
  - In the **Increment** field, type 2.
  - In the Axis Label Row panel, select Grid Lines for the Major grid line.
  - Click **OK**.
- 10. Click the Pareto Plot red triangle and select **Category Legend**.

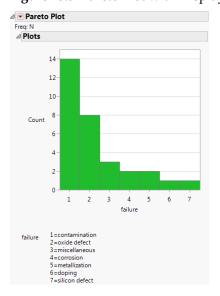
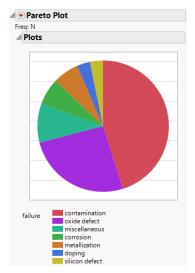


Figure 13.3 shows the counts of different types of failures and has a category legend. The vertical count axis is rescaled and has grid lines at the major tick marks.

11. To view the data as a pie chart, click the Pareto Plot red triangle and select **Pie Chart**.

Figure 13.4 Pareto Plot as a Pie Chart

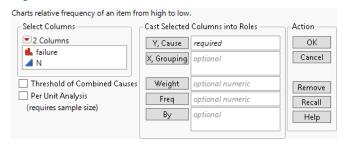


Contamination and Oxide Defect clearly represent the majority of the failures.

# **Launch the Pareto Plot Platform**

Launch the Pareto Plot platform by selecting Analyze > Quality and Process > Pareto Plot.

Figure 13.5 The Pareto Plot Launch Window



For more information about the options in the Select Columns red triangle menu, see *Using IMP*.

The Pareto Plot launch window contains the following options:

- **Y, Cause** Identifies the column whose values are the cause of a problem. It is called the process variable and is the variable that you want to inspect.
- **X, Grouping** Identifies the grouping factor. The grouping variable produces one Pareto plot window with side-by-side plots for each value. You can have no grouping variable, one grouping variable (see "One-Way Comparative Pareto Plot Example"), or two grouping variables (see "Two-Way Comparative Pareto Plot Example").

**Weight** Assigns a variable to give the observations different weights.

**Freq** Identifies the column whose values hold the frequencies.

**By** Identifies a variable to produce a separate analysis for each value that appears in the column.

**Threshold of Combined Causes** Enables you to specify a threshold for combining causes by specifying a minimum rate or count. Select the option and then select **Tail** % or **Count** and enter the threshold value. The Tail percent option combines smaller count groups against the percentage specified of the total (combined small groups count/total group count). The Count option enables you to specify a specific count threshold. For an example, see "Threshold of Combined Causes Example".

**Per Unit Analysis** Enables you to compare defect rates across groups. JMP calculates the defect rate as well as 95% confidence intervals of the defect rate. Select the option and then select **Constant** or **Value in Freq Column** and enter the sample size value or cause code, respectively. The Constant option enables you to specify a constant sample size on the

launch window. The Value In Freq Column option enables you to specify a unique sample size for a group through a special cause code to designate the rows as cause rows.

Although causes are allowed to be combined in Pareto plots, the calculations for these analyses do not change correspondingly.

For examples, see "Using a Constant Size across Groups Example" and "Using a Non-Constant Sample Size across Groups Example".

# The Pareto Plot Report

The Pareto plot combines a bar chart displaying percentages of variables in the data with a line graph showing cumulative percentages of the variables.

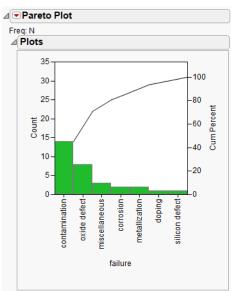


Figure 13.6 Pareto Plot Example

The Pareto plot can chart a single Y (process) variable with no X classification variables, with a single X, or with two X variables. The Pareto plot does not distinguish between numeric and character variables or between modeling types. All values are treated as discrete, and bars represent either counts or percentages. The following list describes the arrangement of the Pareto plot:

- A *Y* variable with no *X* classification variables produces a single chart with a bar for each value of the *Y* variable. For an example, see "Example of the Pareto Plot Platform".
- A *Y* variable with one *X* classification variable produces a row of Pareto plots. There is a plot for each level of the *X* variable with bars for each *Y* level. These plots are referred to as

- the *cells* of a comparative Pareto plot. There is a cell for each level of the *X* (classification) variable. Because there is only one *X* variable, this is called a *one-way comparative Pareto plot*. For an example, see "One-Way Comparative Pareto Plot Example".
- A *Y* variable with two *X* variables produces rows and columns of Pareto plots. There is a row for each level of the first *X* variable and a column for each level of the second *X* variable. Because there are two *X* variables, this is called a *two-way comparative Pareto plot*. The rows have a Pareto plot for each value of the first *X* variable, as described previously. The upper left cell is called the *key cell*. Its bars are arranged in descending order. The bars in the other cells are in the same order as the key cell. You can reorder the rows and columns of cells. The cell that moves to the upper left corner becomes the new key cell and the bars in all other cells rearrange accordingly. For an example, see "Two-Way Comparative Pareto Plot Example".
- Each bar is the color for which the rows for that *Y* level are assigned in the associated data table. Otherwise, a single color is used for all of the bars whose *Y* levels do not have rows with an assigned color. If the rows for a *Y* level have different colors, the bar for that *Y* level is the color of the first row for that *Y* level in the data table.

You can change the type of scale and arrangement of bars and convert the bars into a pie chart using the options in the Pareto Plot red triangle menu. See "Pareto Plot Platform Options".

# **Pareto Plot Platform Options**

The Pareto Plot red triangle menu contains options that customize the appearance of the plots. It also has options in the **Causes** submenu that affect individual bars within a Pareto plot. The following commands affect the appearance of the Pareto plot as a whole:

**Percent Scale** Shows or hides the count and percent left vertical axis display.

**N Legend** Shows or hides the total sample size in the plot area.

**Category Legend** Shows or hides labeled bars and a separate category legend.

**Pie Chart** Shows or hides the bar chart and pie chart representation.

**Reorder Horizontal, Reorder Vertical** Reorders grouped Pareto plots when there is one or more grouping variables.

**Ungroup Plots** Splits up a group of Pareto charts into separate plots.

**Count Analysis** Performs defect per unit analyses. Enables you to compare defect rates and perform ratio tests across and within groups:

**Per Unit Rates** Compares defect rates across groups. If a sample size is specified, Defects Per Unit (DPU) and Parts Per Million (PPM) columns are added to the report.

the Pareto Plot Platform".

- **Test Rate Within Groups** Performs a likelihood ratio Chi-square test to determine whether the rates across causes are the same within a group. See "Statistical Details for
- **Test Rates Across Groups** Performs a likelihood ratio Chi-square test to determine whether the rate for each cause is the same across groups. See "Statistical Details for the Pareto Plot Platform".
- **Show Cum Percent Curve** Shows or hides the cumulative percent curve above the bars and the cumulative percent axis on the vertical right axis.
- **Show Cum Percent Axis** Shows or hides the cumulative percent axis on the vertical right axis.
- **Show Cum Percent Points** Shows or hides the points on the cumulative percent curve.
- **Label Cum Percent Points** Shows or hides the labels on the points on the cumulative curve.
- **Cum Percent Curve Color** Changes the color of the cumulative percent curve.
- **Causes** Has options that affect one or more individual chart bars. See "Causes Options", for a description of these options.
- See *Using JMP* for more information about the following options:
- **Local Data Filter** Shows or hides the local data filter that enables you to filter the data used in a specific report.
- **Redo** Contains options that enable you to repeat or relaunch the analysis. In platforms that support the feature, the Automatic Recalc option immediately reflects the changes that you make to the data table in the corresponding report window.
- **Save Script** Contains options that enable you to save a script that reproduces the report to several destinations.
- **Save By-Group Script** Contains options that enable you to save a script that reproduces the platform report for all levels of a By variable to several destinations. Available only when a By variable is specified in the launch window.

### **Causes Options**

You can highlight a bar by clicking on it. Use Control-click to select multiple bars that are not contiguous. When you select bars, you can access the commands on the red triangle menu that affect Pareto plot bars. They are found on the **Causes** submenu on the red triangle menu. These options are also available with a right-click anywhere in the plot area. The following options apply to highlighted bars instead of to the chart as a whole:

**Combine Causes** Combines selected (highlighted) bars. You can select either **Selected**, **Last Causes**, **First Causes** or select from a list of variables.

Figure 13.7 Combine Causes Window



**Separate Causes** Separates selected bars into their original component bars.

**Move to First** Moves one or more highlighted bars to the left (first) position.

**Move to Last** Moves one or more highlighted bars to the right (last) position.

**Colors** Shows the colors palette for coloring one or more highlighted bars.

**Markers** Shows the markers palette for assigning a marker to the points on the cumulative percent curve, when the **Show Cum Percent Points** command is in effect.

**Label** Displays the bar value at the top of all highlighted bars.

# Additional Examples of the Pareto Plot Platform

- "Threshold of Combined Causes Example"
- "Using a Constant Size across Groups Example"
- "Using a Non-Constant Sample Size across Groups Example"
- "One-Way Comparative Pareto Plot Example"
- "Two-Way Comparative Pareto Plot Example"

#### **Threshold of Combined Causes Example**

This example uses the Failure.jmp sample data table, which contains failure data and a frequency column. It lists causes of failure during the fabrication of integrated circuits and the number of times each type of defect occurred. A threshold value of 2 is specified for this example.

- 1. Select **Help > Sample Data Library** and open Quality Control/Failure.jmp.
- 2. Select Analyze > Quality and Process > Pareto Plot.
- 3. Select failure and click Y, Cause.
- 4. Select N and click Freq.
- 5. Select Threshold of Combined Causes and then select Count.
- 6. Enter 2 as the threshold value.
- 7. Click OK.

Figure 13.8 Pareto Plot with a Threshold Count of 2

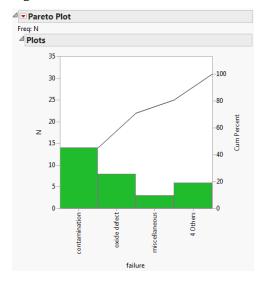
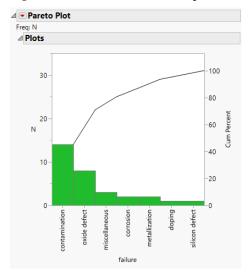


Figure 13.8 displays the plot after specifying a count of 2. All causes with counts 2 or fewer are combined into the final bar labeled 4 Others.

8. To separate the combined bars into original categories as shown in Figure 13.9, select **Causes** > **Separate Causes**.

Figure 13.9 Pareto Plot with Separated Causes



### **Using a Constant Size across Groups Example**

This example uses the Failures.jmp sample data table, which contains failure data and a frequency column. It lists causes of failure during the fabrication of integrated circuits and the number of times each type of defect occurred for two processes. A constant sample size of 1000 is specified for this example.

- 1. Select **Help > Sample Data Library** and open Quality Control/Failures.jmp.
- 2. Select Analyze > Quality and Process > Pareto Plot.
- 3. Select Causes and click Y, Cause.
- 4. Select Process and click X, Grouping.
- 5. Select Count and click **Freq.**
- 6. Select **Per Unit Analysis** and then select **Constant.**
- 7. Enter 1000 in **Sample Size.**
- 8. Click OK.

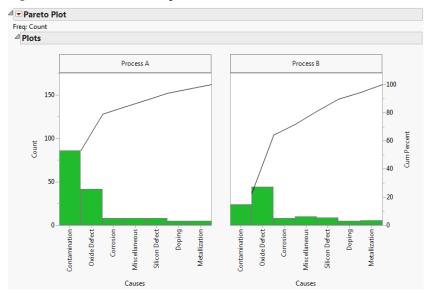


Figure 13.10 Pareto Plot Report Window

Process A indicates Contamination as the top failure while Process B indicates Oxide Defect as the leading failure.

9. Click the Pareto Plot red triangle and select **Count Analysis** > **Test Rates Across Groups**.

Figure 13.11 Test Rates across Groups Results

Test Rate Across Groups								
Test rate across group: Process								
Cause	<b>DPU Diff</b>	8642	0 .2 .4 .6 .8	Std Error	ChiSquare	DF	Prob>ChiSq	
Contamination	0.0620			0.0105	37.0810	1	<.0001*	
Oxide Defect	-0.0020			0.0093	0.0465	1	0.8292	
Corrosion	0.0000			0.0040	0.0000	1	1.0000	
Miscellaneous	-0.0020			0.0042	0.2227	1	0.6370	
Silicon Defect	-0.0010			0.0041	0.0589	1	0.8083	
Doping	0.0000			0.0032	0.0000	1	1.0000	
Metallization	-0.0010			0.0033	0.0910	1	0.7629	
Pooled Total	0.0080			0.0023	11.7882	1	0.0006*	

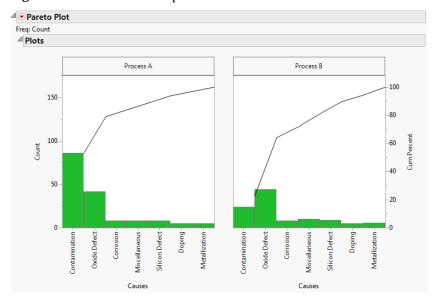
Note that the DPU for Contamination across groups (Process A and B) is around 0.06.

#### **Using a Non-Constant Sample Size across Groups Example**

This example uses the Failuressize.jmp sample data table, which contains failure data and a frequency column. It lists causes of failure during the fabrication of integrated circuits and the number of times each type of defect occurred for two processes. Among the other causes (Oxide Defect, Silicon Defect, and so on) is a cause labeled *size*. Specifying size as the cause code designates the rows as size rows.

- 1. Select **Help > Sample Data Library** and open Quality Control/Failuressize.jmp.
- 2. Select Analyze > Quality and Process > Pareto Plot.
- 3. Select Causes and click Y, Cause.
- 4. Select Process and click X, Grouping.
- 5. Select Count and click Freq.
- 6. Select **Per Unit Analysis** and then select **Value in Freq Column.**
- 7. Enter size in Cause Code.
- 8. Click OK.

Figure 13.12 Pareto Plot Report Window



 Click the Pareto Plot red triangle and select Count Analysis > Per Unit Rates and Count Analysis > Test Rates Across Groups.

Process	Cause	Count	DPU		PPM Low	er 95%	Upper 959
	Contamination	86	0.8515	8514	85.15	0.6811	1.051
	Oxide Defect	42	0.4158	4158	41.58	0.2997	0.562
	Corrosion	8	0.0792	79207.92		0.0342	0.156
	Miscellaneous	8	0.0792	2 79207.92		0.0342	0.156
	Silicon Defect	8	0.0792	79207.92 49504.95 49504.95		0.0342 0.0161 0.0161	0.156
	Doping	5	0.0495				0.115
	Metallization	5	0.0495				0.115
	Pooled Total	162	0.2291	2291	229137.20		0.267
	size	101					
Process B	Contamination	24	0.1655	1655	517.24	0.1061	0.246
Cor	Oxide Defect	44	0.3034	3034	48.28	0.2205	0.407
	Corrosion	8	0.0552	551	72.41	0.0238	0.108
	Miscellaneous	10	0.0690	68965.52	0.0331	0.126	
	Silicon Defect	9	0.0621	620	68.97	0.0284	0.11
Dopi	Doping	5	0.0345			0.0112 0.0152	0.080
	Metallization	6	0.0414				0.090
Pooled Total		106	0.1044	1044	33.50	0.0855	0.12
	size	145					
Test Ra	te Across Gro	ups					
Test rate as	cross group: Proc	ess 8642 0 .2 .	168 c	td Error	ChiSquare	DE	Prob>ChiSq
Contamin		0.0.4.2 0.2.	4.0.0	0.0978	63.0776	1	*.0001 *
Oxide Defe				0.0788	2.1195	1	0.1454
Corrosion	0.0240	-		0.0341	0.5202	1	0.4707
Miscellane	eous 0.0102			0.0355	0.0847	1	0.7710
Silicon De	fect 0.0171			0.0348	0.2500	1	0.6171
Doping	0.0150			0.0270	0.3251	1	0.5685
Metallizati	ion 0.0081			0.0278	0.0871	1	0.7679
Pooled To	tal 0.1247			0.0207	40.7524	1	<.0001*

Figure 13.13 Per Unit Rates and Test Rates across Groups Results

Note that the sample size of 101 is used to calculate the DPU for the causes in group A. However, the sample size of 145 is used to calculate the DPU for the causes in group B.

If there are two group variables (say, Day and Process), Per Unit Rates lists DPU or rates for every combination of Day and Process for each cause. However, Test Rate Across Groups only tests overall differences between groups.

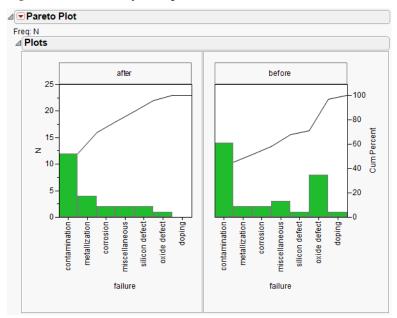
#### **One-Way Comparative Pareto Plot Example**

This example uses the Failure2.jmp sample data table. This table records failures in a sample of capacitors manufactured before cleaning a tube in the diffusion furnace and in a sample manufactured after cleaning the furnace. For each type of failure, the variable clean identifies the samples with the values "before" or "after."

- 1. Select **Help > Sample Data Library** and open Quality Control/Failure2.jmp.
- 2. Select Analyze > Quality and Process > Pareto Plot.
- 3. Select failure and click **Y**, **Cause**.
- 4. Select clean and click **X**, **Grouping**.
- Select N and click Freq.
- 6. Click OK.

Figure 13.14 displays the side-by-side plots for each value of the variable, clean.

Figure 13.14 One-way Comparative Pareto Plot



The horizontal and vertical axes are scaled identically for both plots. The bars in the first plot are in descending order of the *y*-axis values and determine the order for all cells.

7. Rearrange the order of the plots by clicking the title (*after*) in the first tile and dragging it to the title of the next tile (*before*).

A comparison of these two plots shows a reduction in oxide defects after cleaning. However, the plots are easier to interpret when presented as the before-and-after plot shown in Figure 13.15. Note that the order of the causes changes to reflect the order based on the first cell.

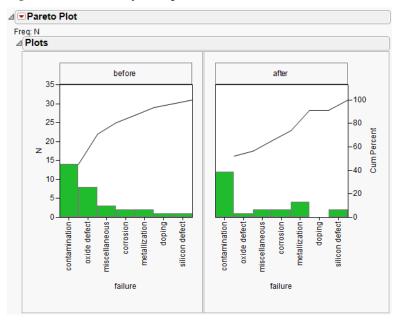


Figure 13.15 One-way Comparative Pareto Plot with Reordered Cells

# **Two-Way Comparative Pareto Plot Example**

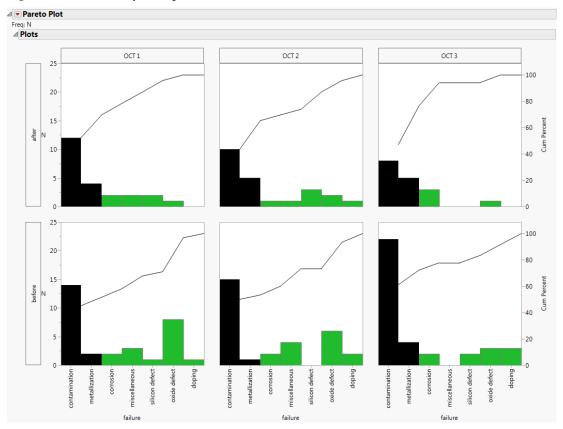
This example uses the Failure3.jmp sample data table. The data monitors production samples before and after a furnace cleaning for three days for a capacitor manufacturing process. The data table has a column called date with values OCT 1, OCT 2, and OCT 3.

- 1. Select **Help > Sample Data Library** and open Quality Control/Failure3.jmp.
- Select Analyze > Quality and Process > Pareto Plot.
- 3. Select failure and click **Y**, **Cause**.
- 4. Select clean and date and click **X**, **Grouping**.
- Select N and click Freq.
- 6. Click OK.

Figure 13.16 displays the Pareto plot with a two-way layout of plots that show each level of both *X* variables. The upper left cell is called the *key cell*. Its bars are arranged in descending order. The bars in the other cells are in the same order as the key cell.

7. Click Contamination and Metallization in the key cell and the bars for the corresponding categories highlight in all other cells.

Figure 13.16 Two-way Comparative Pareto Plot



The Pareto plot illustrates highlighting the *vital few*. In each cell of the two-way comparative plot, the bars representing the two most frequently occurring problems are selected. Contamination and Metallization are the two vital categories in all cells. After furnace cleaning, Contamination is less of a problem.

### Statistical Details for the Pareto Plot Platform

# **Likelihood Ratio Chi-Square Test**

#### Notation

The likelihood ratio Chi-square test statistic computed in the Pareto Plot platform uses the following notation:

•  $n_{ij}$  is the count for Cause i in Group j.

- $E_j$  is the expected count for Group j. This is the mean count of each group, across causes.
- $E_i$  is the expected count for Cause i. This is the mean count of each cause, across groups.

#### Likelihood Ratio Chi-Square Test Statistic within Groups

$$G_j^2 = 2\sum_{i=1}^K n_{ij} \ln(n_{ij}/E_j)$$

### Likelihood Ratio Chi-Square Test Statistic across Groups

$$G_i^2 = 2 \sum_{j=1}^{J} n_{ij} \ln(n_{ij}/E_i)$$

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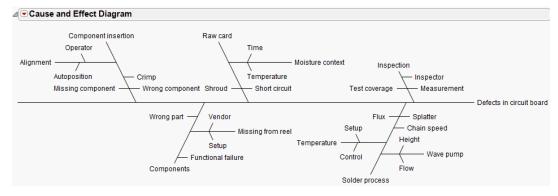
# **Cause-and-Effect Diagrams**

**Identify Root Causes** 

Use the Diagram platform to construct cause-and-effect diagrams, also known as *Ishikawa charts* or *fishbone charts*. Use these diagrams to:

- Organize the causes of an effect (sources of a problem)
- Brainstorm
- Identify variables in preparation for further experimentation

Figure 14.1 Example of a Cause-and-Effect Diagram



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## **Overview of Cause-and-Effect Diagrams**

Use the Diagram platform to construct cause-and-effect diagrams, also known as *Ishikawa charts* or *fishbone charts*. Use these diagrams to:

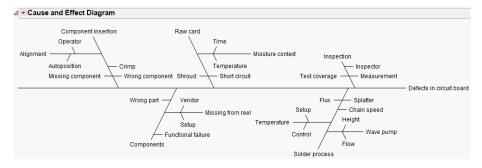
- Organize the causes of an effect (sources of a problem)
- Brainstorm
- Identify variables in preparation for further experimentation

# **Example of a Cause-and-Effect Diagram**

You have data about defects in a circuit board. You want to examine the major factors and possible causes of the defects in a diagram.

- 1. Select **Help > Sample Data Library** and open Ishikawa.jmp.
- 2. Select Analyze > Quality and Process > Diagram.
- 3. Select Parent and click **X**, **Parent**.
- 4. Select Child and click **Y**, **Child**.
- 5. Click **OK**.

Figure 14.2 Ishikawa.jmp Diagram



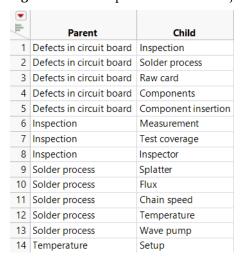
The major factors are Inspection, Solder process, Raw card, Components, and Component insertion. From each major factor, possible causes branch off, such as Inspection, Measurement, and Test coverage for the Inspection factor.

You can focus on one area at a time to further examine the possible causes or sources of variation for each major factor.

# **Prepare the Data**

Before you produce the diagram, begin with your data in two columns of a data table.

Figure 14.3 Example of the Ishikawa.jmp Data Table

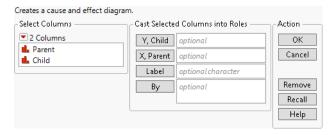


Notice that the Parent value Defects in circuit board (the effect) has five major factors, listed in the Child column. One of these major factors is Inspection, which has its own causes listed in the Child column. Parent values have children, and children can have their own children (and therefore be listed in both the Parent and Child columns.)

# **Launch the Diagram Platform**

Launch the Diagram platform by selecting Analyze > Quality And Process > Diagram.

Figure 14.4 The Diagram Launch Window



For more information about the options in the Select Columns red triangle menu, see *Using JMP*.

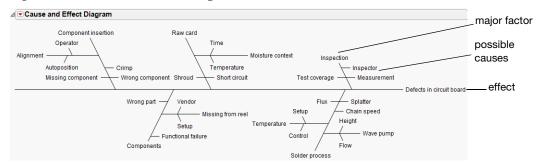
**Tip:** To create a basic diagram that is not based on a data table, leave the **Y, Child**, and **X, Parent** fields empty and click **OK**. Then edit the nodes using the options in the right-click menu. See "Right-Click Menus".

- **Y, Child** Represents the child factors contributing to the parent factors.
- **X**, **Parent** Represents the parent factors (including the effect) that have child factors.
- **Label** Includes the text from the Label columns in the nodes of the diagram.
- **By** Produces separate diagrams for each value of the By variable.

## The Cause-and-Effect Diagram

In Figure 14.5, the effect or problem, Defects in circuit board, appears on the right as the center line. The major contributing factors appear at the end of the branches (Inspection, Solder process, Raw Card, and so on.) Possible causes branch off each major factor.

**Figure 14.5** Cause-and-Effect Diagram



### **Right-Click Menus**

Right-click a highlighted node to modify text, insert new nodes, change the diagram type, and more. Note the following:

- Right-click a title to change the font and color, positioning, visibility, or formatting.
- Click and highlight a node to rename it.
- Click and drag a node to move it.

#### **Text Menu**

The Text menu contains the following options:

**Font** Select the font of the text or numeric characters.

**Color** Select the color of the text or numeric characters.

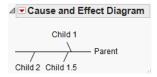
**Rotate Left, Rotate Right, Horizontal** Rotates the text or numbers to be horizontal, 90 degrees left, or 90 degrees right.

#### **Insert Menu**

Use the **Insert** menu to insert items onto existing nodes. The Insert menu contains the following options:

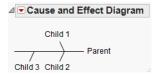
**Before** Inserts a new node to the right of the highlighted node. For example, Figure 14.6 inserts Child 1.5 before Child 2.

Figure 14.6 Insert Before



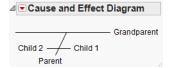
**After** Inserts a new node to the left of the highlighted node. For example, Figure 14.7 inserts Child 3 after Child 2.

**Figure 14.7** Insert After



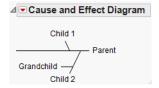
**Above** Inserts a new node at a level above the current node. For example, Figure 14.8 inserts Grandparent at a level above Parent.

Figure 14.8 Insert Above



**Below** Inserts a new node at a level below the current node. For example, Figure 14.9 inserts Grandchild at a level below Child 2.

Figure 14.9 Insert Below



#### Move Menu

Use the Move menu to move nodes or branches. The Move menu contains the following options:

**First** Moves the highlighted node to the first position under its parent.

**Last** Moves the highlighted node to the last position under its parent.

**Other Side** Moves the highlighted node to the opposite side of its parent line.

**Force Left** Makes all horizontally drawn elements appear to the left of their parent.

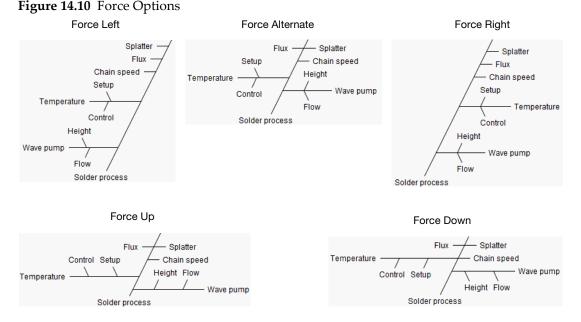
**Force Right** Makes all horizontally drawn elements appear to the right of their parent.

**Force Up** Makes all vertically drawn elements appear above their parent.

**Force Down** Makes all vertically drawn elements appear below their parent.

**Force Alternate** Draws children on alternate sides of the parent line.

T' 1110 F 0 11



#### **Other Menu Options**

The right-click menu for a highlighted node also contains these options:

**Change Type** Changes the entire chart type to **Fishbone**, **Hierarchy**, or **Nested**.

**Uneditable** Disables all other commands except **Move** and **Change Type**.

**Text Wrap Width** Specifies the width of labels where text wrapping occurs.

**Make Into Data Table** Converts the currently highlighted node into a data table. Convert the all nodes by highlighting the whole diagram (effect).

**Close** Shows the highlighted node.

**Delete** Deletes the highlighted node and all of its children.

## **Cause and Effect Diagram Menu Options**

The Cause and Effect Diagram red triangle menu contains the following options:

See *Using JMP* for more information about the following options:

**Redo** Contains options that enable you to repeat or relaunch the analysis. In platforms that support the feature, the Automatic Recalc option immediately reflects the changes that you make to the data table in the corresponding report window.

**Save Script** Contains options that enable you to save a script that reproduces the report to several destinations.

**Save By-Group Script** Contains options that enable you to save a script that reproduces the platform report for all levels of a By variable to several destinations. Available only when a By variable is specified in the launch window.

## Save the Diagram

There are different ways to save your diagram. Choose from one of the following:

- save the diagram as a data table
- save the diagram as a journal
- save the diagram as a script

### Save the Diagram as a Data Table

Note the following about this approach:

- If you have other processes that need to update the data table, this can be a good approach to choose.
- Very little customization is available, because the data table cannot represent the customization.

To save the diagram as a data table:

- 1. Highlight the entire diagram.
- 2. Right-click and select **Make Into Data Table**.
- Save the new data table.

### Save the Diagram as a Journal

Note the following about this approach:

- This option can be a good choice for impromptu work. For example, you can manually build the diagram, save it as a journal, then reopen the journal later and continue building and editing the diagram.
- Any customization exists only in the journal, and the journal is not connected to the data table.

To save the diagram as a journal:

- 1. Highlight the entire diagram.
- 2. Right-click and select **Edit > Journal**.
- 3. Save the new journal.

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### Save the Diagram as a Script

Note the following about this approach:

- If you have other processes that need to update the data table, this can be a good approach to choose.
- If you created the diagram from a data table, a simple script appears that relaunches against the data table with no customization.
- If you created the diagram without using a data table (or from a journal), a more complex script appears that contains all the commands needed to add and customize each area of the diagram.

*To save the diagram as a script:* 

- 1. Click the red triangle next to Cause and Effect Diagram and select **Save Script > To Script Window**.
- 2. Save the new script.

# Chapter 15

# **Quality Utilities**

## **Manage Specification Limits and Create OC Curves**

This chapter covers utilities in the Analyze > Quality and Process menu. Specifically, the Manage Spec Limits utility and OC Curves utility are discussed.

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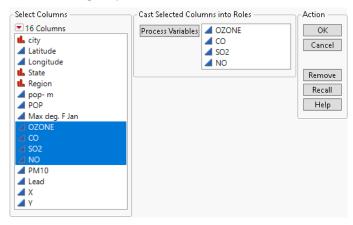
## **Manage Spec Limits Utility**

The Manage Spec Limits utility enables you to quickly add or edit many specification limits for several columns at once. The specification limits are then used in any future analyses. You can also specify importance values for each process and indicate whether limits should appear in graphs as reference lines.

### **Example of the Manage Spec Limits Utility**

- 1. Select **Help > Sample Data Library** and open Cities.jmp.
- 2. Select Analyze > Quality and Process > Manage Spec Limits.
- 3. Specify the columns that you want to set specification limits on. For this example, select OZONE, CO, SO2, and NO, and click **Process Variables**.

Figure 15.1 Specify Columns



- 4. Click OK.
- 5. Add your specification limits. You can do this by loading existing limits from a JMP data table (Load from Limits Table) or by entering limits manually. For this example, enter the following limits manually:
  - OZONE: LSL 0.12, USL 0.2
  - CO: LSL 6, USL 12
  - SO2: LSL 0.015, USL 0.06
  - NO: LSL 0.02, USL 0.04
- 6. Click the red triangle next to Manage Spec Limits and select **Show Limits All**.

Manage Spec Limits Utility

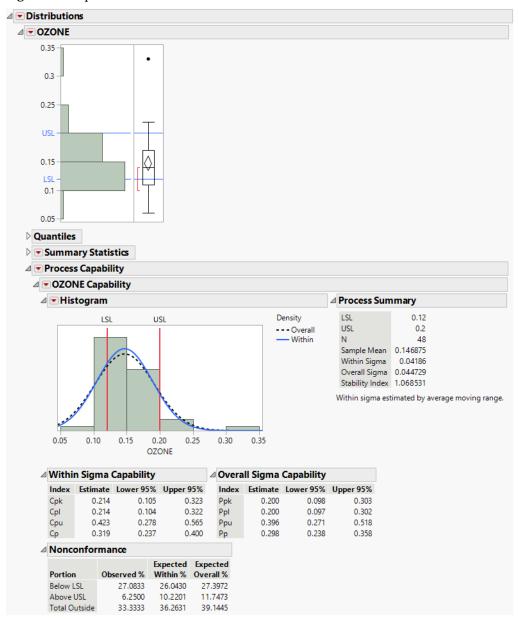
Specification limits for all columns will appear in graphs for any future analyses. If you want to show the specification limits only for individual columns, check the **Show Limits** box next to those columns.

Figure 15.2 Set Specification Limits

Column	LSL	Target	USL	Show Limits	Process Importance	Unit
OZONE	0.12		0.2	✓		
co	6		12	<b>✓</b>		
SO2	0.015		0.06	✓		
NO	0.02		0.04	✓		
	v Limits -> Shov	v as Graph Refere		ole		

- 7. Choose how you want to save the specification limits. For this example, click **Save to Column Properties**. This saves them as column properties in the corresponding data table.
  You could also save them to a new data table (tall or wide format).
  - In the Cities.jmp data table Columns panel, notice that asterisks indicating the Spec Limits column property appear next to OZONE, CO, SO2, and NO.
- 8. To see values that are outside the limits in the data table, click the red triangle next to Manage Spec Limits and select **Color Out of Spec Values**. Go to the Cities.jmp data table, and you can see that any values that are outside the limits are now colored.
- 9. Now, you can run any analysis. For this example, select **Analyze > Distribution**.
- 10. Select OZONE, CO, SO2, and NO, and click **Y, Columns**.
- 11. Click **OK**.

Figure 15.3 Specification Limits for OZONE in Distribution



The specification limits that you added to the OZONE column appear in the histogram. Because the column contains a Spec Limits column property, the Distribution report also contains a Capability Analysis report.

## **Manage Spec Limits Options**

In the window where you set specification limits, there are buttons to save and load specification limits, and options in the Manage Spec Limits red triangle menu.

#### Report Table Columns

The table at the top of the Manage Spec Limits report contains a row for each process column specified in the launch window. This table enables you to specify specification limits as well as the following options for each column:

**Show Limits** Specifies that the Show as Graph Reference Lines option is selected in the Spec Limits column property for the specified column.

**Process Importance** Specifies the process importance value for each column. Process importance values provide a mechanism to sort processes in the order that you prefer. Process importance values are used to size markers in many platform graphs.

**Units** Specifies the units for each column.

#### **Buttons**

**Load from Limits Table** Loads specification limits from a JMP data table.

**Save to Column Properties** Saves the specification limits as column properties in the associated data table.

**Save to Tall Spec Limits Table** Saves the specification limits to a new data table in tall format.

**Save to Wide Spec Limits Table** Saves the specification limits to a new data table in wide format.

#### **Red Triangle Options**

**Show Limits All** Selects boxes under Show Limits for all of the columns. If Show Limits is selected for a column, the Show as Graph Reference Lines option is selected in the Spec Limits column property. The Show as Graph Reference Lines option displays the specification limits and target that you specify as reference lines in select analysis plots.

**Note:** If all boxes under Show Limits are selected, the Show Limits All option deselects all of the boxes under Show Limits.

**Round Decimals** Sets the number of decimal places to which you want the specification limits rounded.

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**Color Out of Spec Values** Colors any values in the data table that are outside the specification limits for the columns.

See *Using JMP* for more information about the following options:

**Redo** Contains options that enable you to repeat or relaunch the analysis. In platforms that support the feature, the Automatic Recalc option immediately reflects the changes that you make to the data table in the corresponding report window.

**Save Script** Contains options that enable you to save a script that reproduces the report to several destinations.

## **Operating Characteristic Curves Utility**

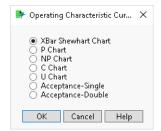
The Operating Characteristic (OC) Curves utility enables you to construct OC curves for control charts and attribute acceptance sampling plans. OC curves are available for XBar, P, NP, C, and U charts. For specified control charts, the OC curve shows the probability of failing to detect a shift of a particular size. In addition, there are OC curves for single and double attribute acceptance sampling plans. For a specified acceptance sampling plan, the OC curve shows how the probability of accepting a lot changes with the lot quality.

**Note:** The OC curves for control charts are two-sided curves. They are drawn for negative and positive shifts. Often OC curves display one curve for the absolute shift.

### Launch the OC Curves Utility

Launch the Operating Characteristic Curves by selecting **Analyze > Quality and Process > OC Curves.** Select the OC curve of interest and click OK to launch.

Figure 15.4 OC Curves Launch Window



### **OC Curves for Control Chart Options**

For control charts, you can use OC curves to explore how chart parameter settings impact  $\beta$ , which is the probability of failing to detect a specified shift of interest. Use the text boxes, sliders, or the LCL, Shift, and UCL handles on the OC curve to set and adjust chart parameters. The chart parameters are as follows:

**Lower Control Limit** Specifies the lower control limit from your control chart.

**Upper Control Limit** Specifics the upper control limit from your control chart.

**Sample Size** (Not available for C charts.) Specifies the sample size used for your control chart measure.

**Sigma** (Available only for XBar charts.) Specifies your control chart sigma.

**Shift** Specifies the shift to detect.

**Beta** Specifies the probability of failing to detect the specified shift given the control chart specifications. Beta updates as the specifications are changed.

## **OC Curves for Acceptance Sampling Options**

For attributes acceptance sampling, you can use OC curves to explore how sampling plans and assumed product quality impact the probability of accepting a lot. Use the text boxes, sliders, or fraction defective handle on the OC curve to set and adjust your sampling plan.

#### Single Sampling OC Curve Options

**Sampling Type** Enables you to select Lot Sampling or Binomial Sampling.

**Lot Sampling** Enables you to specify and explore an acceptance plan based on a fixed lot size.

**Binomial Sampling** Enables you to specify and explore an acceptance plan for a continuous process or other situation where the binomial distribution is appropriate.

**Lot size (N)** (Available only for Lot Sampling.) Specifies the size of the lot that you are sampling from.

**Sample Size (n)** Specifies the number of units for inspection.

**Acceptable failures (c1)** specifies the number of allowable failures. If the number of observed defects is greater than c1, then the lot is rejected.

**Fraction Defective** Specifies the expected fraction defective in the lot.

**Probability of Acceptance** Specifies the probability of accepting the lot given the sampling plan as defined. The Probability of Acceptance updates as the specifications are changed, but you can also adjust this value directly. When you adjust the Probability of Acceptance directly, the Fraction Defective value is updated.

#### Double Sampling OC Curve Options

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**First Sample** Contains the following settings for the first sample:

**Number inspected (n1)** Specifies the number of units inspected in the first sample.

**Acceptable failures (c1)** specifies the number of allowable failures in the first sample.

**Second Sample** Contains the following settings for the second sample:

**Number inspected (n2)** Specifies the number of units inspected in the second sample.

**Acceptable failures (c1+c2)** specifies the total number of allowable failures.

**Fraction Defective** Specifies the expected fraction defective in the lot.

**Probability of Acceptance** Specifies the probability of accepting the lot given the sampling plan as defined. The Probability of Acceptance updates as the specifications are changed, but you can also adjust this value directly. When you adjust the Probability of Acceptance directly, the Fraction Defective value is updated.

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# Appendix A

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